



NATIONAL RADIO ASTRONOMY OBSERVATORY



TOWARDS OPTICS DESIGN FOR THE ngVLA

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ngVLA

The Next Generation Very Large Array

Session J2: Next Generation Very Large Array

January 4, 2017

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- 2. CLASSICAL Vs. SHAPED**
- 3. SYMMETRIC/ASYMMETRIC ANTENNA**
- 4. VARIANCE OF DUAL-OFFSET ANTENNA**
- 5. OPTICS DESIGN CONCEPTS**
- 6. CONCLUSIONS**

INTRODUCTION

Sensitivity 10x VLA (35 GHz)

~300 antennas-18 m diameter; Diameters 12-25m considered

1.2-116 GHz

1.2-10.8 GHz (2 or 3 bands; $h_a = 0.65$)

11-50 GHz (3 bands; $h_a = 0.75$)

70-116 GHz (1 band; $h_a = 0.4, 0.3$)

Dual-offset reflector antenna

Shaping to optimize G/T_{sys}

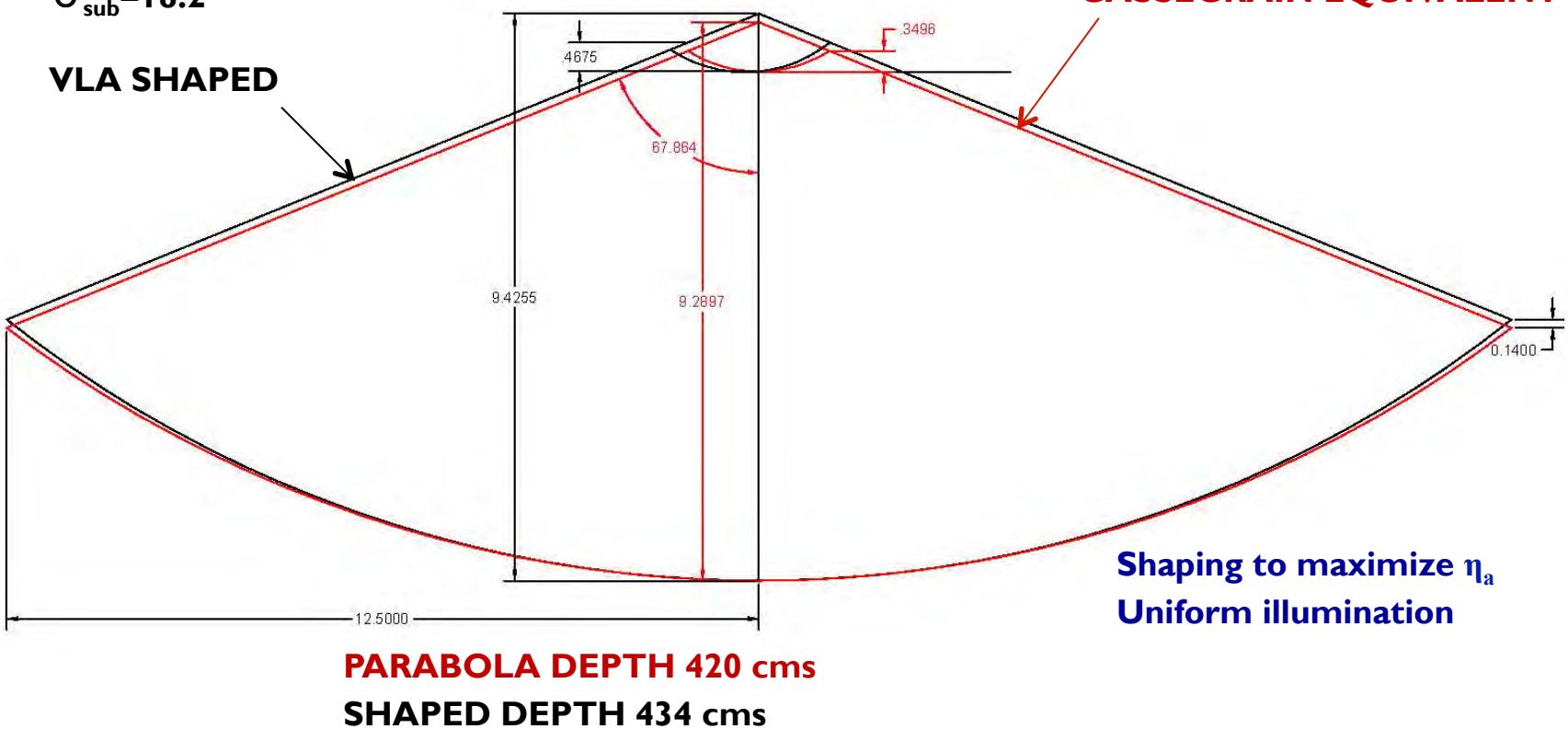
VLA (SHAPED) & CASSEGRAIN EQUIVALENT

CASSEGRAIN DEPTH 34.9 cms; Dia 2.35m

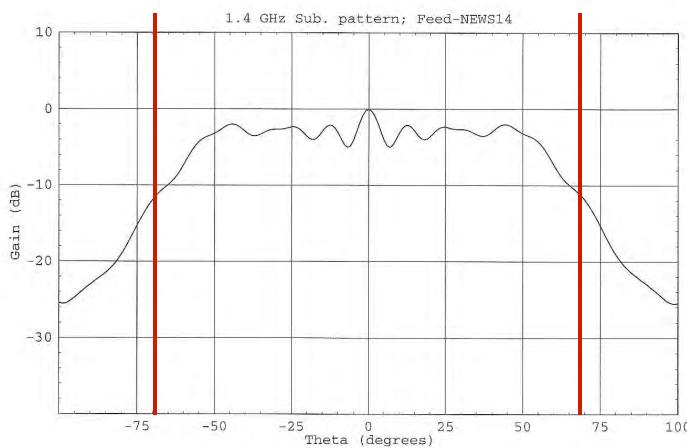
SHAPED DEPTH 46.7 cms

$$\Theta_{\text{sub}} = 18.2^\circ$$

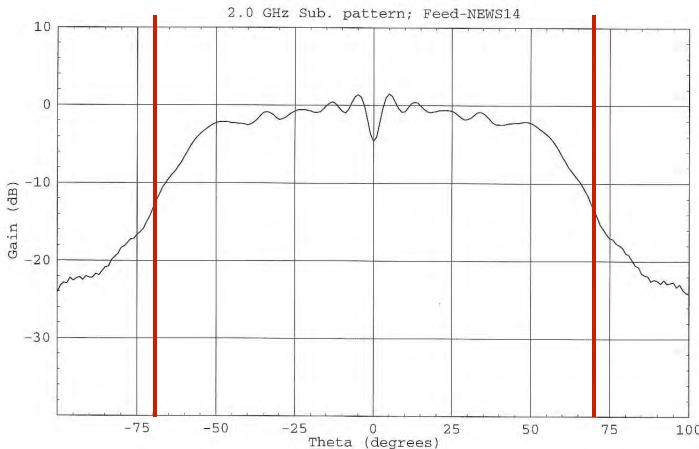
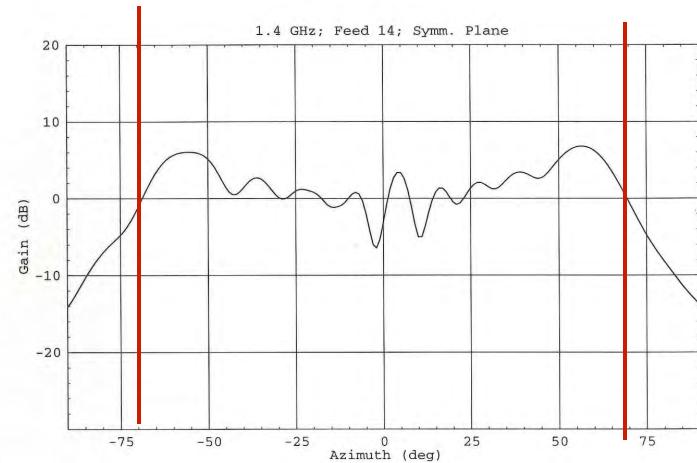
VLA SHAPED



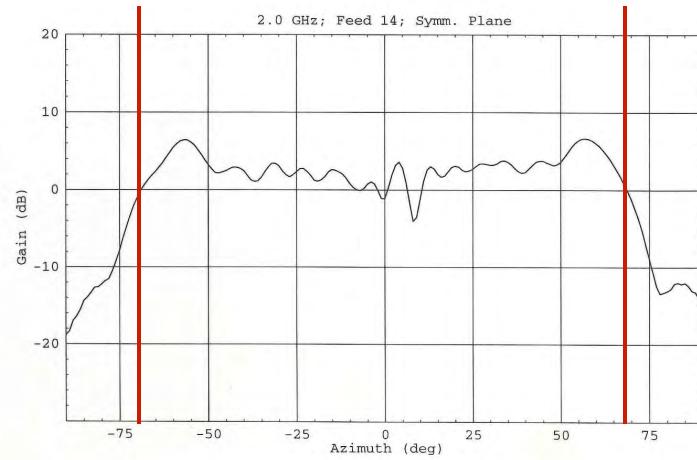
SUBREFLECTOR SCATTERED BEAM



1.4 GHz



2.0 GHz



HYPERBOLIC SUBREFLECTOR

$\Theta_{\text{edge}} = 67.86^\circ$

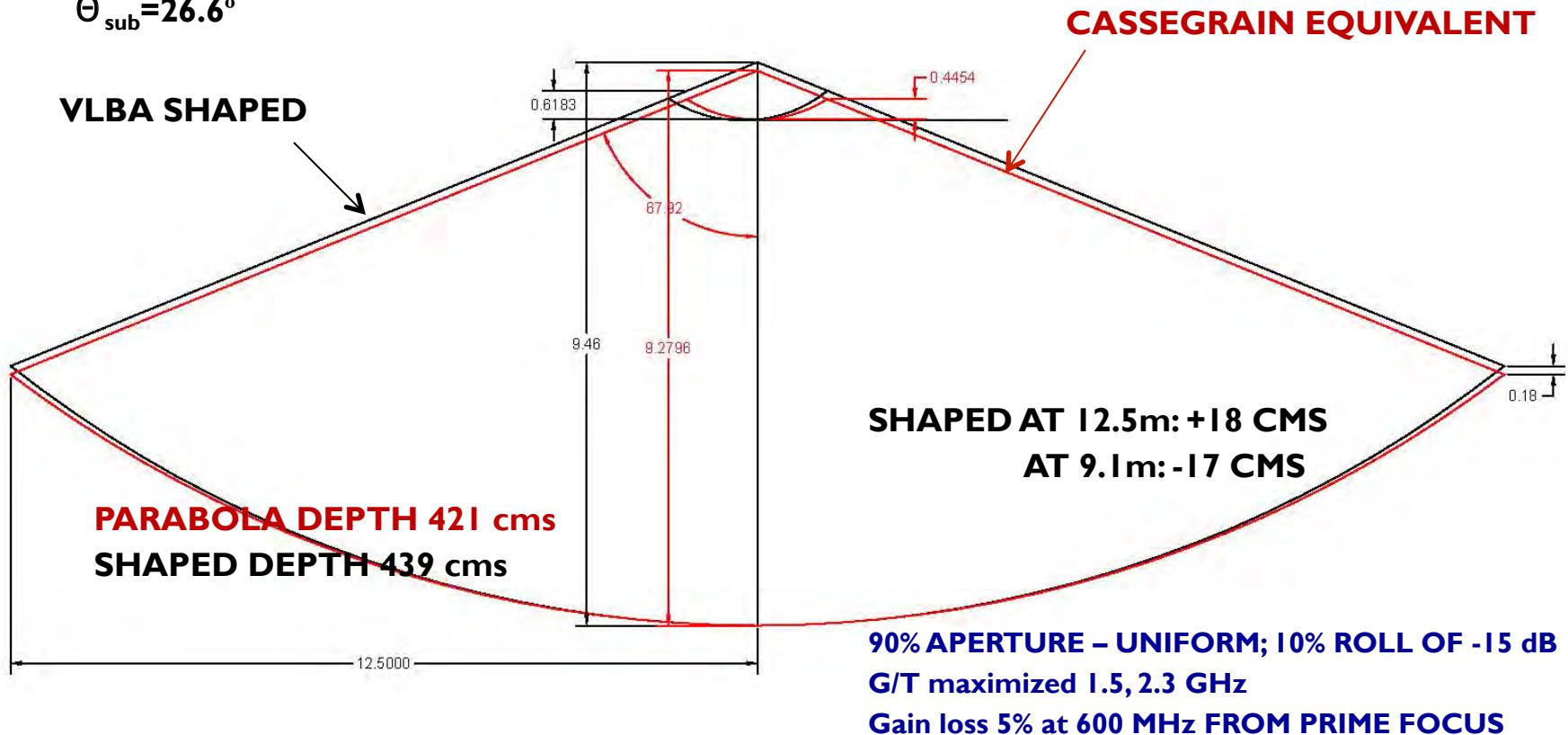
VLA SHAPED

VLBA (SHAPED) & CASSEGRAIN EQUIVALENT

CASSEGRAIN DEPTH 44.5 cms; Dia=3.2m

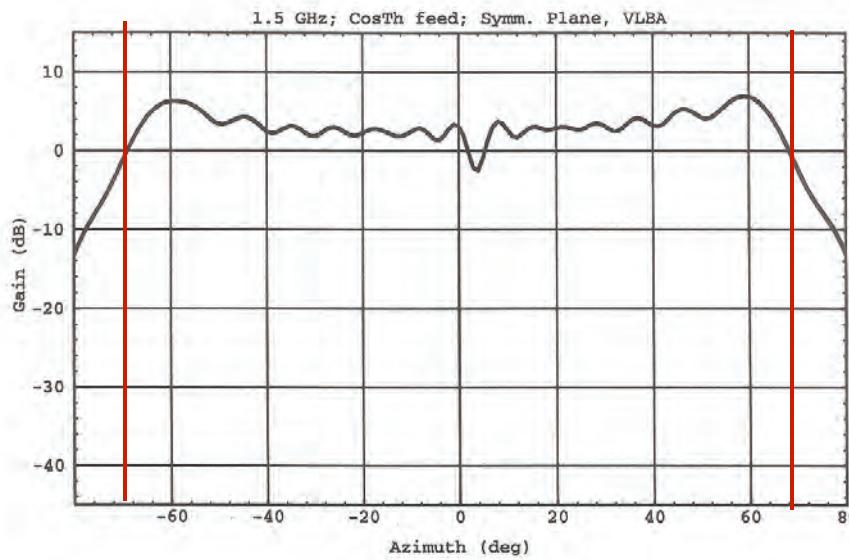
SHAPED DEPTH 61.8 cms

$$\Theta_{\text{sub}} = 26.6^\circ$$

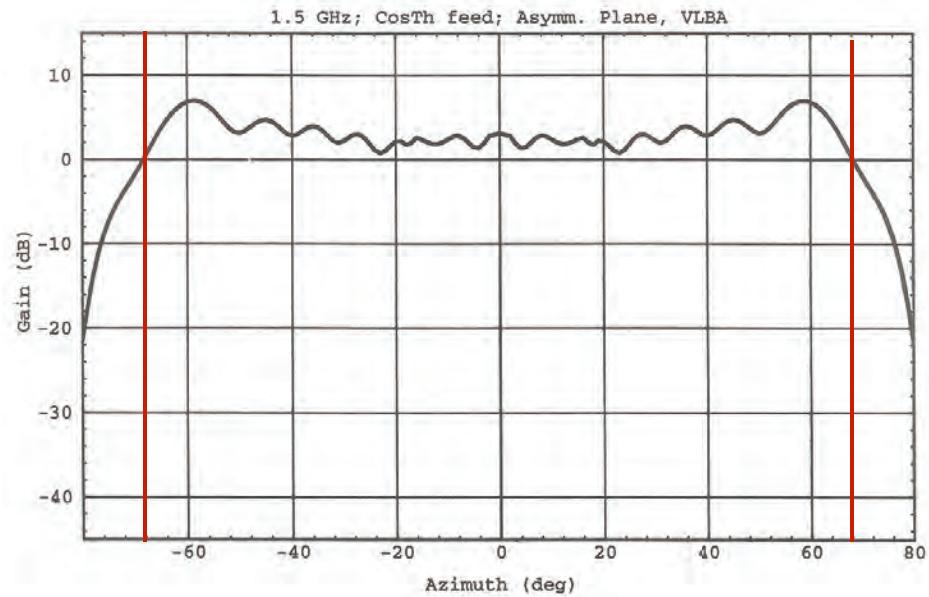


SUBREFLECTOR SCATTERED BEAM (1.5 GHz)

$$\Theta_{\text{edge}} = 67.92^\circ$$



SYMMETRIC PLANE



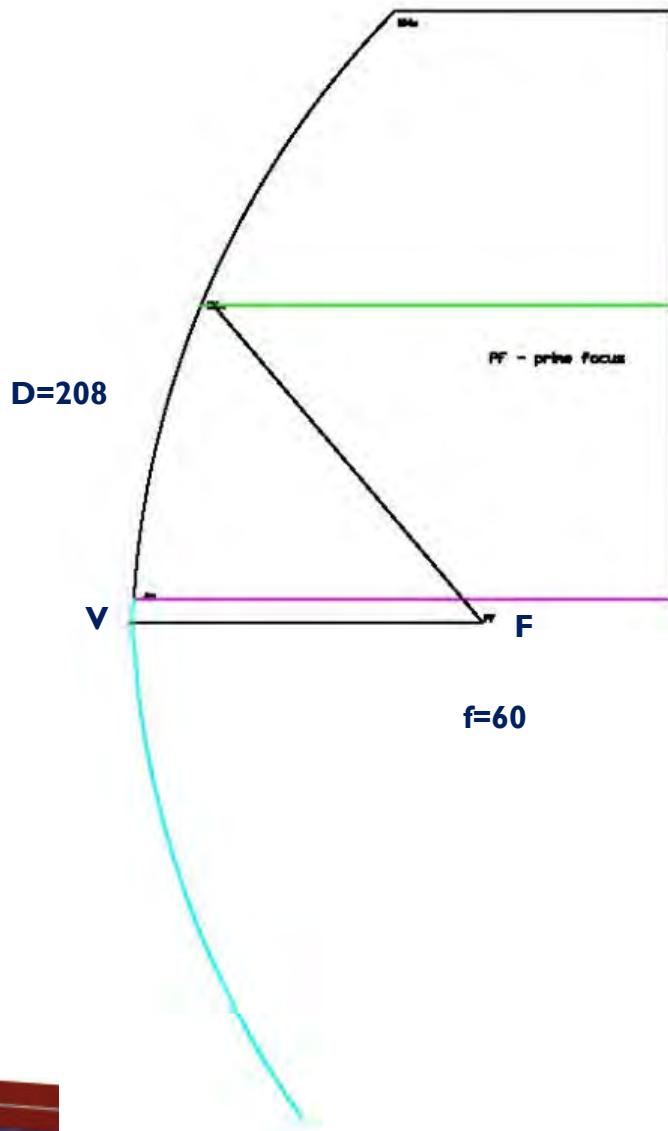
ASYMMETRIC PLANE

More uniform illumination and faster roll-off

DISADVANTAGES OF SHAPING

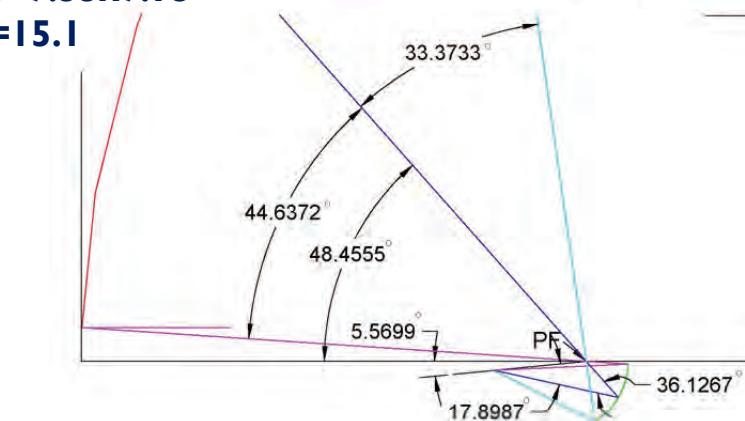
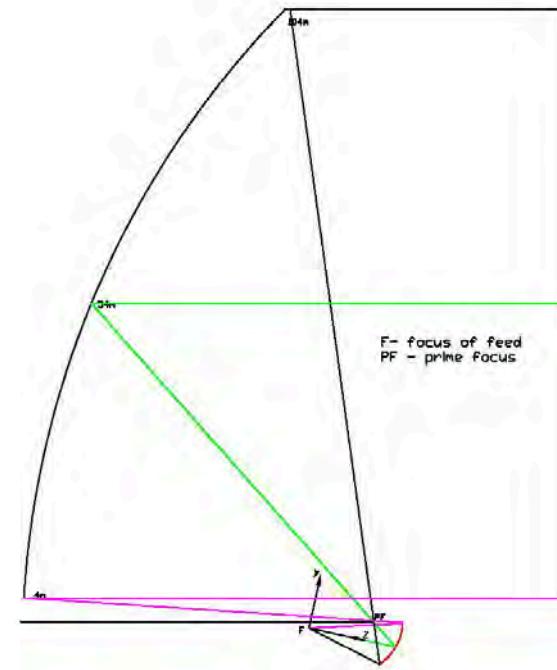
- 1. FREQUENCY DEPENDENT**
- 2. LIMITED FIELD OF VIEW**
- 3. LOSS IN GAIN FROM PRIME FOCUS**
- 4. RELATIVELY LARGER FEED HORNS (MORE SEVERE ILLUMINATION TAPER)**

DUAL-OFFSET ANTENNA (GBT)



CYLINDER DIA 100
CENTER AT 54

ecc=0.528
Yc=54, f=60
fellip=11
M = 3.17
Sub=7.55x7.95
FA=15.1



UNBLOCKED APERTURE Vs SYMMETRIC



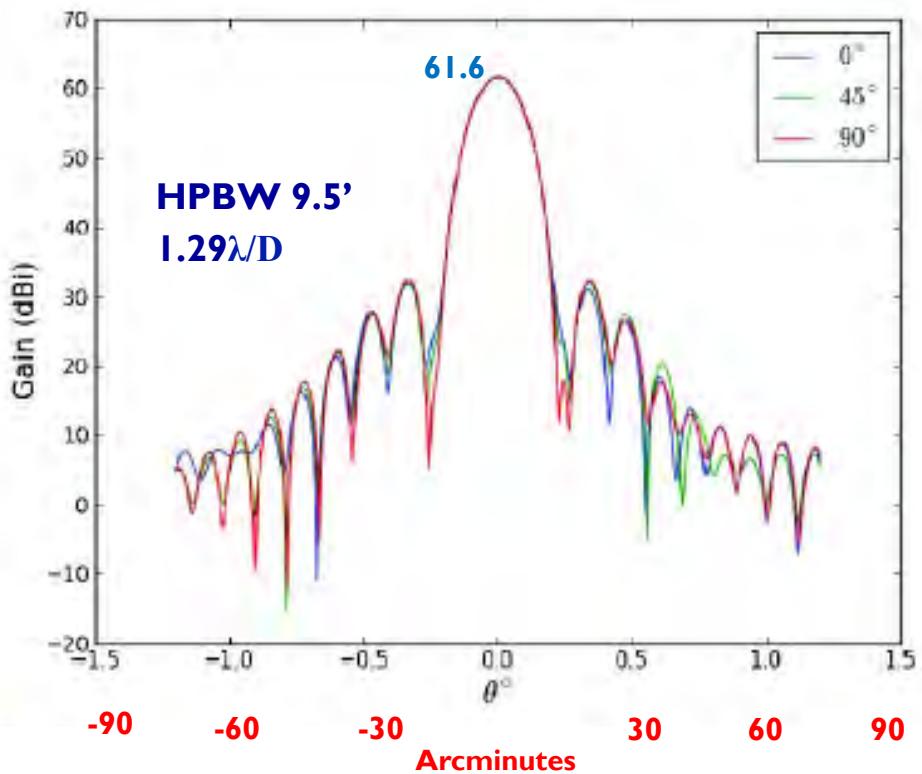
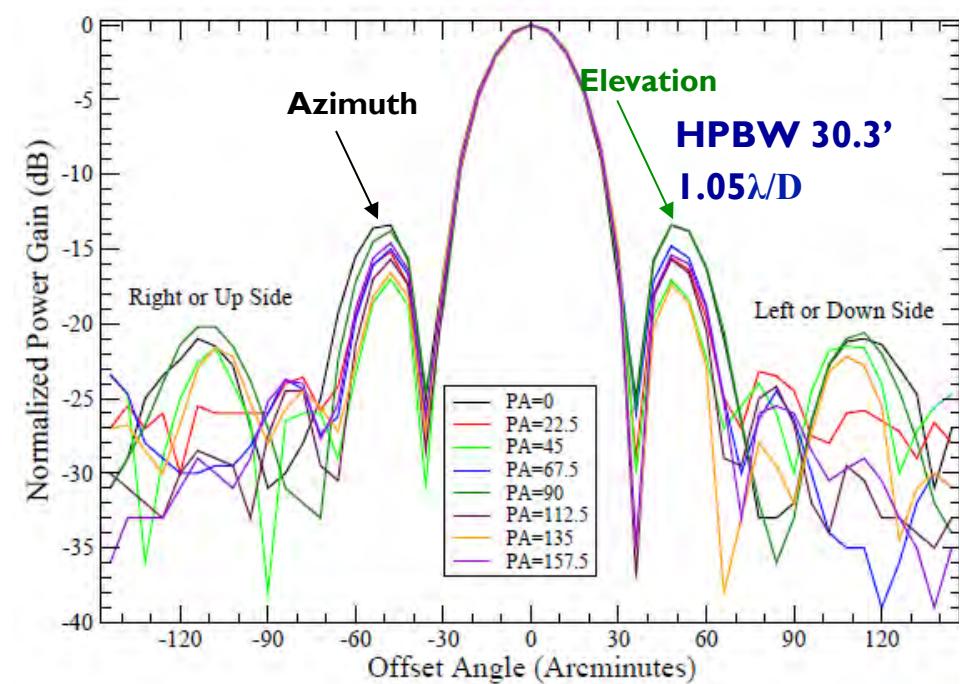
ADVANTAGES:

- Higher aperture efficiency 3 to 5%
- Lower side lobes ~15 dB
- Lower T_{antenna} ~3K
- Minimized standing waves ~25 dB
- Larger real estate

DISADVANTAGES:

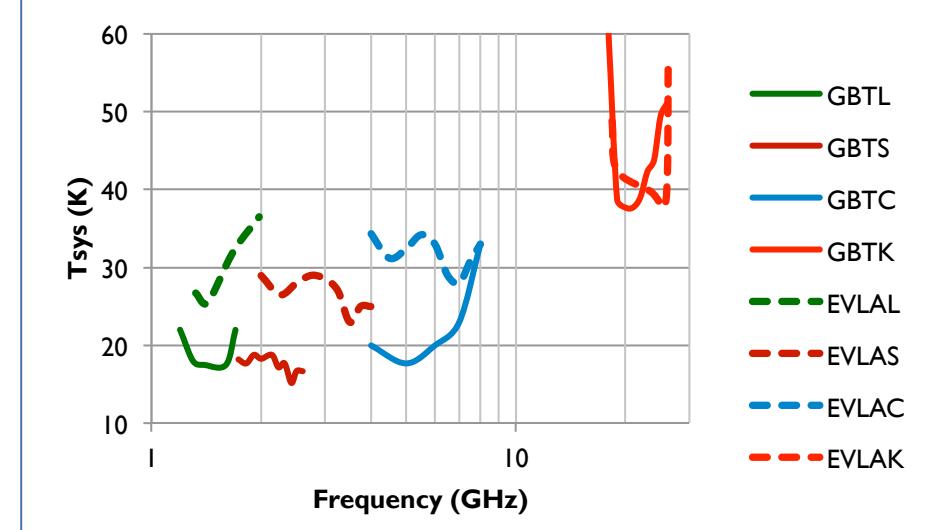
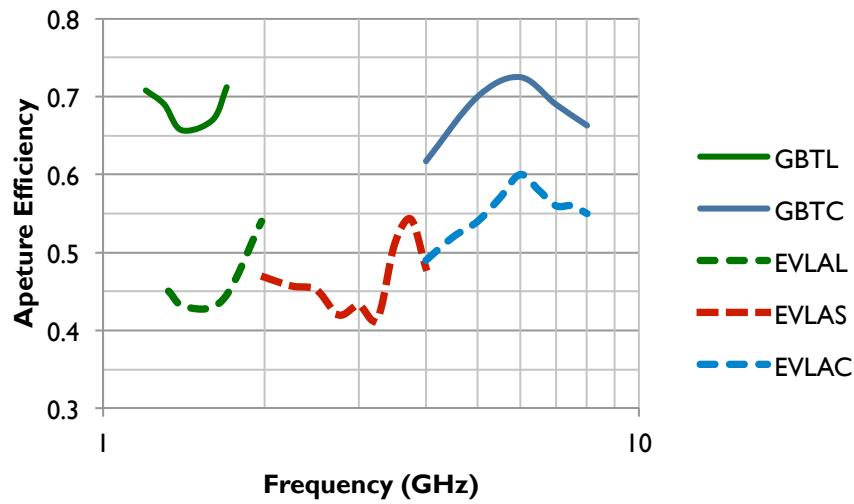
- Complex structure
- Poorer polarization performance – prime focus
- Higher scan loss
- Requires turret rotation/translation

BEAM OF THE EVLA (1.425 GHz) & GBT (1.4 GHz)

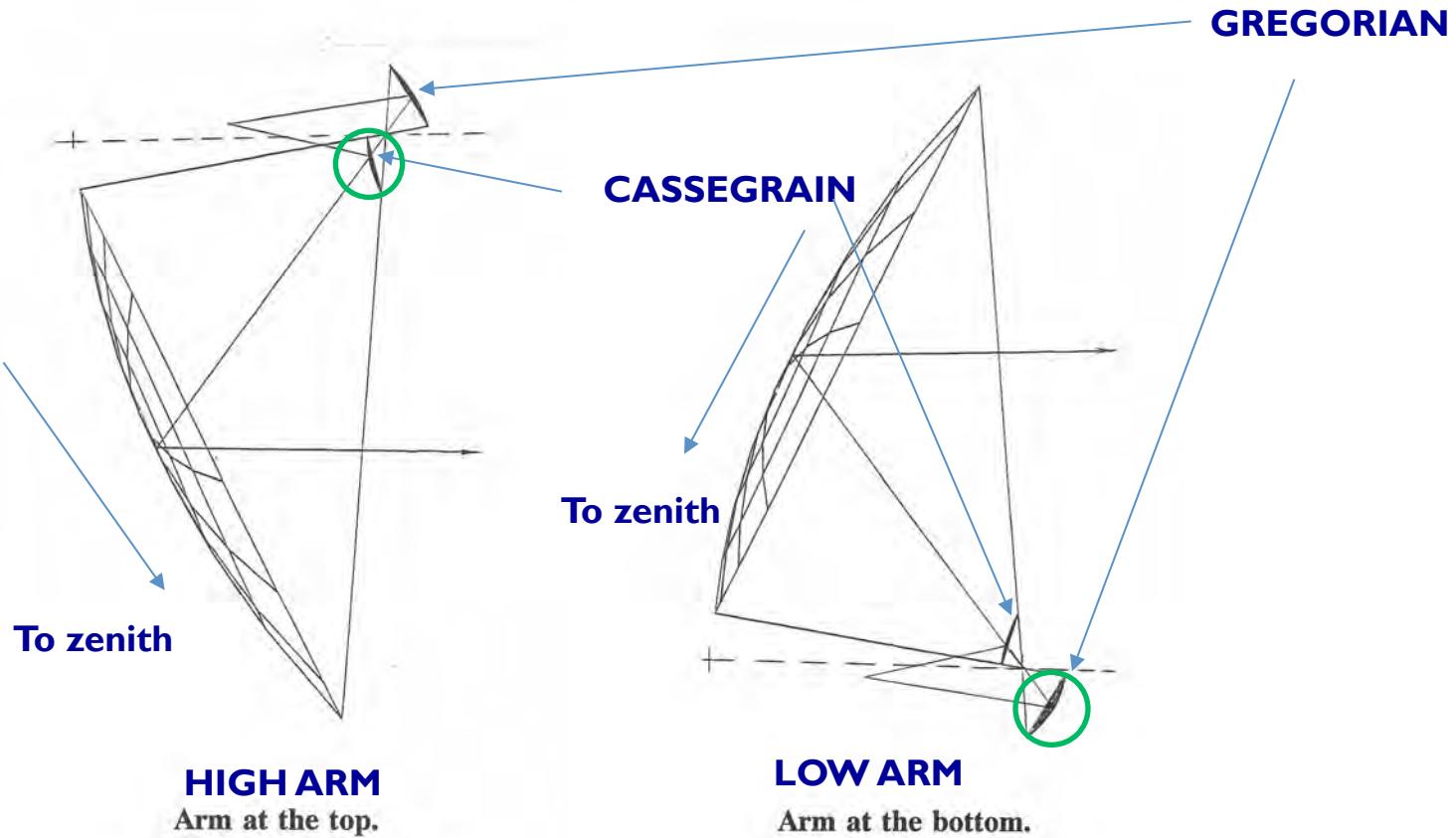


R. Perley et al., “Testing of the EVLA L-Band Feed”,
EVLA Memo 85

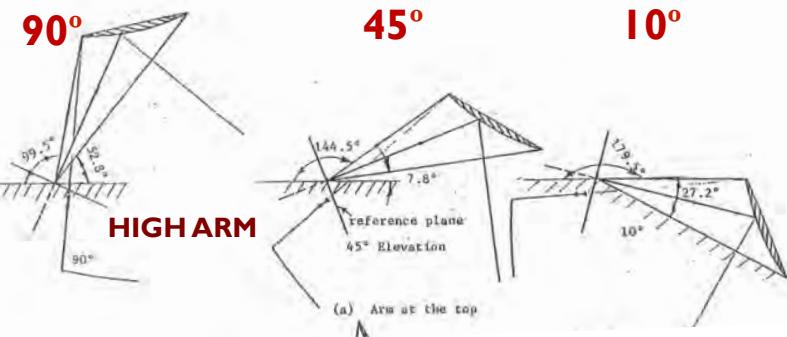
APERTURE η AND SYSTEM TEMPERATURE



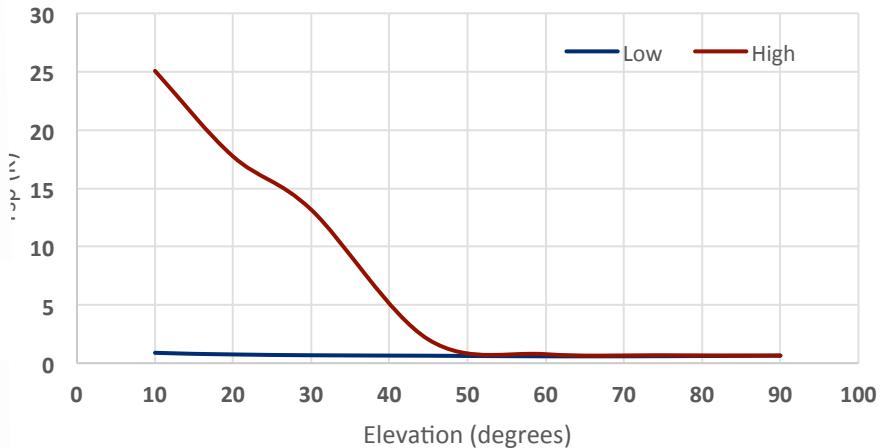
DUAL-OFFSET CASSEGRAIN, GREGORIAN ANTENNA



FORWARD SPILLOVER – PAST SUBREFLECTOR



Forward Spillover - Cassegrain subreflector



Forward Spillover - Gregorian subreflector

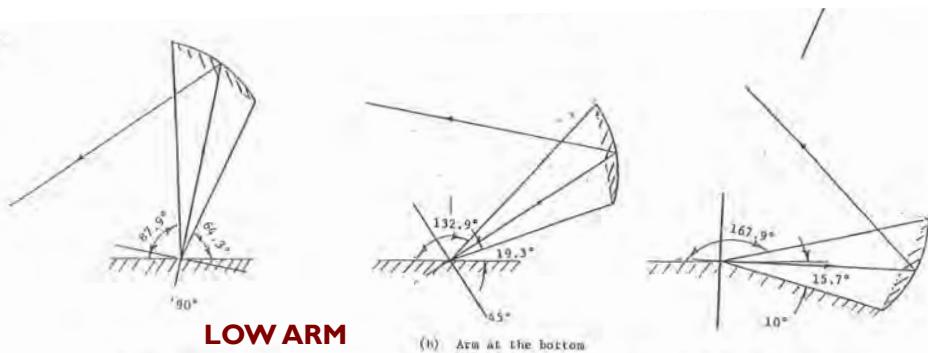


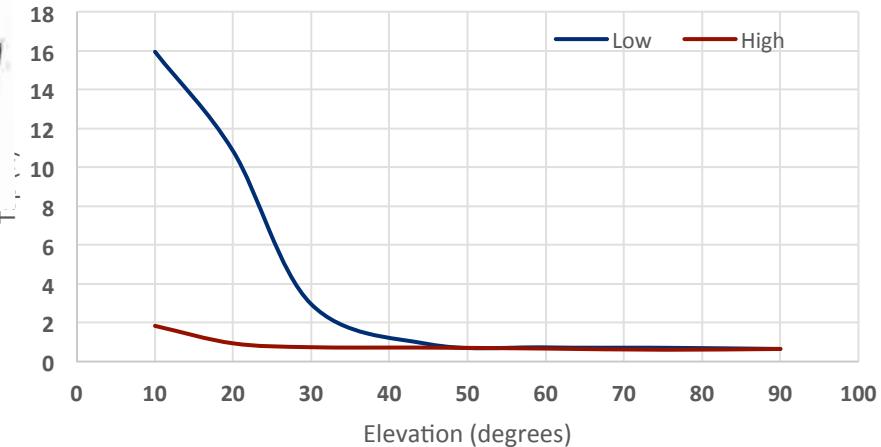
FIG. 4. Forward Spillover. Gregorian Subreflector Orientation with Respect to Ground (shaded).

90° 45° 10°

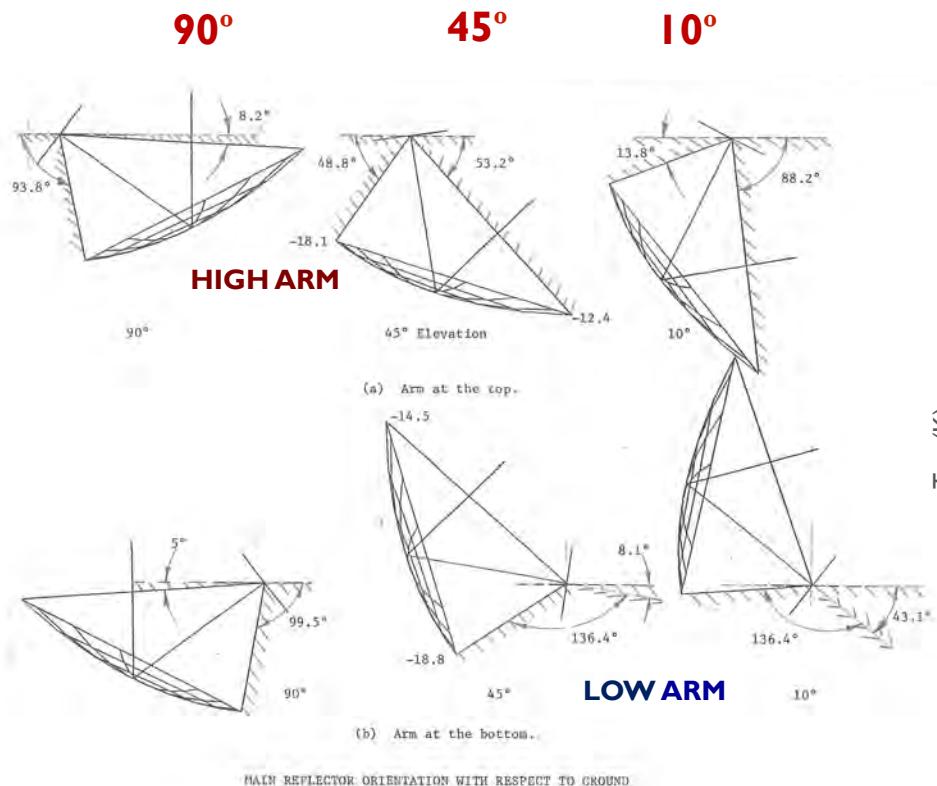
1.42 GHz; -12 dB taper

$D_{\text{sub}} = 35\lambda$; $\Theta_{\text{sub}} = 28^\circ$

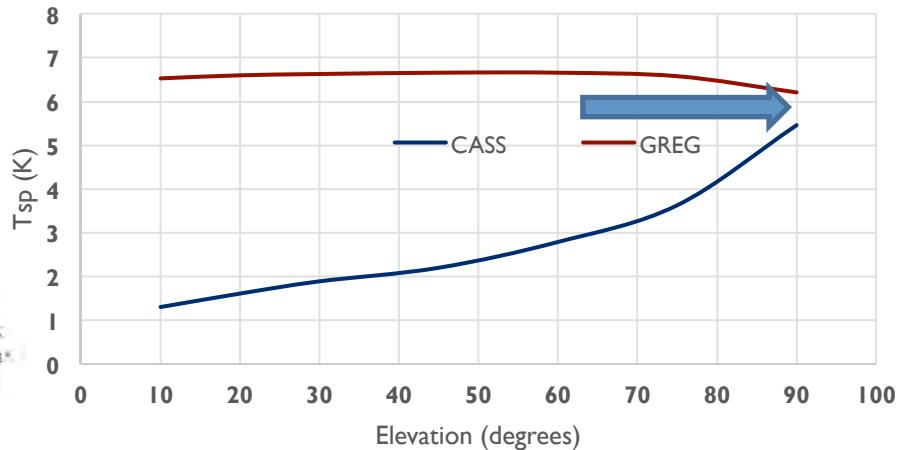
S. Srikanth, "Spillover noise temperature calculations for the Green Bank clear aperture antenna," GBT Memo #16, October 4, 1989.



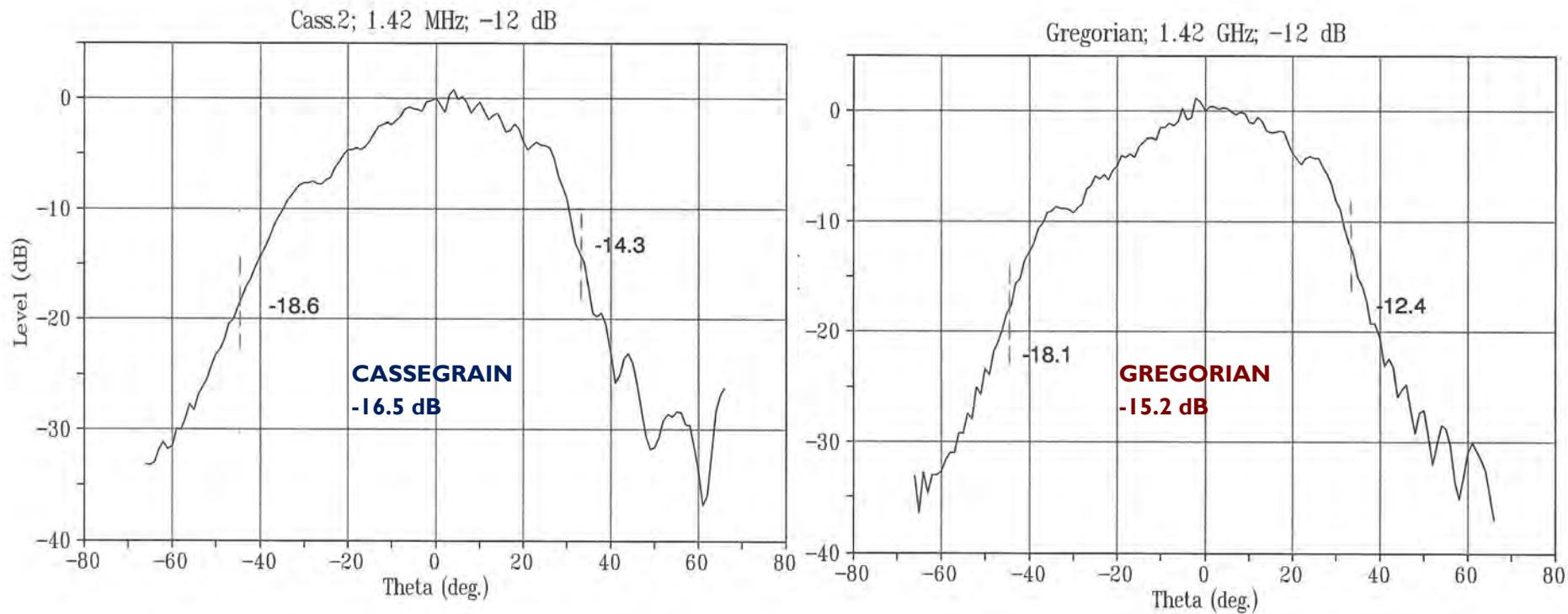
REAR SPILLOVER – LOW CASS., HIGH GREG.



Rear Spillover - Low Cass, High Greg



SUBREFLECTOR SCATTERED PATTERN



DIFFRACTION LOSS

Lateral extent of the transition region of edge diffracted field

$$\Delta\rho = \sqrt{\lambda / \pi} S_a / 1 \pm S_a / |\rho r| /$$

S_a – distance between edges of subreflector
and main reflector

ρ_r – subreflector edge to prime focus distance

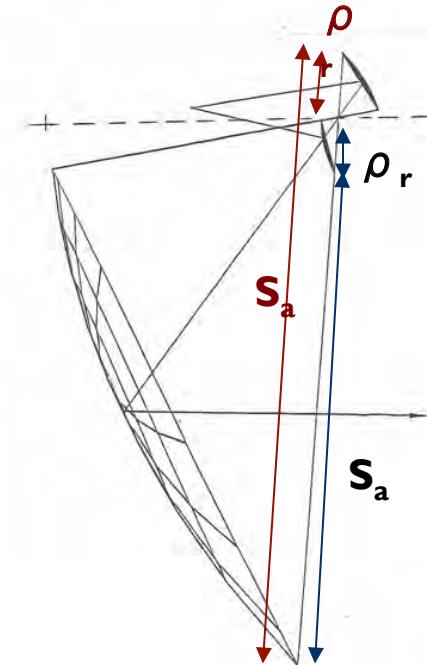
$\Delta\rho_{\text{gregorian}} > \Delta\rho_{\text{cassegrain}}$

Spillover past main reflector for -10 dB taper

$$\Delta\rho = 0.09 \Delta\rho_a / D$$

$\Delta\rho_a$ – average of $\Delta\rho$ of the two edges

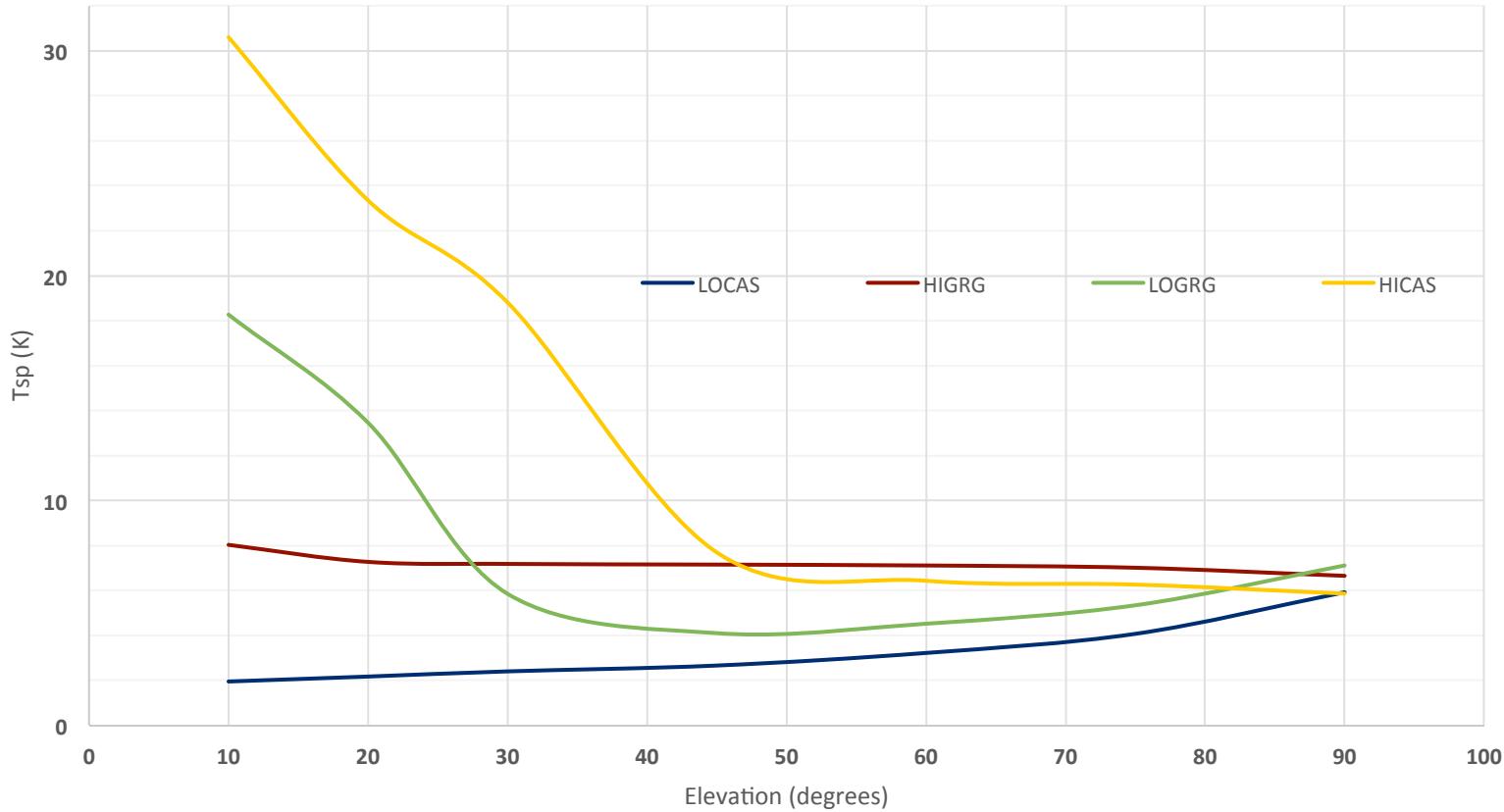
D – diameter of main reflector



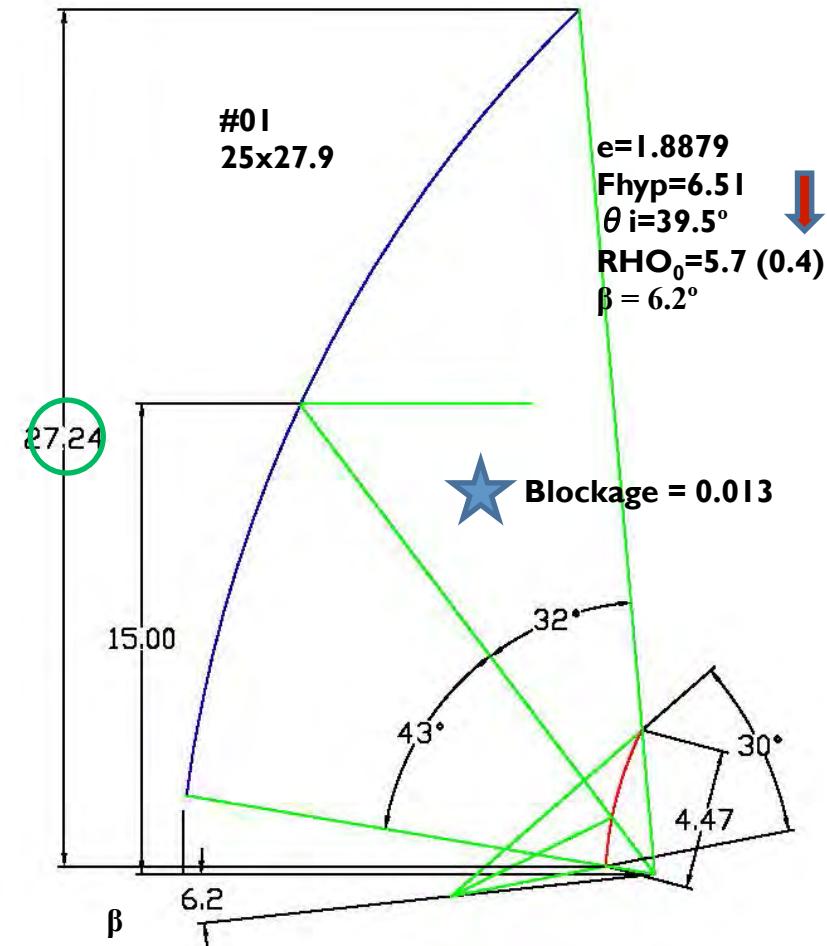
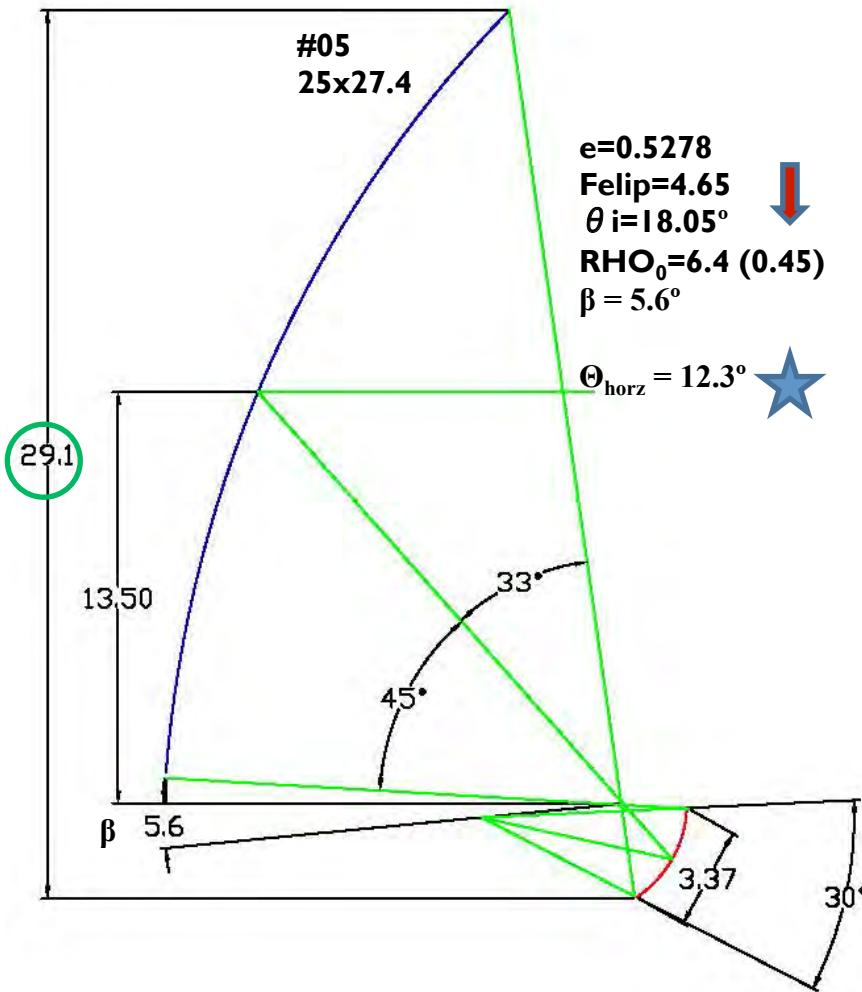
1. P. Kildal and J. Stamnes "Asymptotic transition region theory for edge diffraction, Part I and Part II," IEEE Trans. Antennas and Propagation, Sept. 1990. AP-S Digest pp. 1350-1373
2. Private commn. P. Kildal Sept. 19, 1990.

TOTAL SPILLOVER

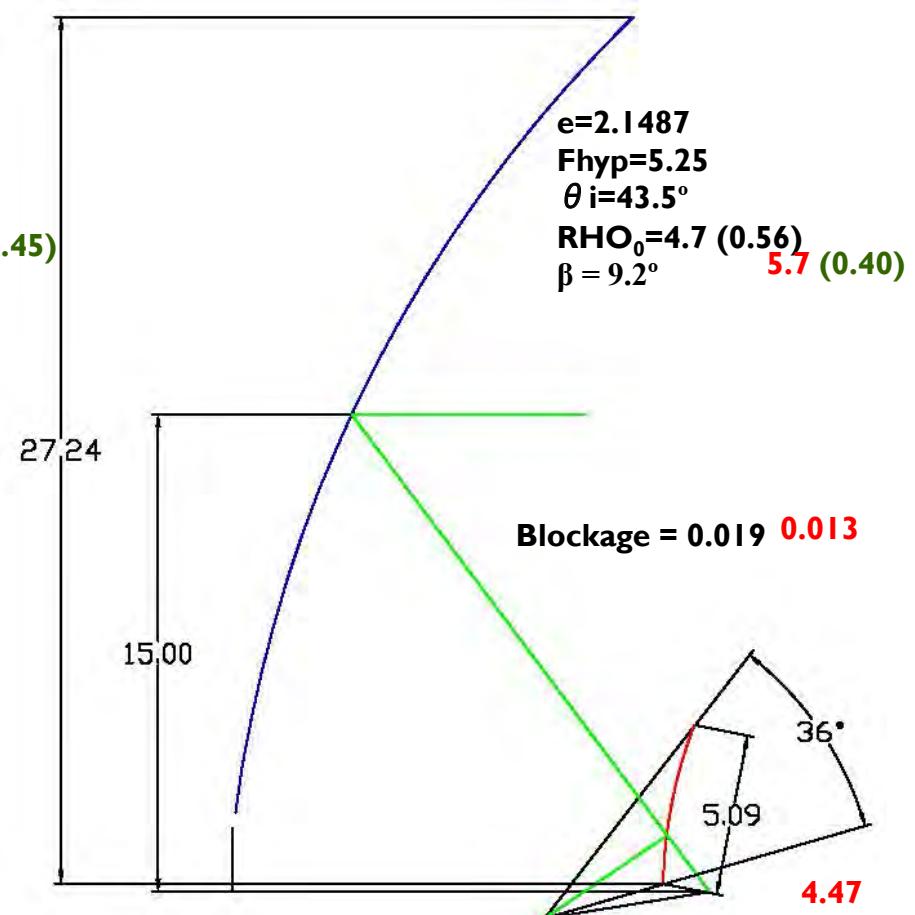
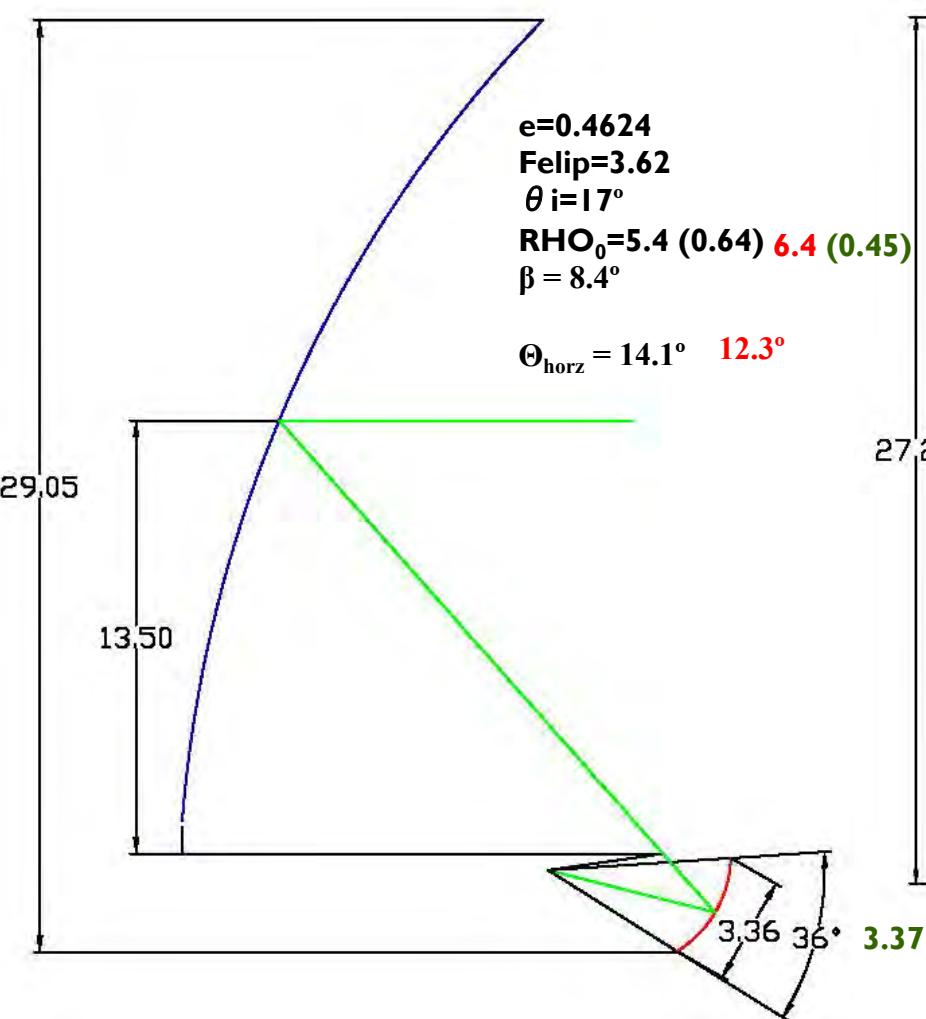
Total Spillover 1.4 GHz



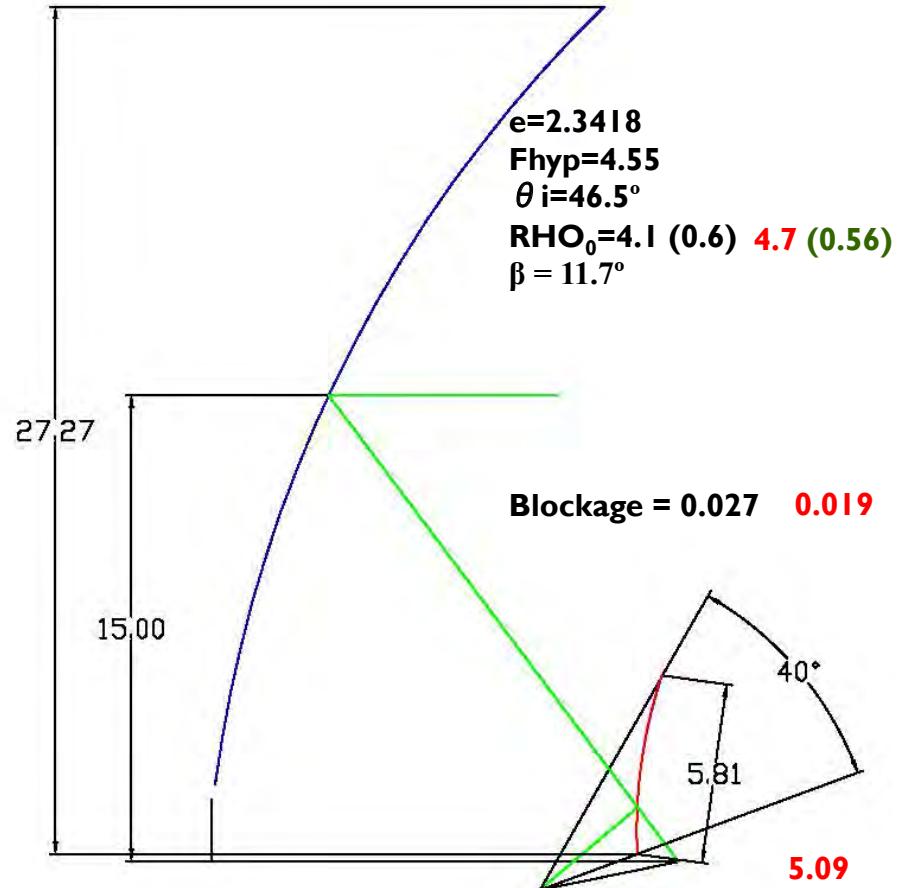
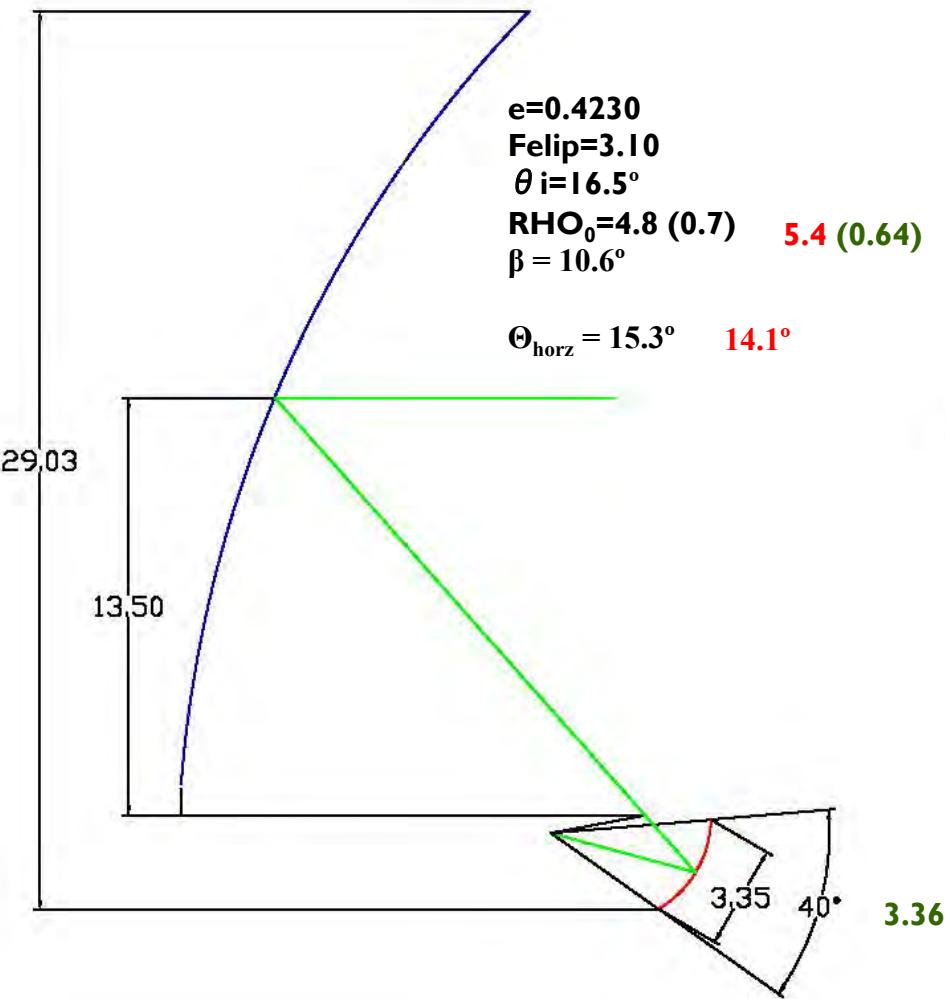
25m MAIN; F=15m; $\theta_{\text{sub}}=30^\circ$



25m MAIN; F=15m; $\theta_{\text{sub}}=36^\circ$



25m MAIN; F=15m; $\theta_{\text{sub}}=40^\circ$



COMPACT FEED HORN – 1.2 to 2.4 GHz

At 15°: -13.1 dB

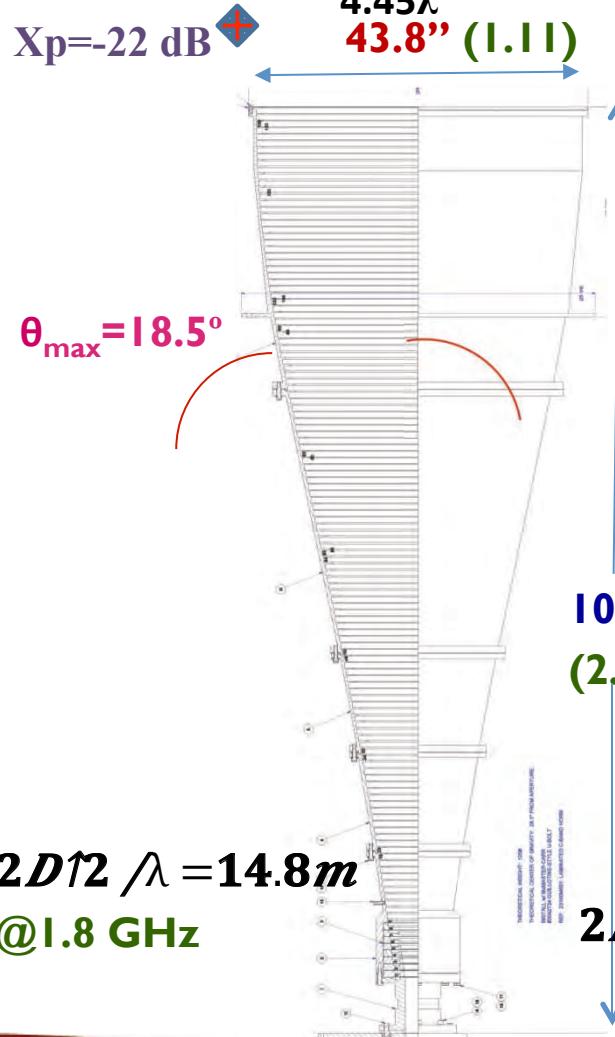
-13.2 dB

$$\theta_{\text{SUB}} = 30^\circ$$

$$4.45\lambda$$

$$43.8'' \text{ (1.11)}$$

$$X_p = -22 \text{ dB} \quad +$$



At 18°: -13.1 dB

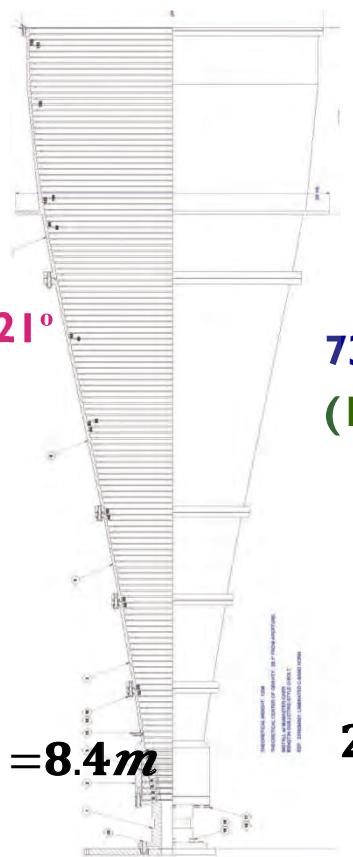
-12.5 dB

$$\theta_{\text{SUB}} = 36^\circ$$

$$3.34\lambda$$

$$32.9'' \text{ (0.84)}$$

$$X_p = -19.1 \text{ dB} \quad +$$



At 20°: -13.4 dB

-12.6 dB

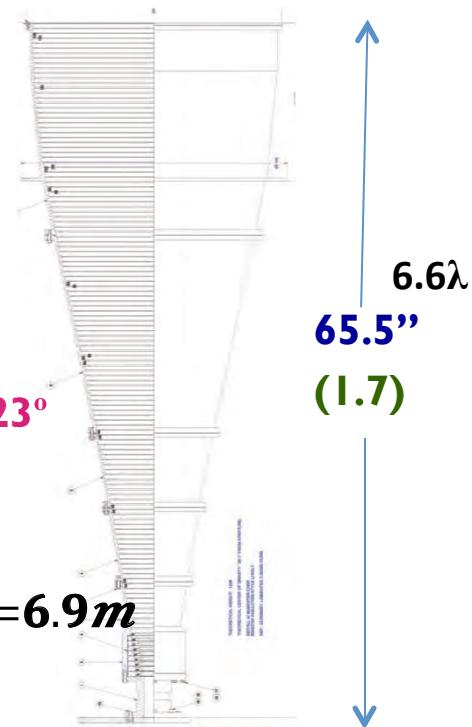
$$X_p = -18.3 \text{ dB} \quad +$$

$$\theta_{\text{SUB}} = 40^\circ$$

$$3.03\lambda$$

$$29.8'' \text{ (0.76)}$$

(m)



LINEAR TAPER FEED HORN – 11 to 18 GHz

At 15°: -13.0 dB

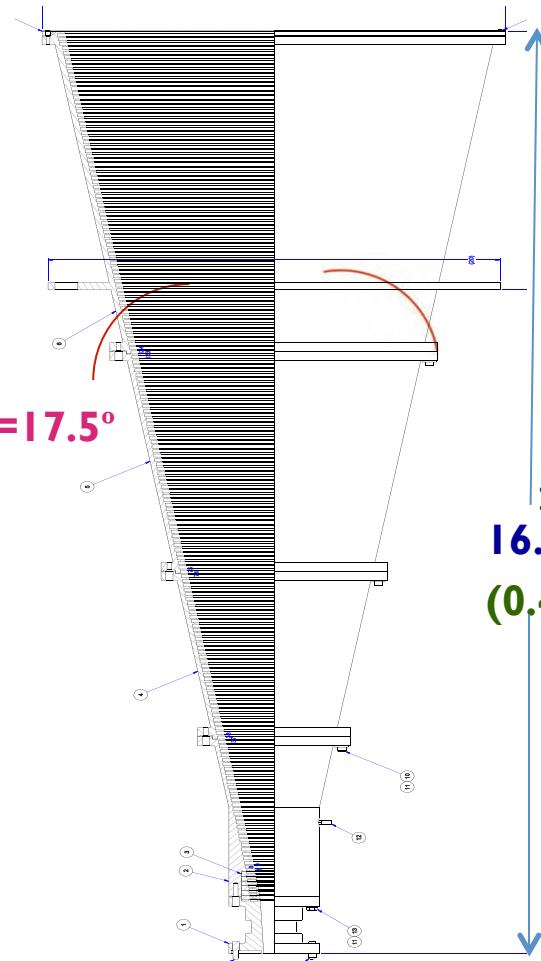
-12.9 dB

$$\theta_{\text{SUB}} = 30^\circ$$

8.5λ

9.10" (0.231)

Xp=-26 dB



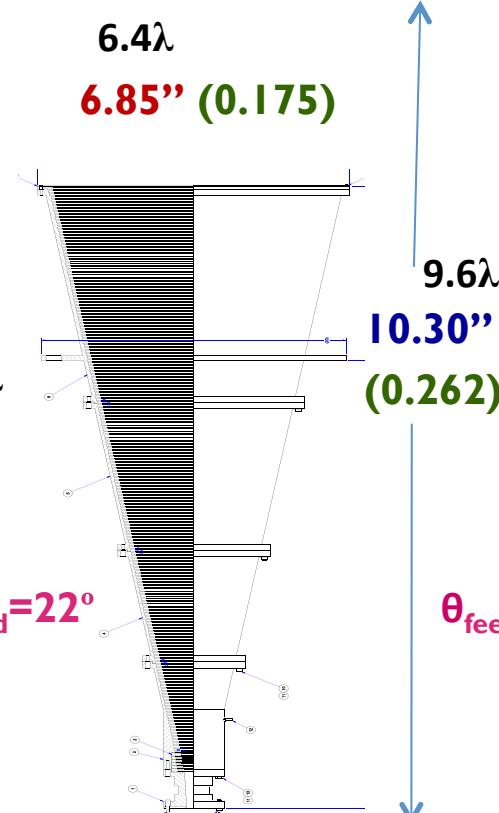
At 18°: -12.8 dB

-12.7 dB,

Xp=-25.4 dB

$$\theta_{\text{SUB}} = 36^\circ$$

6.4λ
6.85" (0.175)



At 20°: -12.5 dB

-12.6 dB

Xp=-23.1 dB

(m)

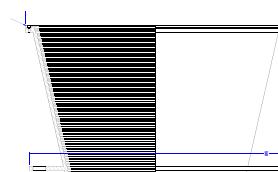
$$\theta_{\text{SUB}} = 40^\circ$$

5.7λ

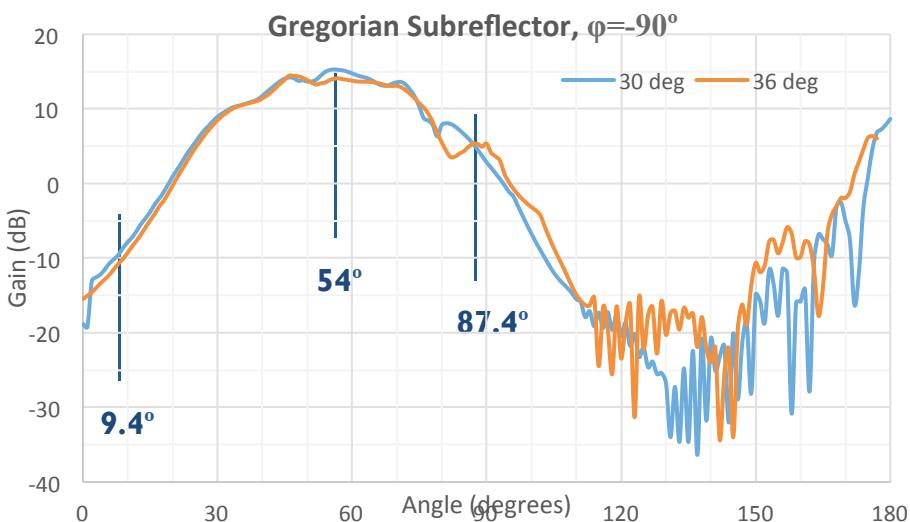
6.14" (0.156)

8.1λ
8.70"
(0.221)

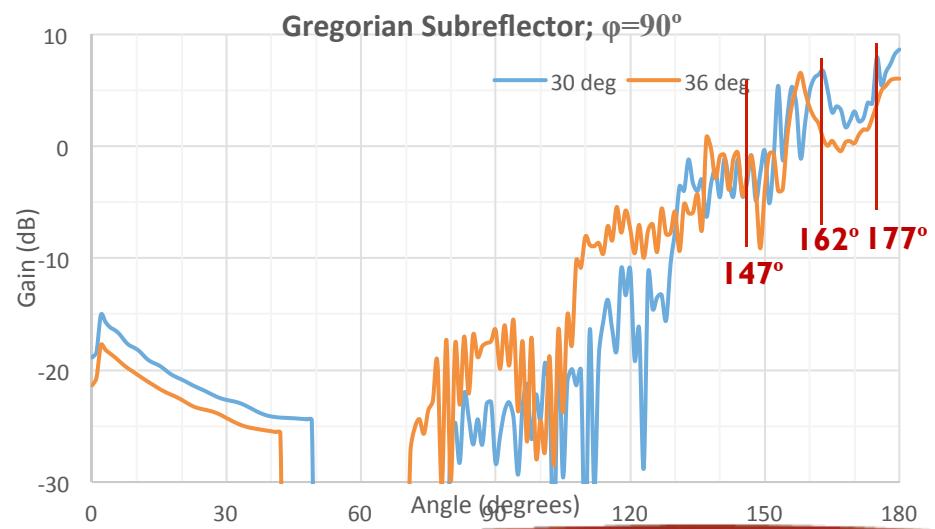
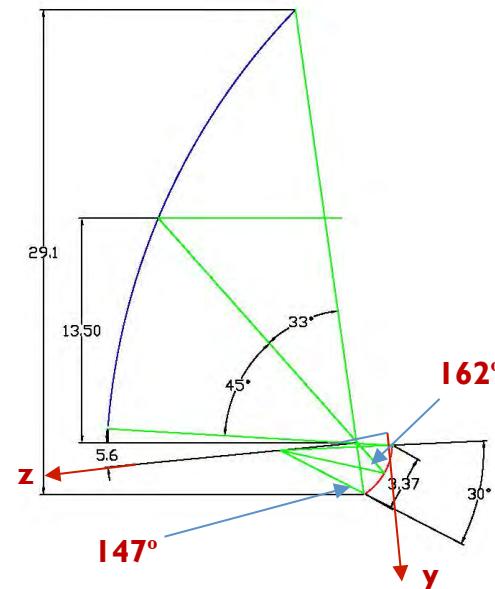
$$\theta_{\text{feed}} = 24.5^\circ$$



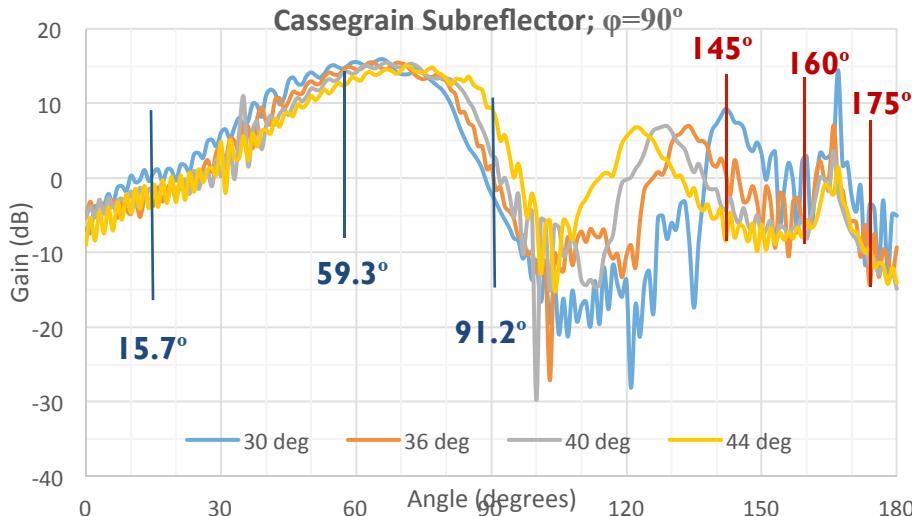
GREGORIAN SUBREFLECTOR SCATTERED PATTERN



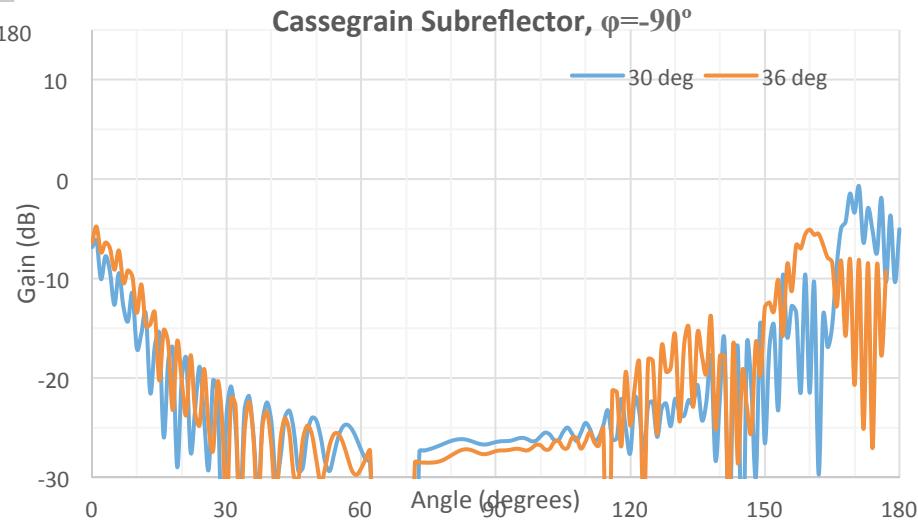
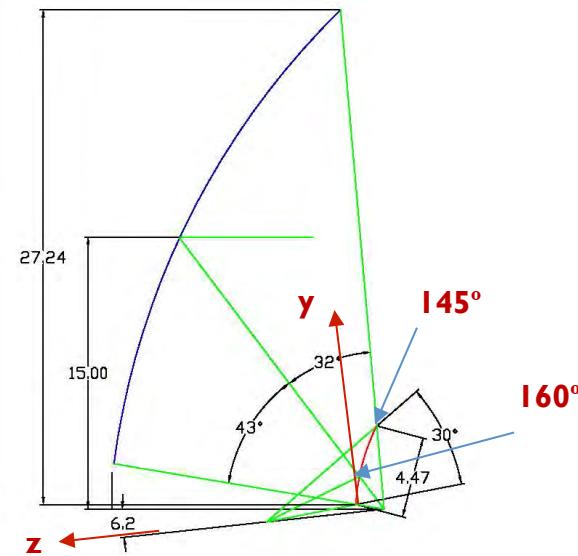
1.6 GHz
At 15° -13.7 dB (H)
-13.2 dB (E)



CASSEGRAIN SUBREFLECTOR SCATTERED PATTERN

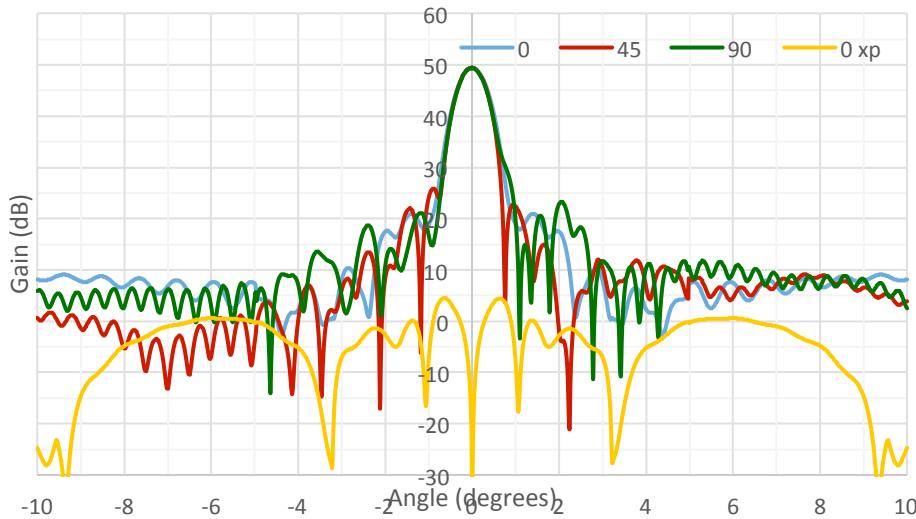


1.6 GHz
At 15° -13.7 dB (H)
-13.2 dB (E)



ANTENNA BEAMS AT 1.6 GHz , $\theta_{\text{sub}}=30^\circ$

30 degrees Gregorian



GREGORIAN

Blockage loss = 0%

$\eta_a = 64\%$

Xpol= -45 dB

CASSEGRAIN

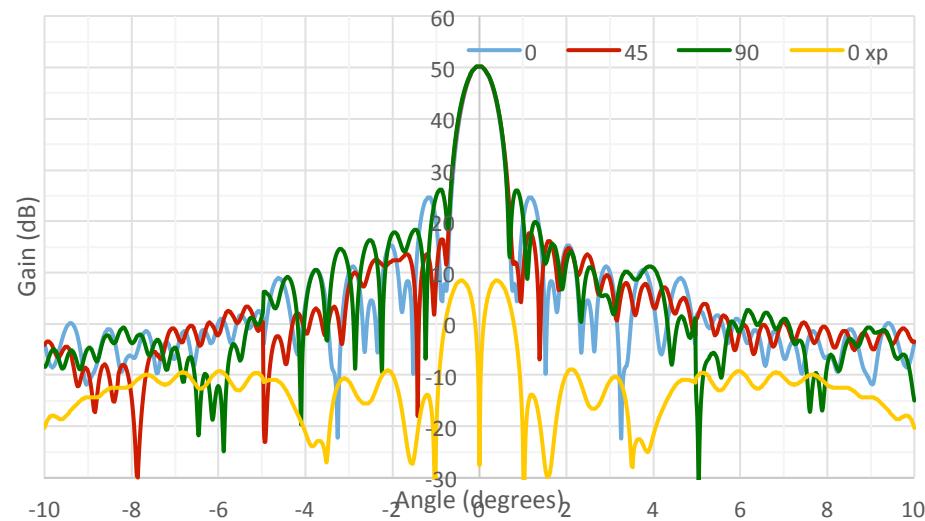
$R_{\text{sub}}^2/R_{\text{main}}^2 = 1.3\%$

Blockage loss = 2.4%

$\eta_a = 63\%$

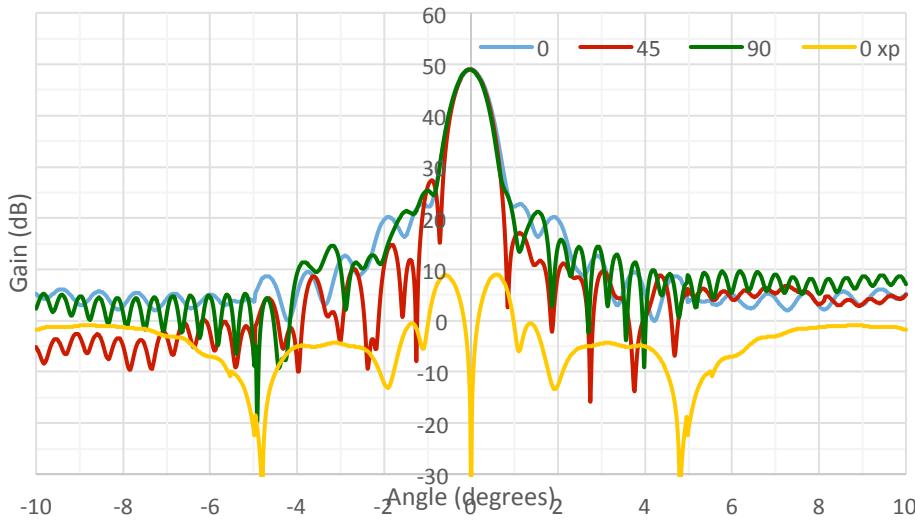
Xpol= -42 dB

30 degrees Cassegrain



ANTENNA BEAMS AT 1.6 GHz , $\theta_{\text{sub}}=36^\circ$

36 degrees Gregorian



GREGORIAN

Blockage loss = 0%

$\eta_a = 62\%$

Xpol=-41 dB

CASSEGRAIN

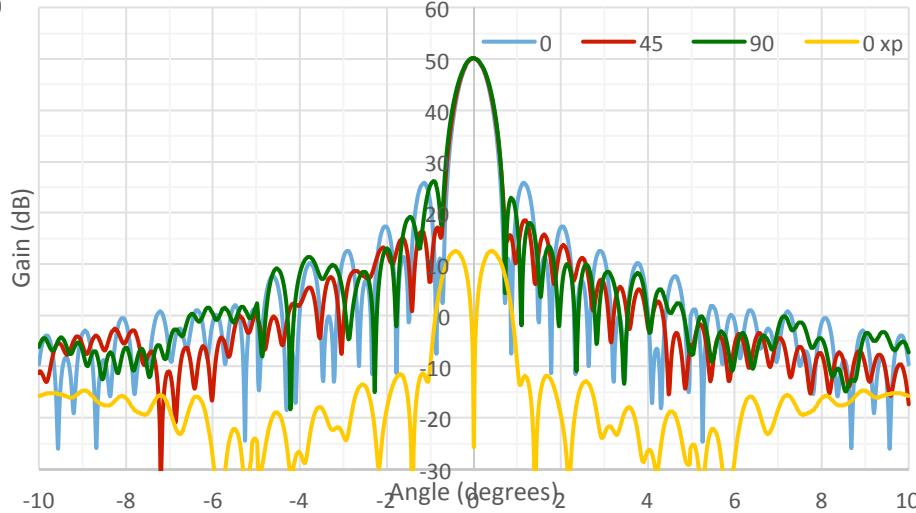
$R_{\text{sub}}^2/R_{\text{main}}^2 = 1.9\%$

Blockage loss = 2.6%

$\eta_a = 61.4\%$

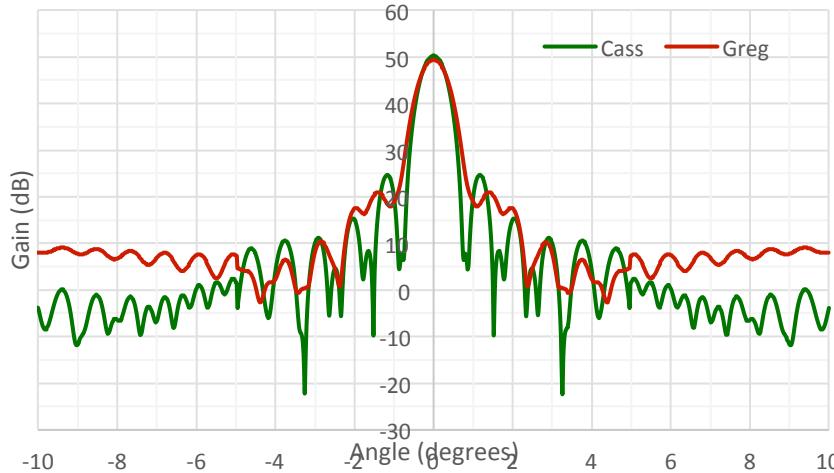
Xpol= -39 dB

36 degrees Cassegrain

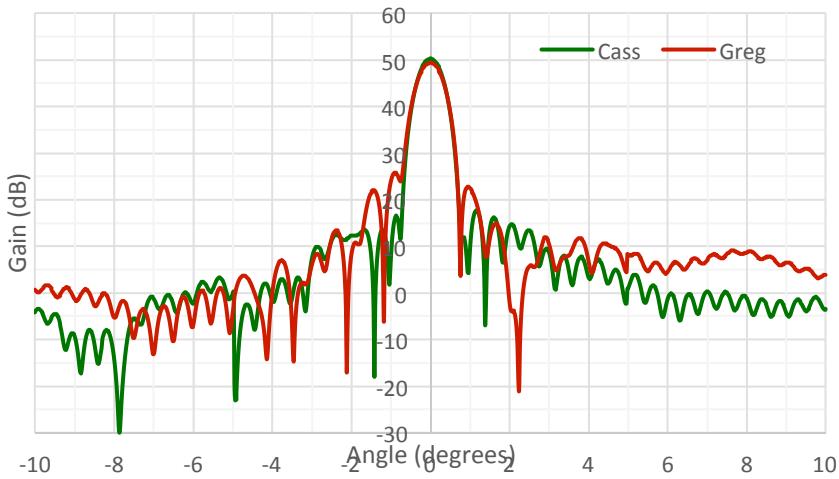


ANTENNA BEAMS AT 1.6 GHz , $\theta_{\text{sub}}=30^\circ$

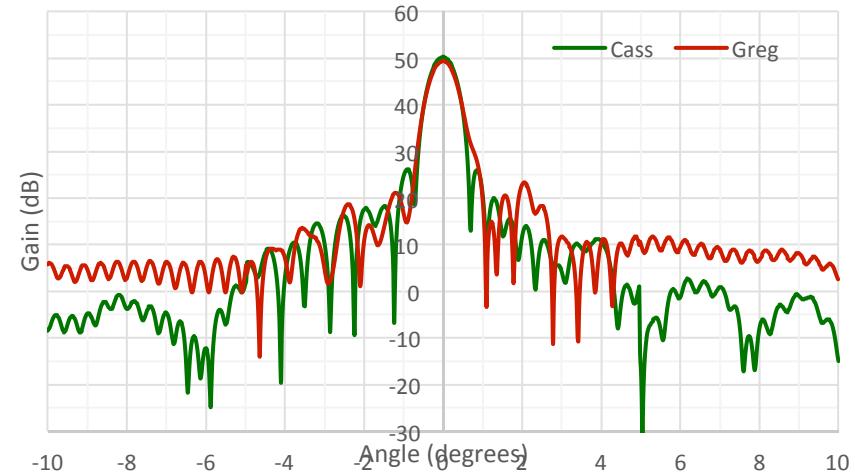
30 degrees Subreflector; 0° -plane



30 degrees Subreflector; 45° -plane



30 degrees Subreflector; symmetric plane



CONCLUSIONS

Gregorian Antenna:

Smaller subreflector

Marginally higher gain

Lower crosspolarization

Larger extent of diffracted fields

Requires ground blocking shield – baseline problems

Cassegrain Antenna:

Blockage

Lower spillover

Smaller envelope

Large real estate

Larger subreflector Opening Angle: $2D/2 \lambda$

Smaller feed horns

Feed to reflector distance smaller – Even smaller

Higher crosspolarization

Cassegrain - larger subreflector

Gregorian – feed horn points more towards ground

GROUND SHIELDS



ATA ANTENNA

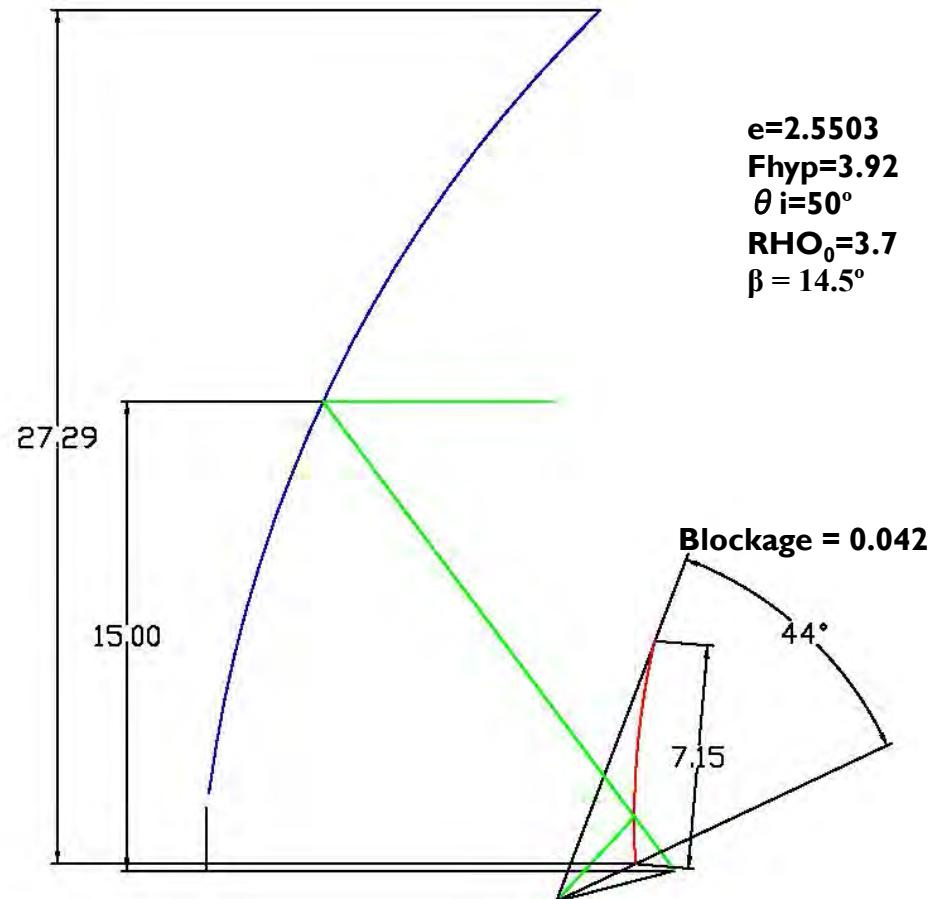
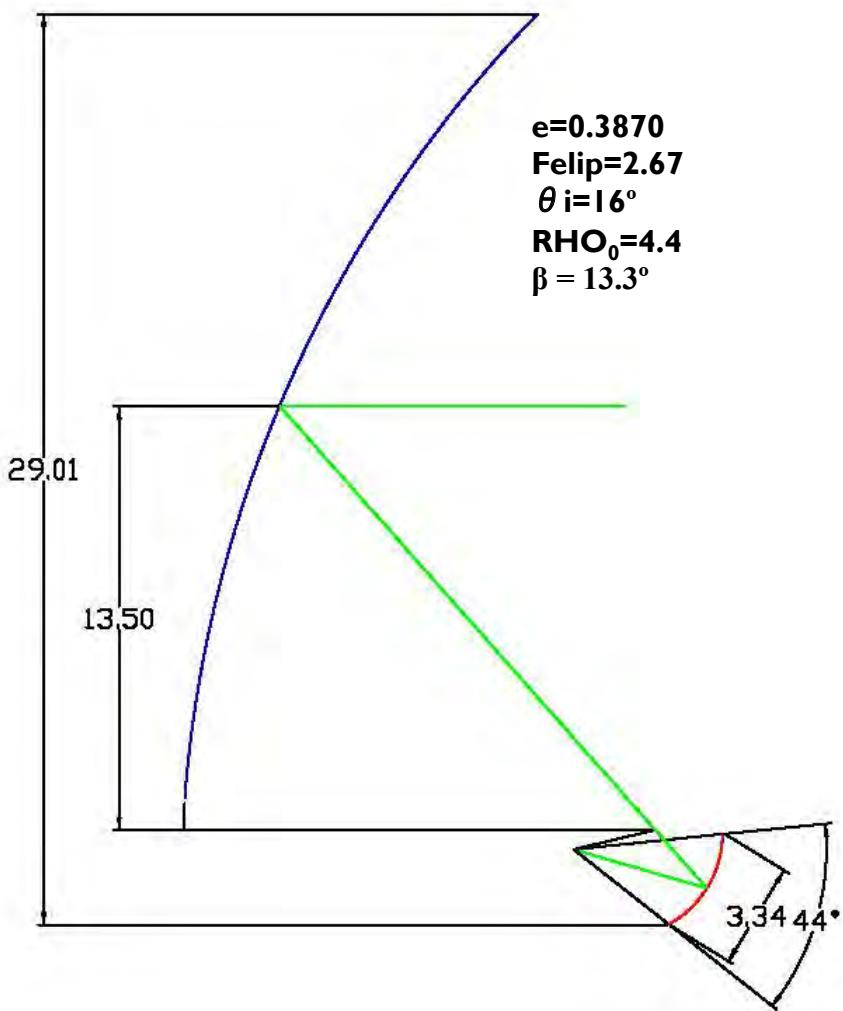


MEERKAT ANTENNA

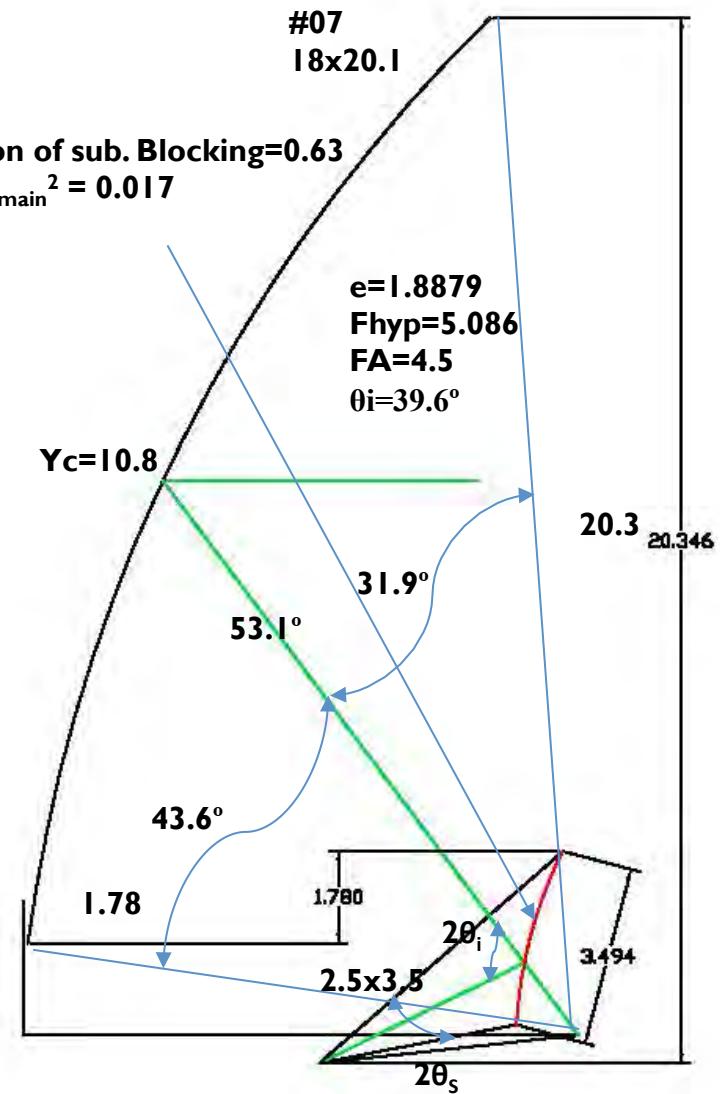
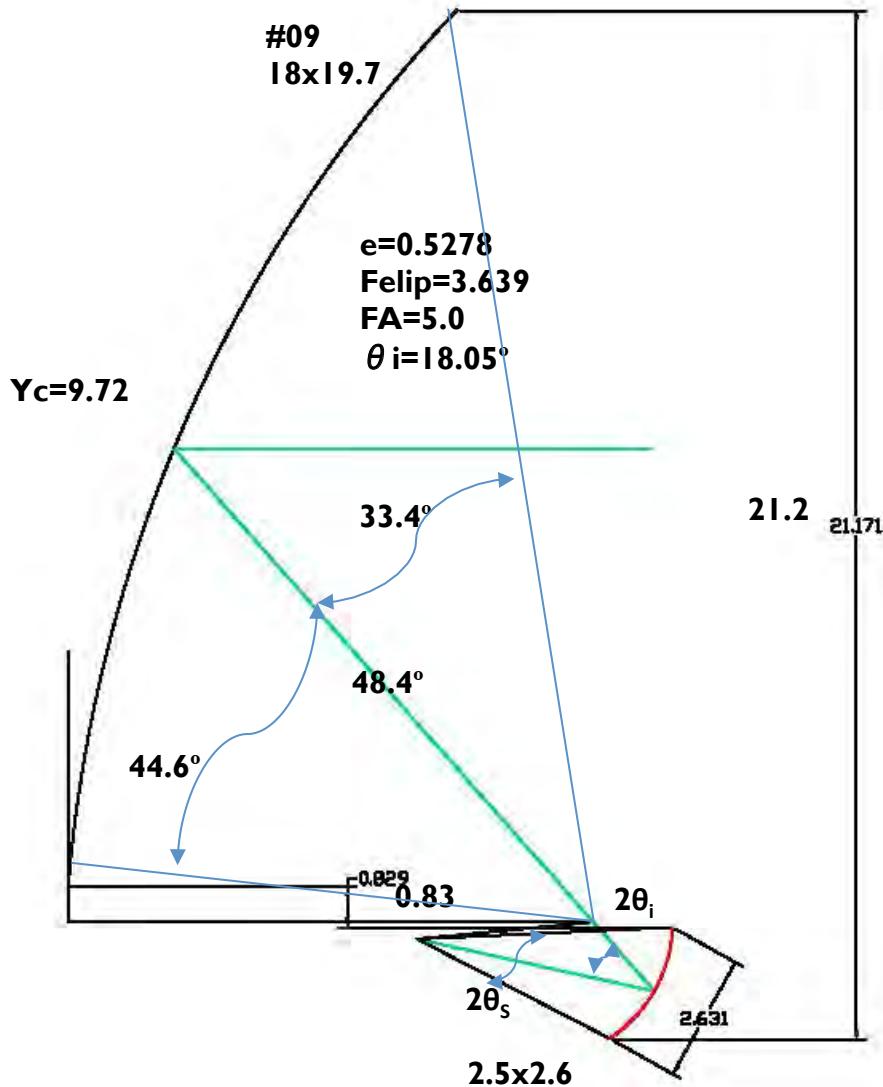
?



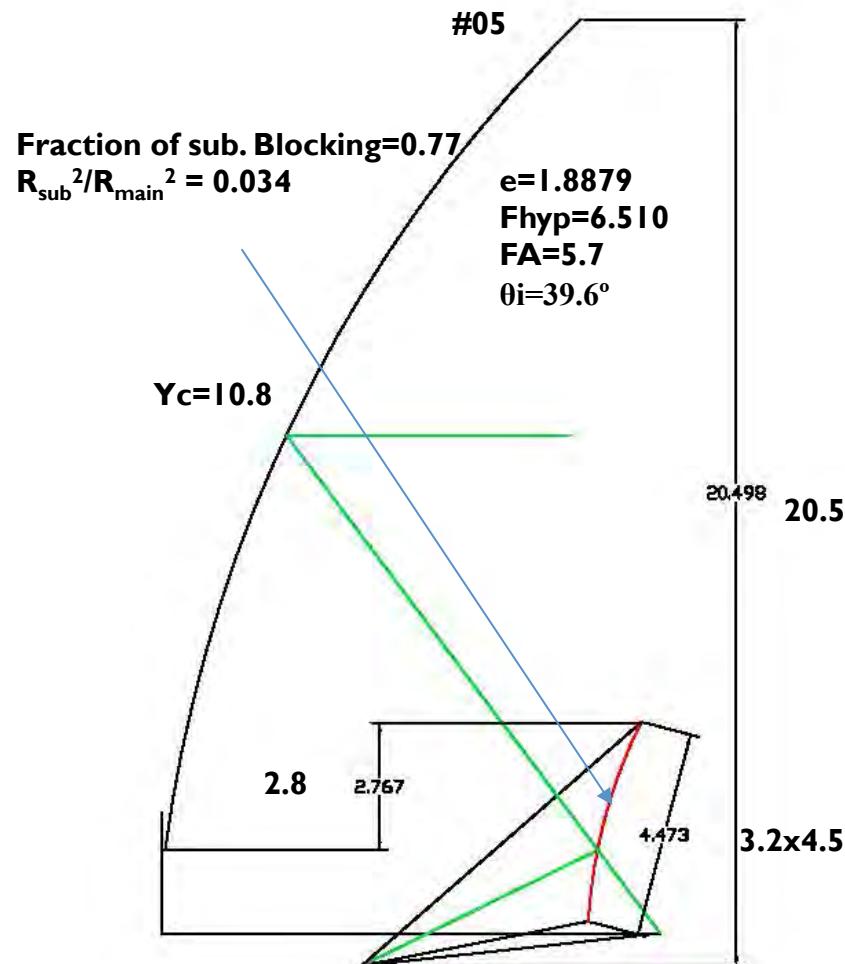
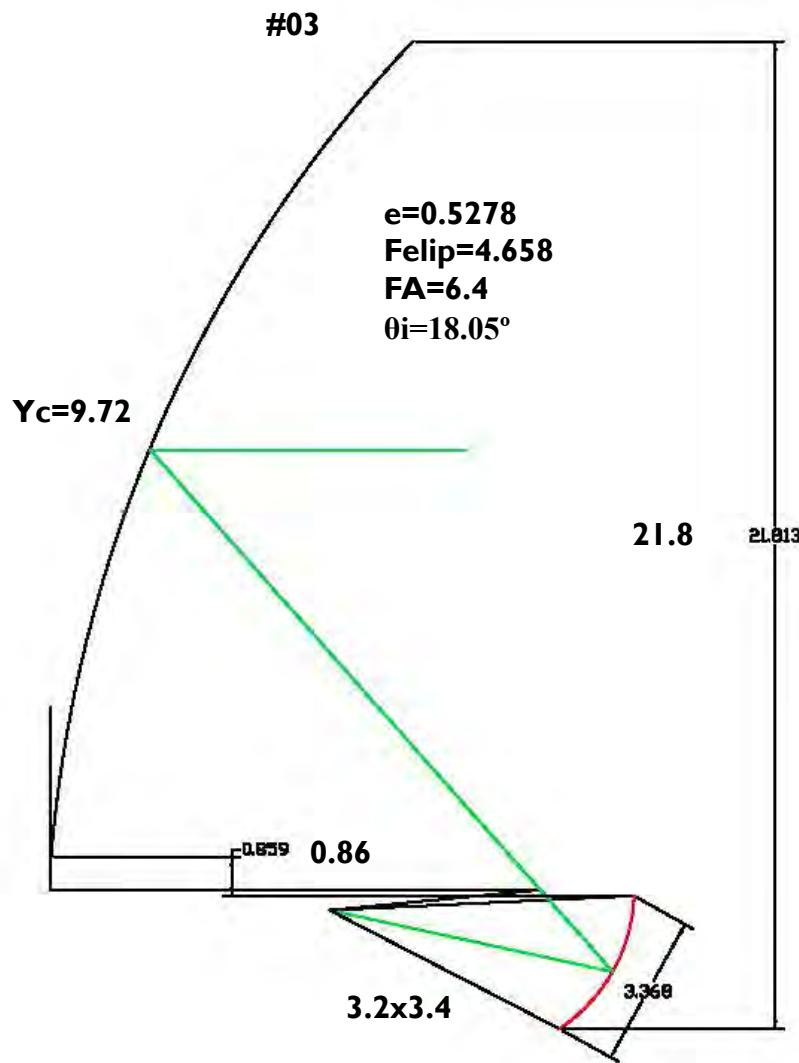
25m MAIN; F=15m; $\theta_{\text{sub}}=44^\circ$



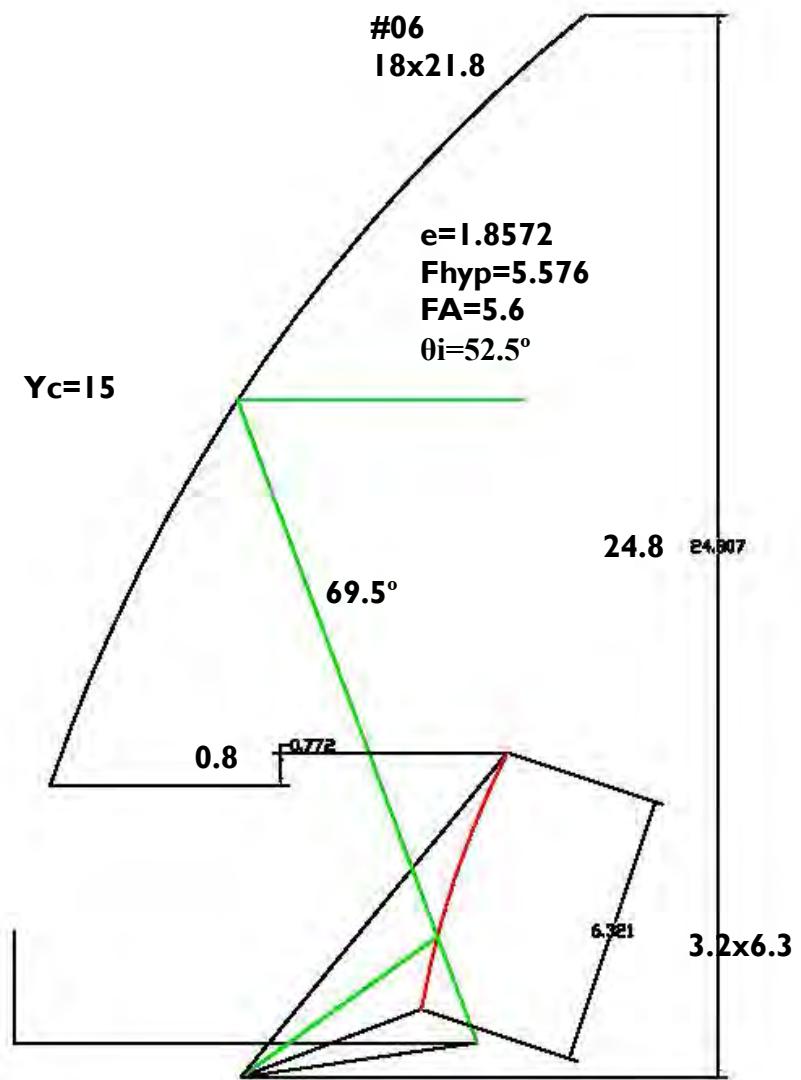
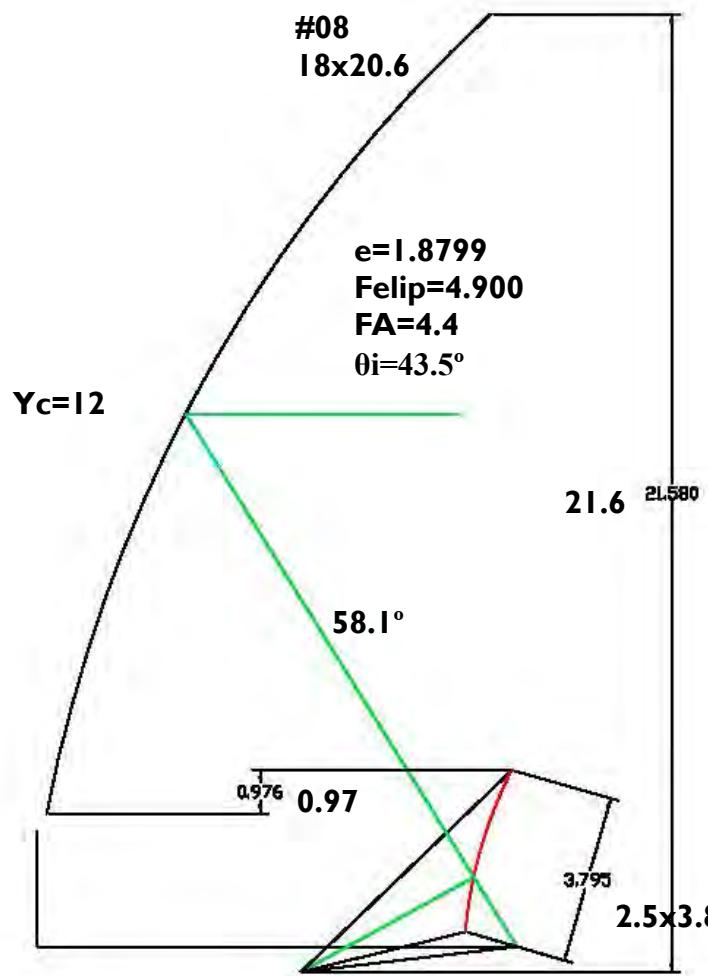
18 m MAIN, F=10.8; 2.5 m($10\lambda_{1.2}$) SUB; $\theta_{\text{sub}}=15^\circ$



18 m MAIN REFLECTOR; 3.2 m ($12.8\lambda_{1.2}$) SUB; $\theta_{\text{sub}}=15^\circ$



18 m MAIN REFLECTOR; 2.5, 3.2 m CASS SUBREFLECTOR



VLA ANTENNA GEOMETRY

Subreflector 2.35m

$$R_{\text{sub}}^2/R_{\text{main}}^2 = 0.0088$$

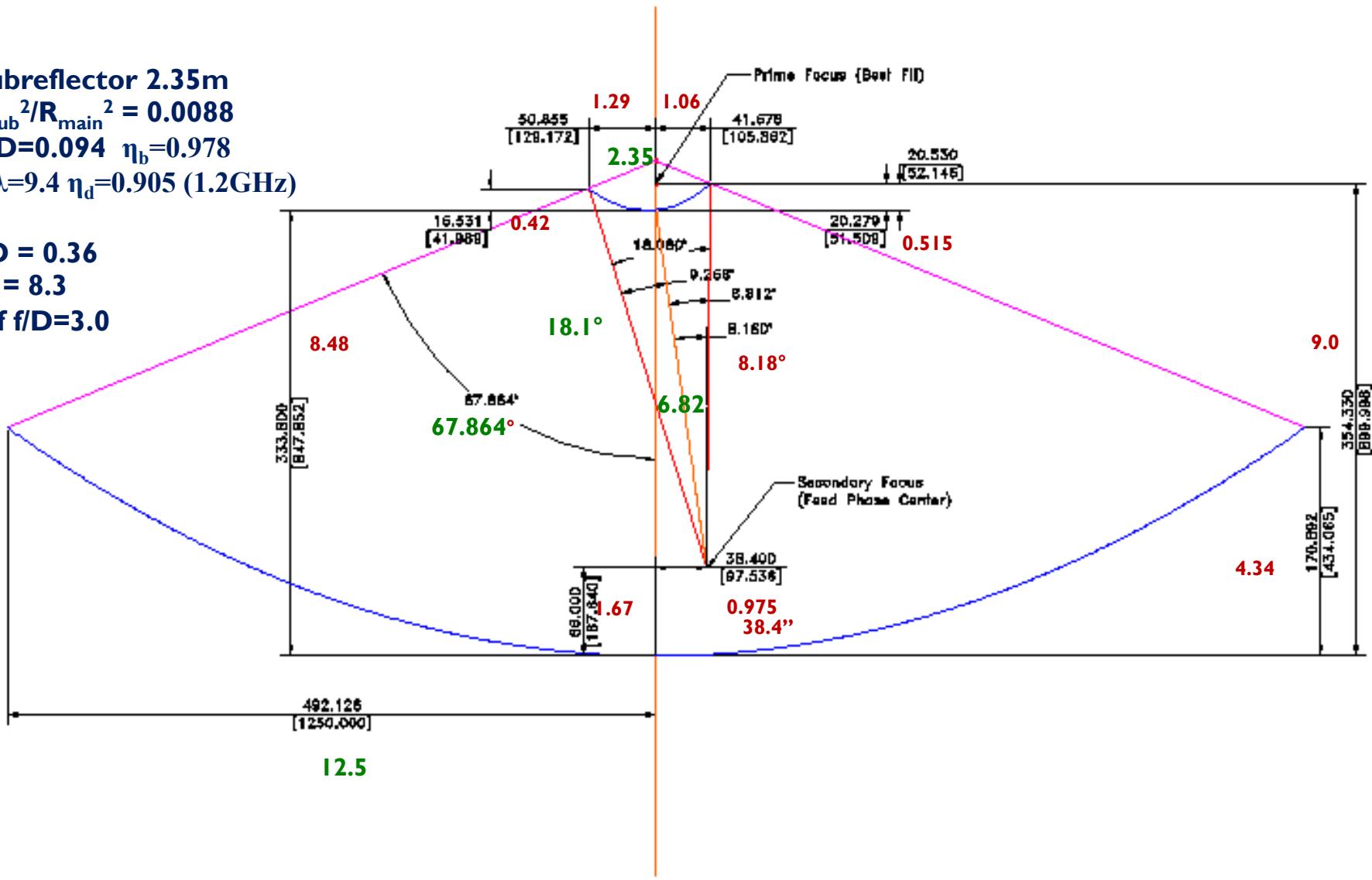
$$d/D = 0.094 \quad \eta_b = 0.978$$

$$d/\lambda = 9.4 \quad \eta_d = 0.905 \text{ (1.2GHz)}$$

$$f/D = 0.36$$

$$M = 8.3$$

$$\text{Eff } f/D = 3.0$$



VLBA ANTENNA GEOMETRY

Subreflector 3.195m

$$R_{\text{sub}}^2/R_{\text{main}}^2 = 0.016$$

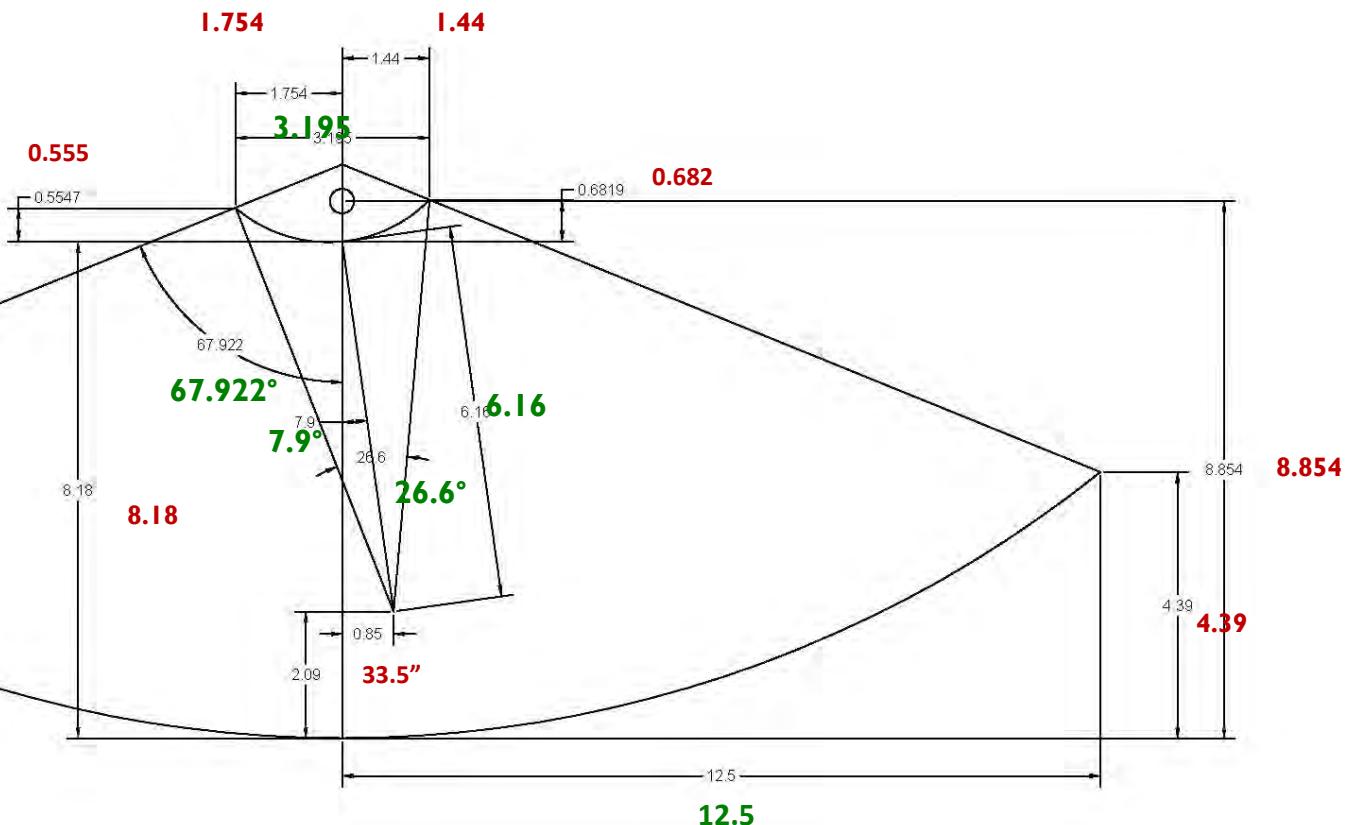
$$d/D = 0.128 \quad \eta_b = 0.96$$

$$d/\lambda = 12.8 \quad \eta_d = 0.975 \text{ (1.2GHz)}$$

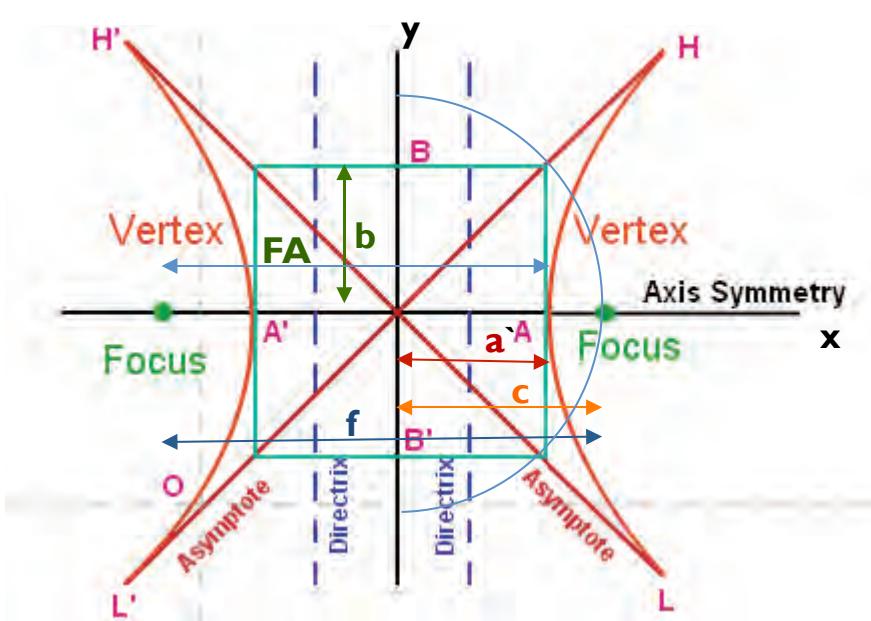
$$f/D = 0.354$$

$$M = 5.78$$

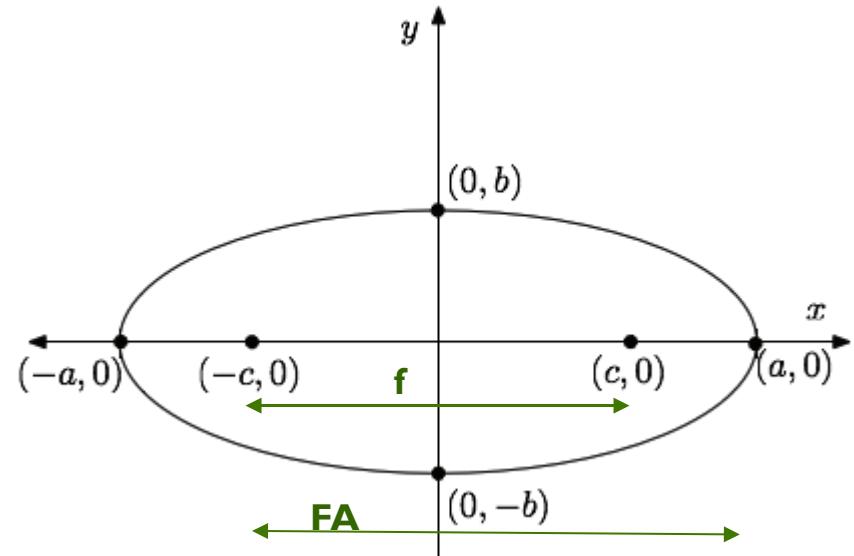
$$\text{Eff } f/D = 2.05$$



HYPERBOLA / ELLIPSE PARAMETERS



$$x^2/a^2 - y^2/b^2 = 1$$



$$x^2/a^2 + y^2/b^2 = 1$$

$$e = \sqrt{a^2 + b^2} / c = \sqrt{a^2 + b^2} \quad e > 1$$

$$e = \sqrt{a^2 - b^2} / c = \sqrt{a^2 - b^2} \quad e < 1$$

$$f = 2c$$

$$f = 2c$$

CASSEGRAIN TELESCOPE DESIGN PARAMETERS

	DIA Main	F _{Main}	Θ_{main} °	e	f _{hyp}	MAG	Θ_{sub} °	DIA Sub	FA
VLAeq	25.0	9.2897	67.864	1.2734	7.691	8.3164	9.250	2.350	6.865
				1.2600	7.691	8.6923	8.8518	2.253	6.897
				1.2900↑	7.691	7.8966	9.7397↑	2.468↑	6.827↓
VLAeq	25.0	9.2897	67.864	1.2734	7.691	8.3164	9.250	2.350	6.865
				1.2734	7.500	8.3164	9.250	2.291	6.695
				1.2734	7.900↑	8.3164	9.250	2.413↑	7.052↑

GREGORIAN TELESCOPE DESIGN PARAMETERS

DIA Main	F _{Main}	Y _c	Θ _{sub} °	e	f _{ellip}	MAG	°	DIA Sub	FA
18x19.7	10.8	9.72	15	0.5278	3.639	3.1649	2.5x2.6		7.659
				0.7600	6.738	7.3333	10.484	2.697	7.802
				0.8000 ↑	6.738	9.0000	8.5503 ↓	2.158 ↓	7.580 ↓
25mGreg	25.0	9.2897	67.864	0.7853	6.738	8.3166	9.250	2.350	7.659
				0.7853	6.540	8.3166	9.250	2.281	7.434
				0.7853	6.940 ↑	8.3166	9.250	2.421 ↑	7.889 ↑

GREGORIAN TELESCOPE DESIGN PARAMETERS

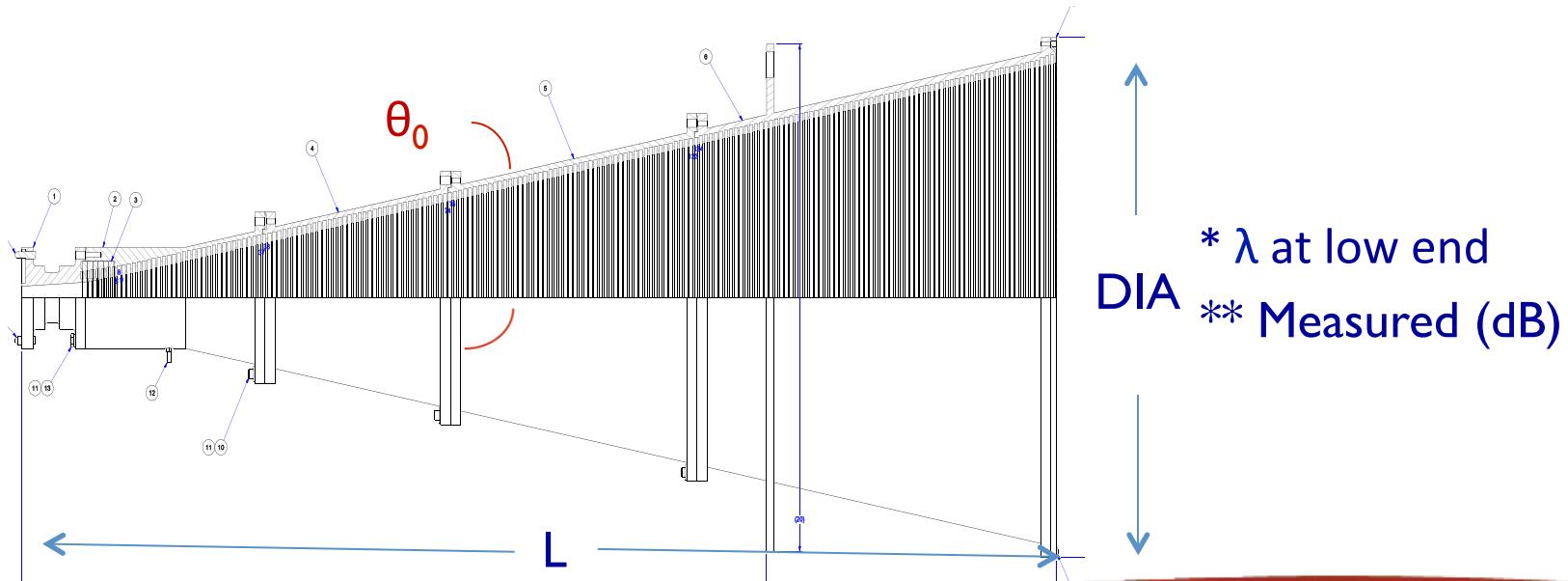
	DIA Main	F Main	Θ_{main} °	e	f ellip	MAG	Θ_{sub} °	DIA Sub	FA
25mGreg	25.0	9.2897	67.864	0.7853	6.738	8.3166	9.250	2.350	7.659
				0.7600	6.738	7.3333	10.484	2.697	7.802
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				0.7853	6.940 ↑	8.3166	9.250	2.421 ↑	7.889 ↑

CASSEGRAIN TELESCOPE DESIGN PARAMETERS

	DIA Main	F Main	Θ_{main} °	e	f_{hyp}	MAG	Θ_{sub} °	DIA Sub	FA
VLAeq	25.0	9.2897	67.864	1.2734	7.691	8.3164	9.250	2.350	6.865
	25.0	9.2796	67.922	1.4179	7.691	5.7857	13.300	3.313	6.558
VLBAeq				1.4179	7.416	5.7857	13.300	3.195	6.323
ALMA	12.0	4.8	64.01	1.0526	6.177	20.00	3.6	0.750	5.883
GBT	100	60	39.005	0.528	11.00	3.166	15.0	7.950	15.1

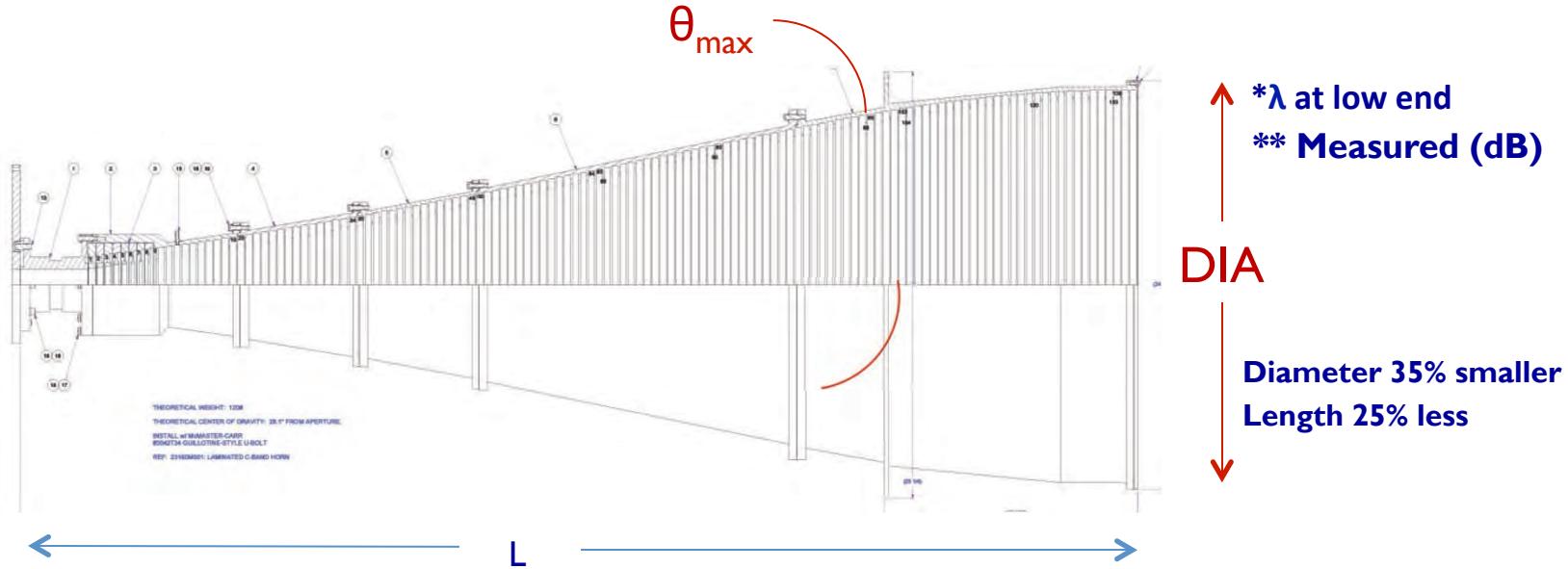
LINEAR TAPER CORRUGATED HORN

FEED	Freq (GHz)	Taper (dB) @ θ_{sub}	θ_0	DIA	DIA/ λ *	L/ λ * **	Taper **
EVLA-Ku	12-18	-14@9.25°	10.5°	12.3"	12.5	33.8	-14.0
VLBA	12-15.4	-14@13.25°	14°	8.0"	8.1	16.2	-14.5
SHAO-Ku	12-18	-15.5@13°	13°	8.5"	8.7	19.3	-15.6

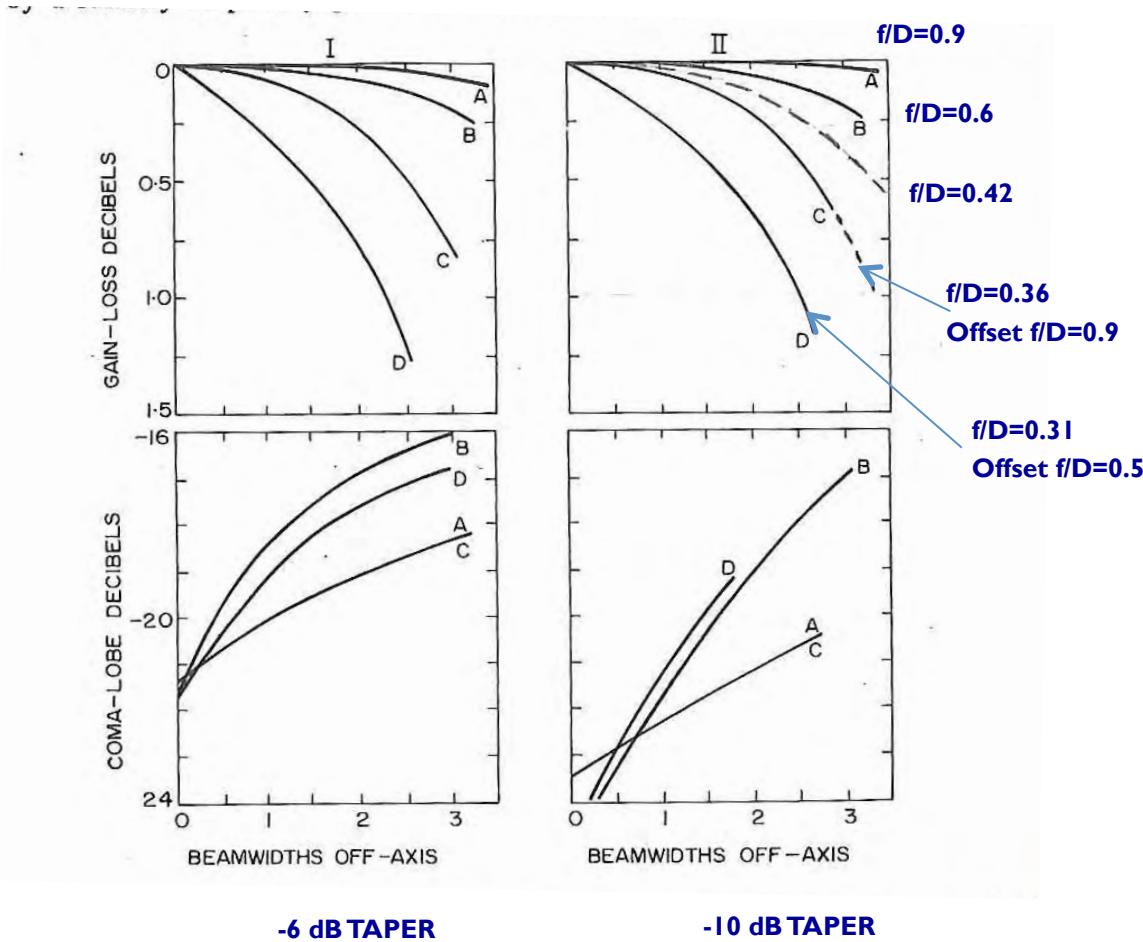


PROFILE TAPER (COMPACT) CORRUGATED HORN

FEED	Freq (GHz)	Taper (dB) @ θ_{sub}	θ_{max}	DIA	DIA/ λ *	L/ λ *	Taper (dB)**	Lin. D/ λ
EVLA-C	4-8	-13@9.25°	12.0°	22.0"	7.5	22.3	-12.5	12.2
VLBA-C	4-8	-14@13.25°	15.0°	14.0"	4.7	10.6	-13.7	8.1

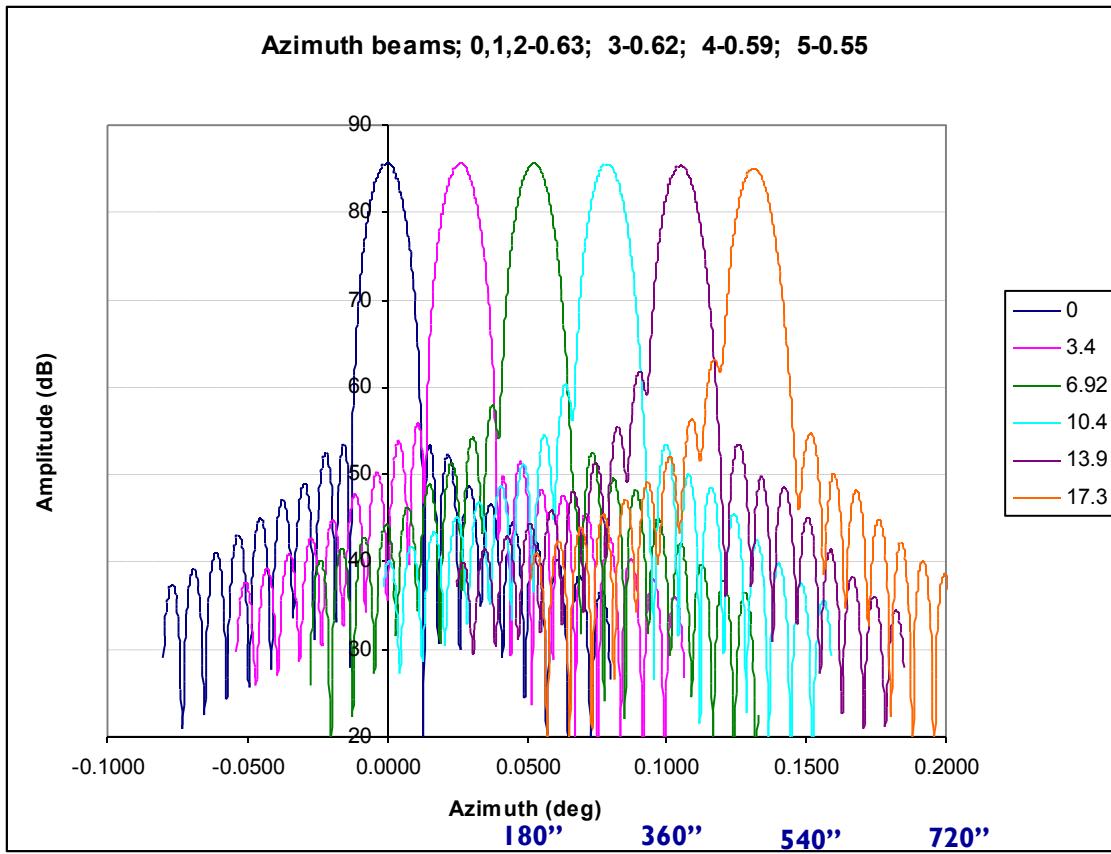


SCAN LOSS, COMA LOBE



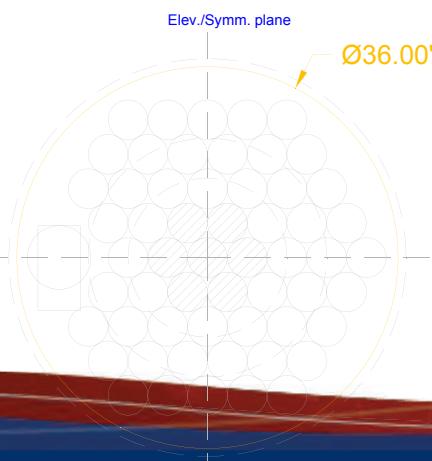
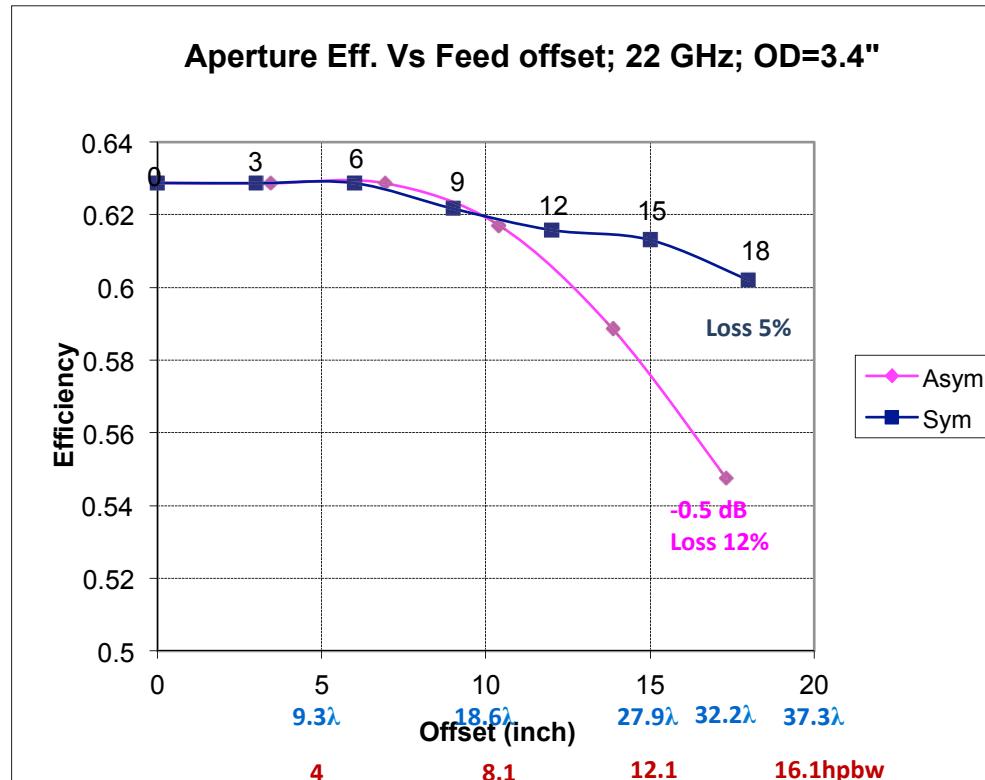
K-BAND ARRAY RECEIVER ON THE GBT

HPBW 34"; Beam throw 27.4"/inch; 0.43HPBW/ λ



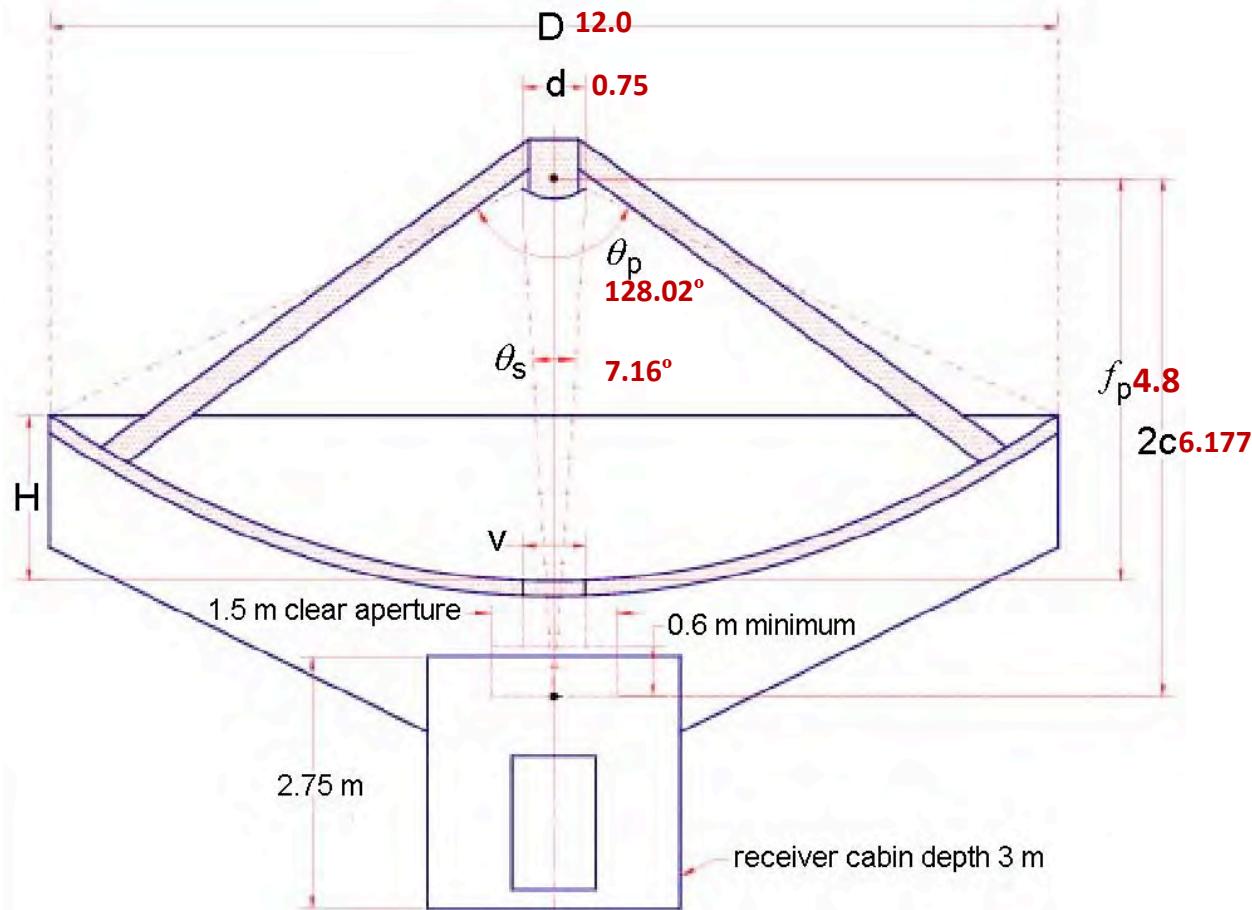
X"	Throw (arcsec)	Throw (HPBW)
0	0	0
3.45	94	2.7
6.9	189	5.5
10.4	284	8.2
13.8	378	11.0
17.3	473	13.7
32.2 λ		

K-BAND ARRAY RECEIVER - LOSS



- Ring #1 (3.4"rad): 62.9%
- Ring #2 (6.9"rad): 62.9%
- Ring #3 (10.4"rad): 61.7% min. -2%; measured -5% at 8.4"offset
- Ring #4 (13.8"rad): 58.9% (az) -6.3%; 61.6% (el) -2%
- Ring #5 (18.0" rad): 54.7% (az); 60.2% (el)

ALMA ANTENNA



	DIA Main	F _{Main}	Θ _{main} °	Ecc	F _{hyp}	MAG	Θ _{sub} °	DIA Sub	FI
ALMA	12.0	4.8	64.01	1.0526	6.177	20.00	3.6	0.750	5.883
				1.0526	5.250	20.00	3.6	0.637	5.000
				1.12445	5.250	17.0707	4.193	0.743	4.959
				1.12445	5.294	17.0707	4.193	0.750	5.001

ALMA ANTENNA CRYOSTAT

Feed dia 14mm (3.2λ)

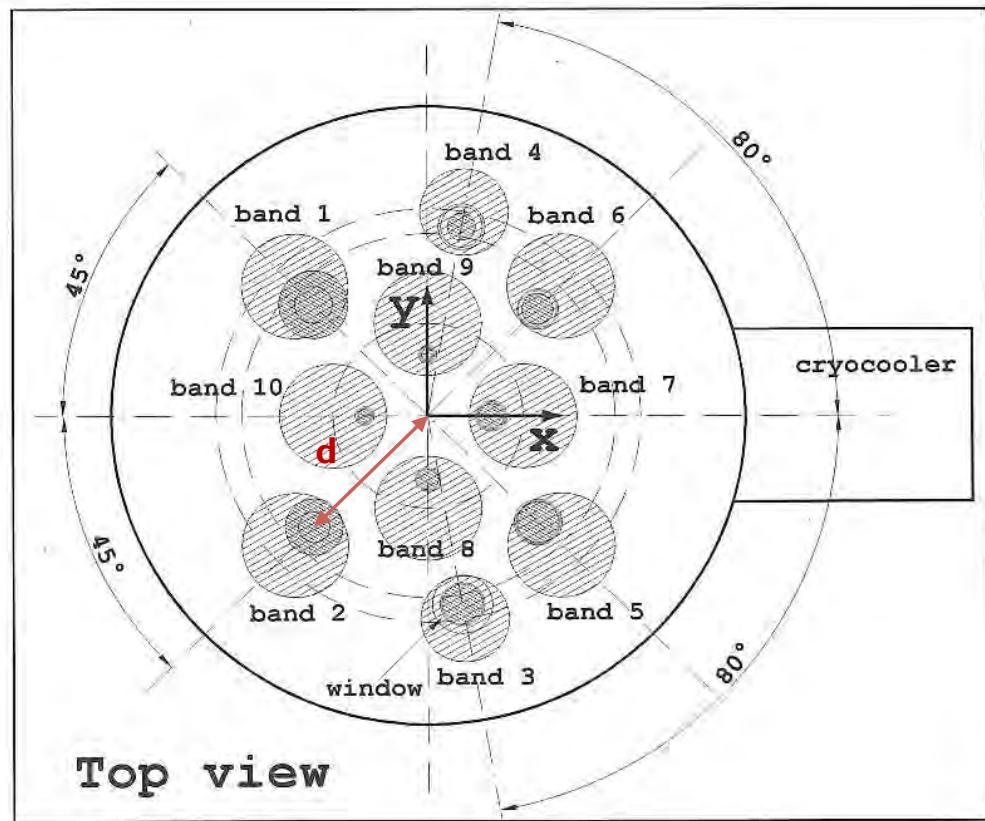
Len 85mm (19.3λ)

Band	d mm	Θ_{sec}°	d/ λ	θ_s/bw	η
1	255	2.48	36.1		
2	255	2.48	67.2		
3	181	1.76	60.4	6.4	0.853
4	181	1.76	86.9		
5	245	2.38	153		
6	245	2.38	198	19.1	0.758
7	100	0.97	108	10.7	0.856

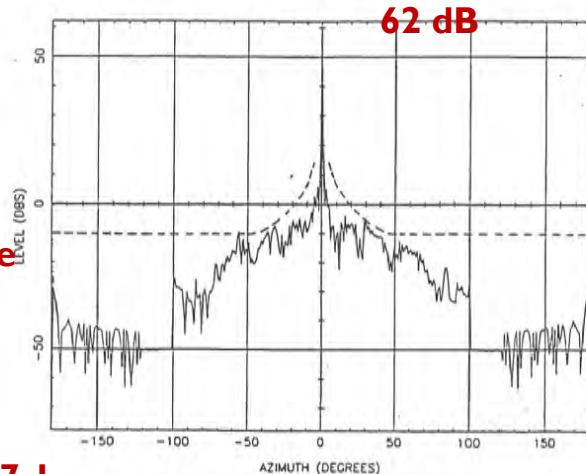
Θ_{sec} - Incident angle at the secondary

θ_s - telescope beam scan angle

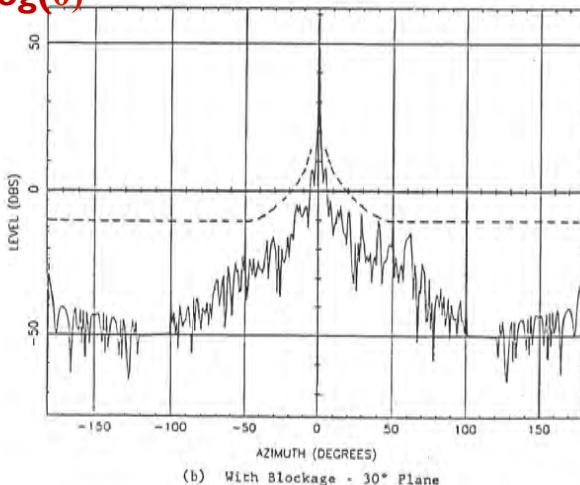
0.1HPBW/ λ



SYMMETRIC AND UNBLOCKED ANTENNA BEAMS

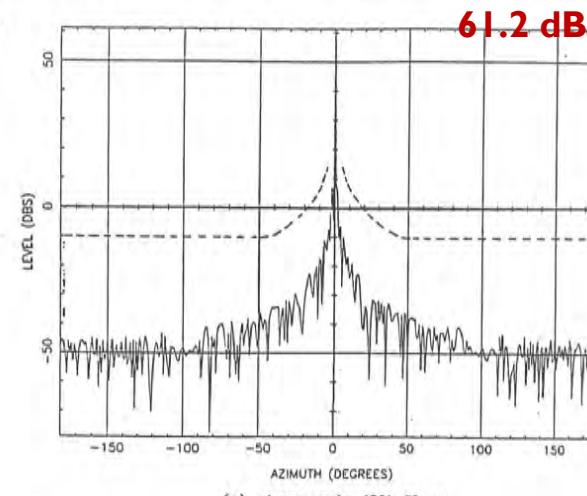


CCIR 677-I
32.25*log(θ)

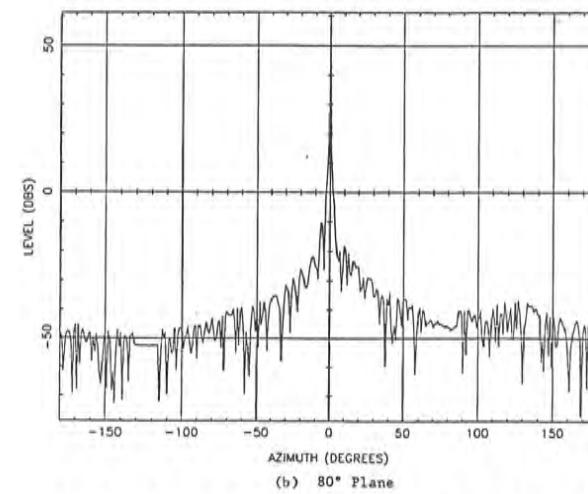


Symmetric 100m, f/d=0.4, sub 7m

1.4 GHz

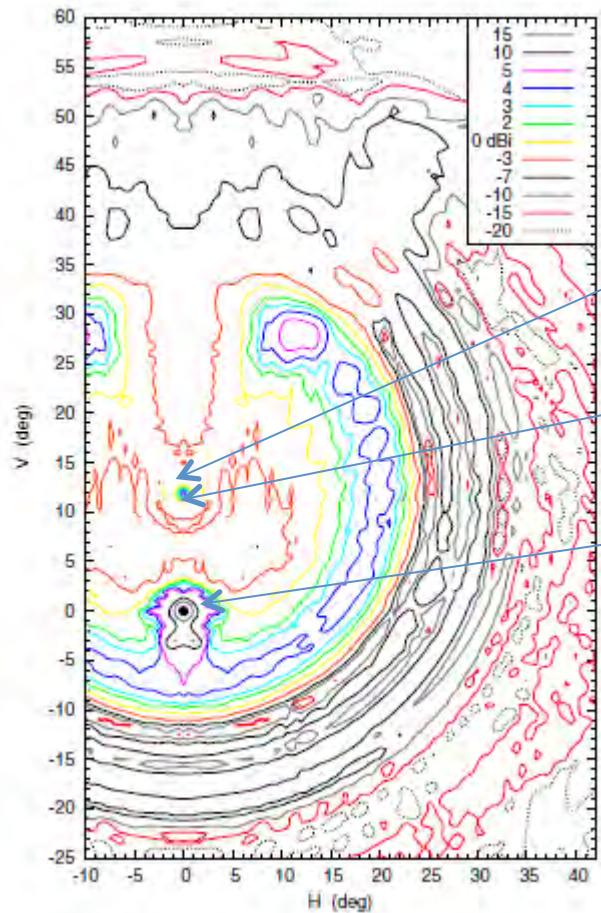


International Radio Consultative Committee CCIR 677-I



Asymmetric 90m, f/d=0.62, sub 7m

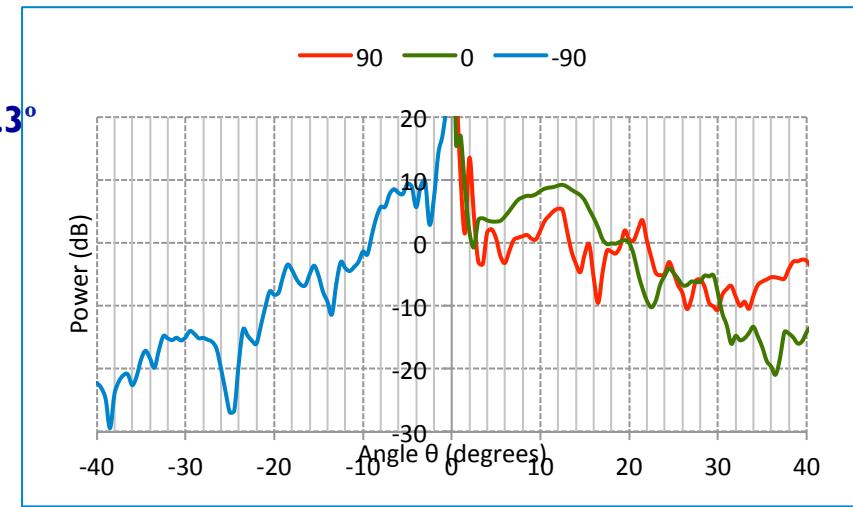
MEASURED SIDELOBE CONTOURS OF GBT AT 21 CMS



Subreflector at 12.3°

Poisson spot

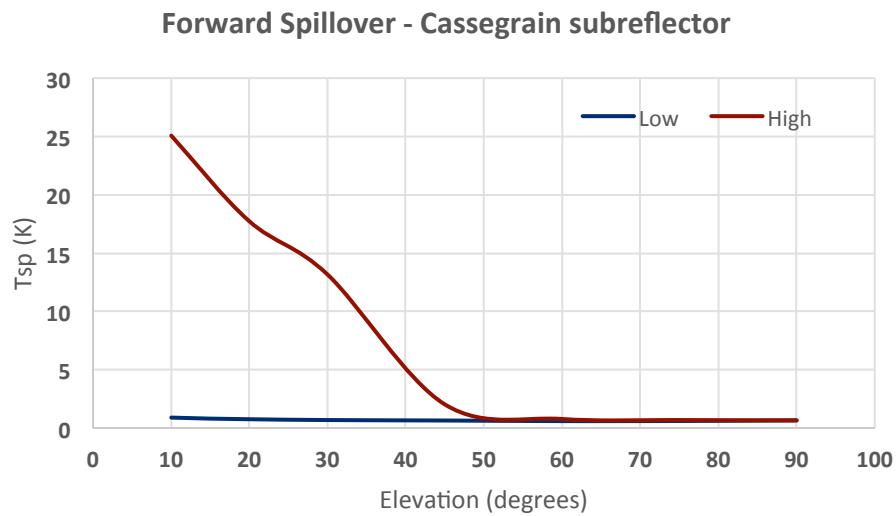
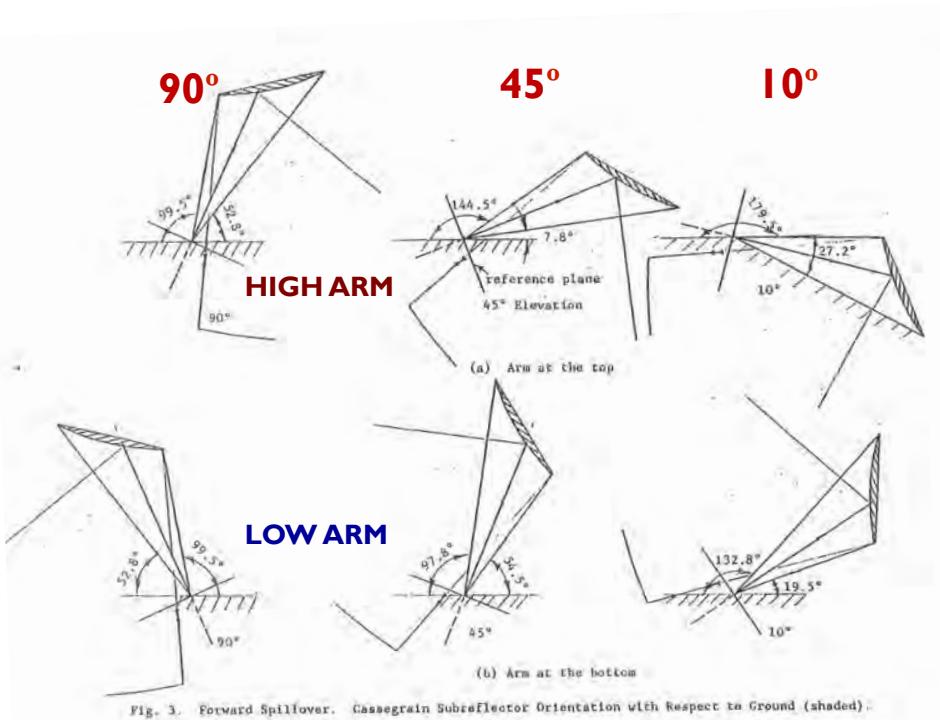
Main beam
61.6 dB



CALCULATED FAR-FIELD PATTERN 1.4 GHz

Boothroyd, A. I. et. al., "Accurate galactic 21-cm HI measurements with the NRAO Green Bank Telescope", *Astronomy & Astrophysics* 536, A81 (2011)

FORWARD SPILLOVER – CASSEGRAIN SUBREFLECTOR



S. Srikanth, "Spillover noise temperature calculations for the Green Bank clear aperture antenna," GBT Memo #16, October 4, 1989.

1.42 GHz
-12 dB taper
 $D_{sub} = 35\lambda$
 $\Theta_{sub} = 14^\circ$

FORWARD SPILLOVER – GREGORIAN SUBREFLECTOR

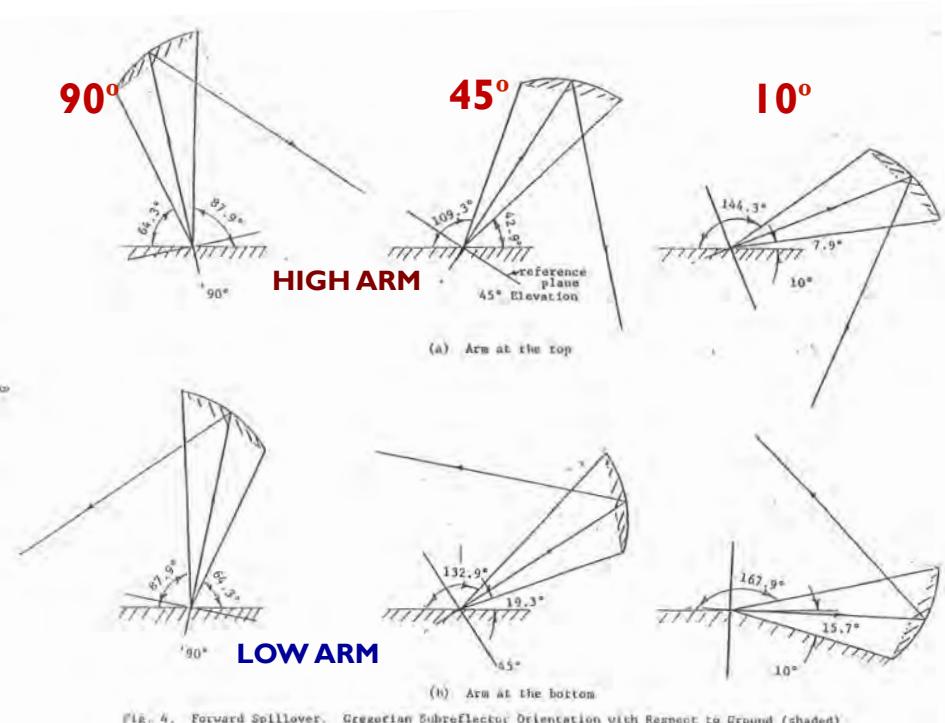
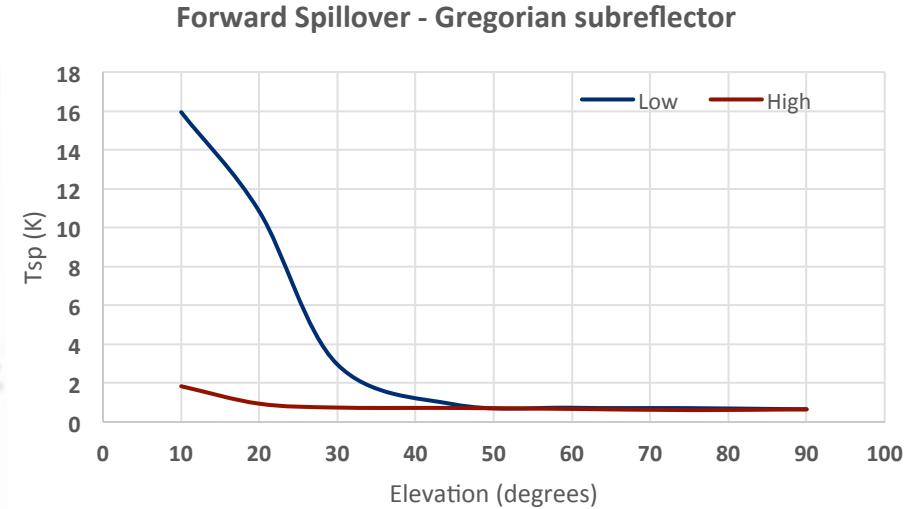
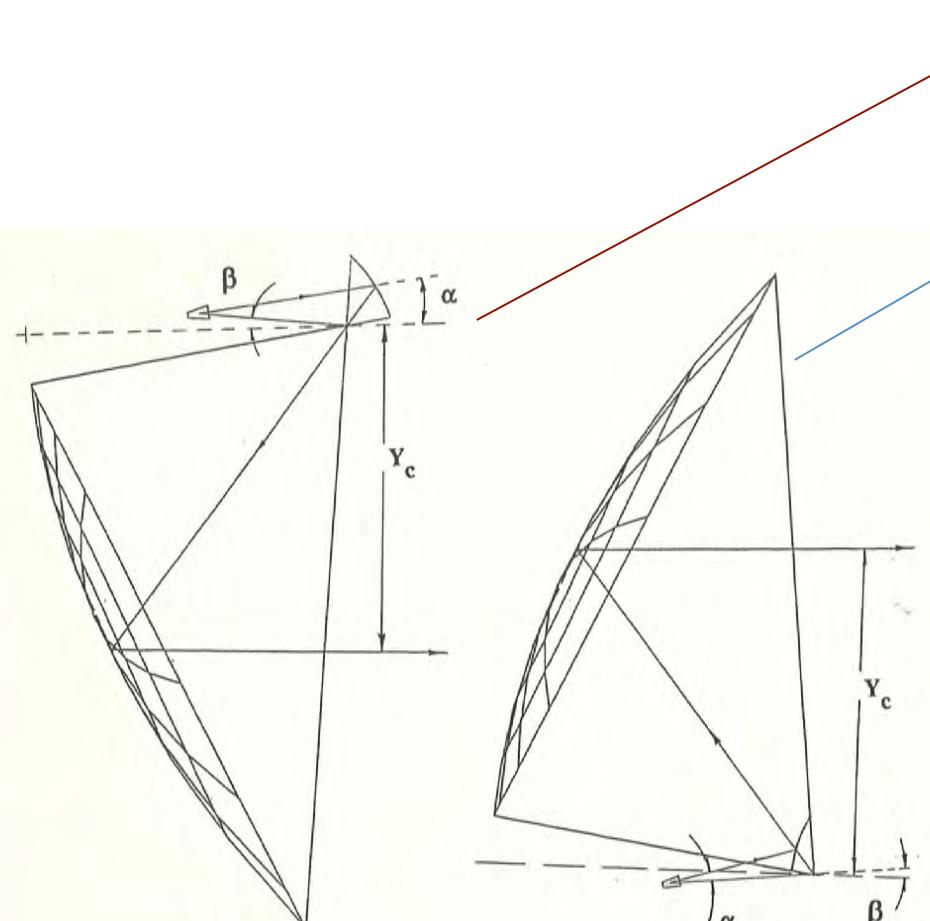


FIG. 4. Forward Spillover. Gregorian Subreflector Orientation with Respect to Ground (shaded).



1.42 GHz
 -12 dB taper
 $D_{\text{sub}}=35\lambda$
 $\Theta_{\text{sub}}=14^\circ$

FORWARD SPILLOVER – HIGH GREG., LOW CASS



Arm at the top.

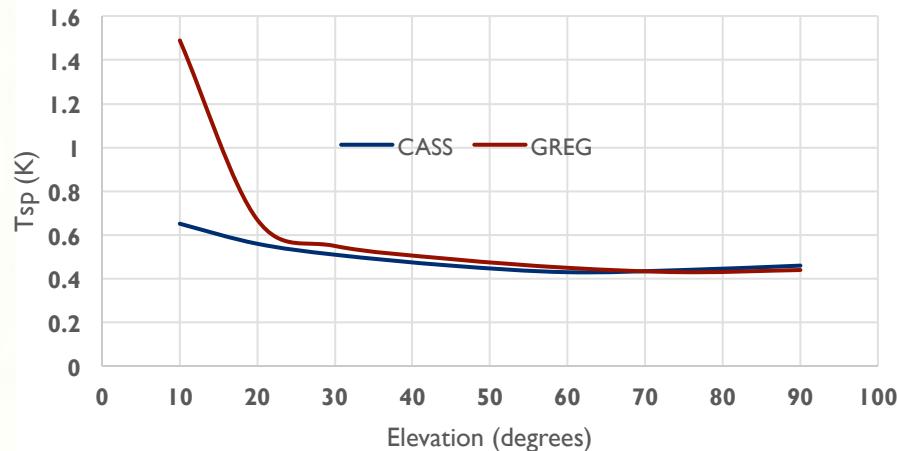
HIGH ARM

Arm at the bottom.

LOW ARM

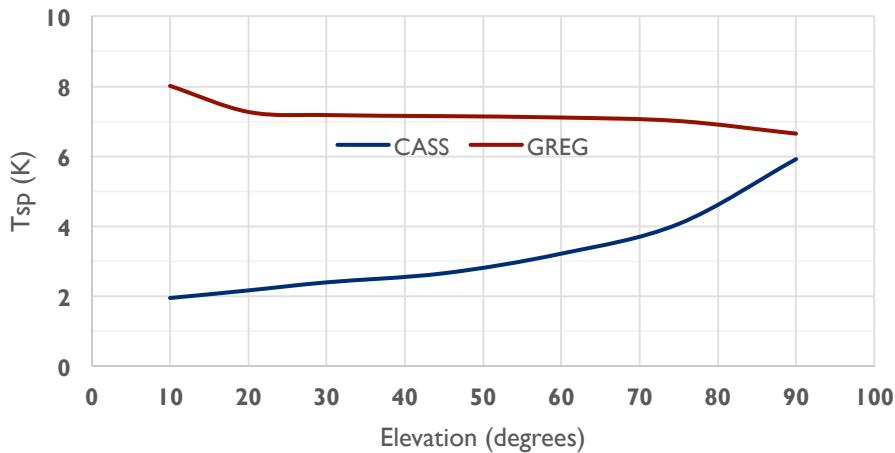
f (m)	Ecc	Yc (m)	α (°)	β (°)	sub (mxm)
GREG	11	0.528	54	17.9	5.57
CASS	14	1.894	54	17.9	5.57

Forward Spillover - Low Cass, High Greg

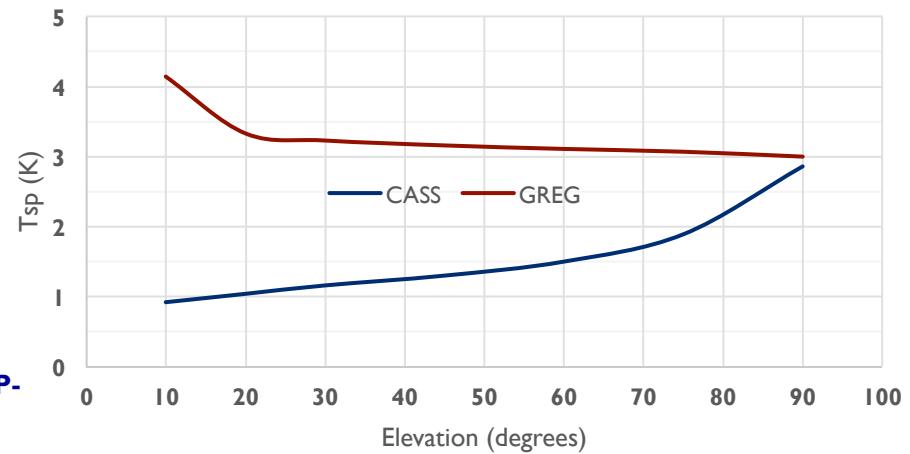


TOTAL SPILLOVER – LOW CASS., HIGH GREG.

Total Spillover - Low Cass, High Greg; 1.4 GHz

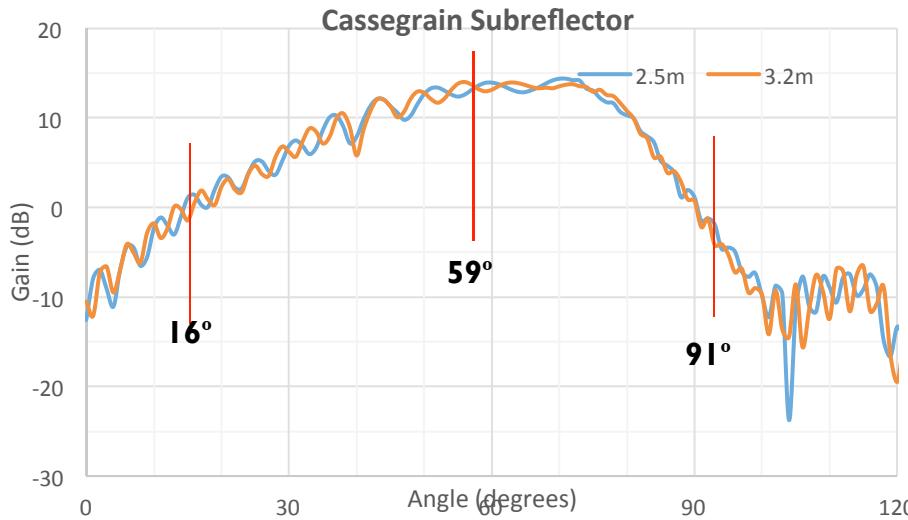


Total Spillover - Low Cass, High Greg; 5GHz



S. Srikanth, "Comparison of Spillover loss of Offset Gregorian and Cassegrain Antennas," IEEE/AP-S Symposium , London, ON, 1991.AP-S Digest pp. 444-447

SUBREFLECTOR PATTERN AT 1.2 GHz

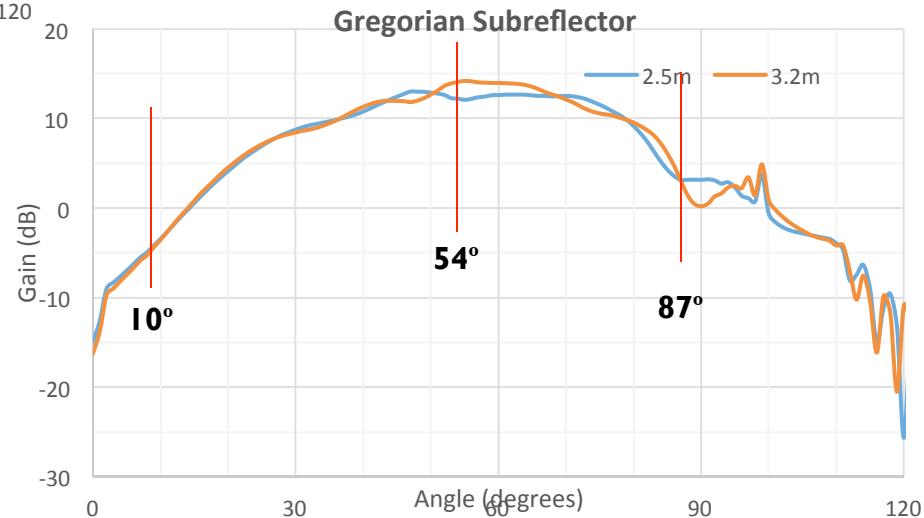


GREGORIAN SUBREFLECTOR

Average taper -12.3 dB (2.5)
Average taper -14.0 dB (3.2)

CASSEGRAIN SUBREFLECTOR

Average taper -13.9 dB (2.5)
Average taper -14.1 dB (3.2)





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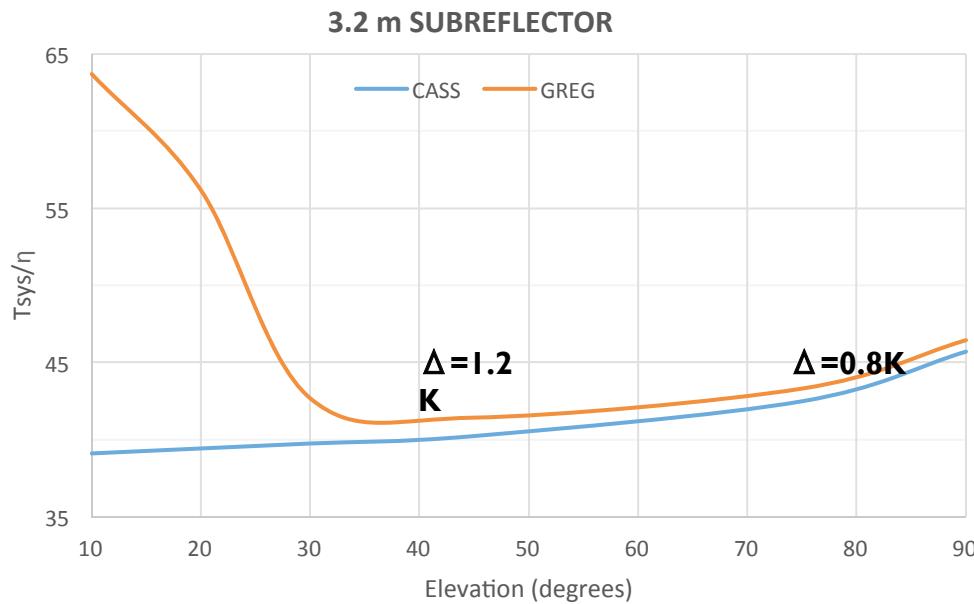


Associated
Universities, Inc.



Associated
Universities, Inc.

$T_{\text{SYS}}/\text{APERTURE EFFICIENCY}$



3.2 m SUBREFLECTOR
 $T_{\text{rx}}=14\text{K}$
 $\eta_a = 62.3\% \text{ CASS}$
 $\eta_a = 64\% \text{ GREG}$

DISH VERIFICATION ANTENNA



MARCHING FORWARD

January 2017

National Radio Science Meeting – Boulder, CO



MARCHING FORWARD

- 1. CALCULATE SPILLOVER FOR 18 M ANTENNA**
- 2. EFFECT OF SHIELD ON LOW GREGORAIN**
- 3. GREGORIAN GEOMETRY – FEED TO HORIZON**
- 4. CASSEGRAIN /GREGORIAN WITH WIDE ANGLE SUBREFLECOTR**
- 5. SYMMETRIC ANTENNA WITH BANDS >10 GHz**



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BLOCKAGE η , DIFFRACTION LOSS

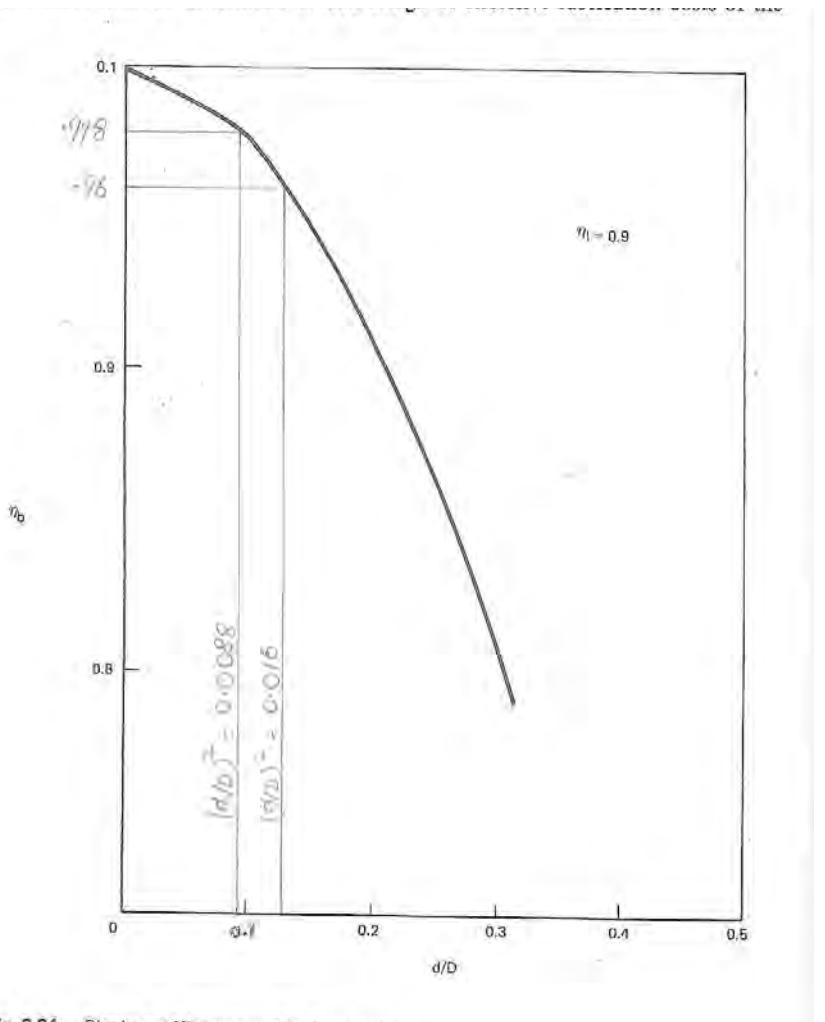


Fig. 3.34 Blockage efficiency vs. blockage ratio

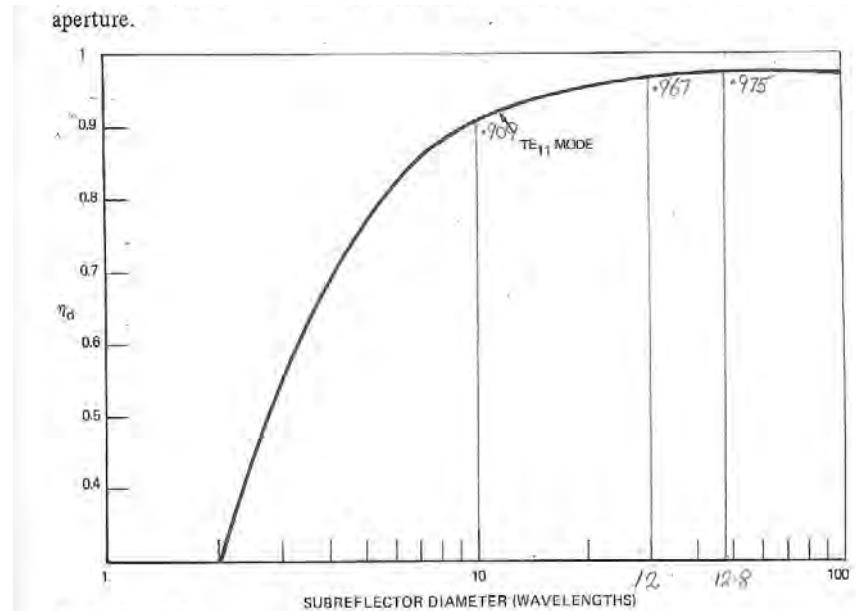
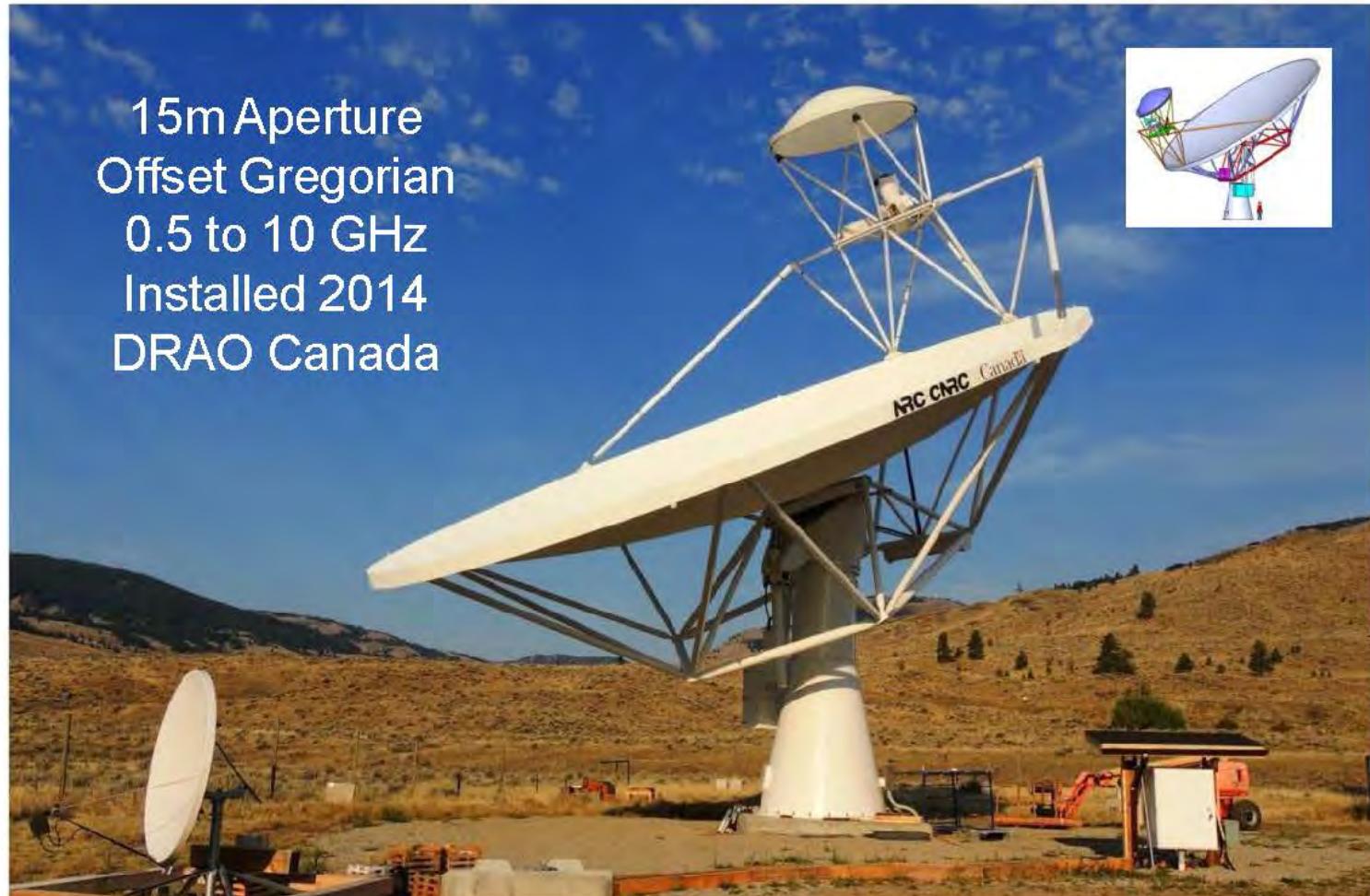


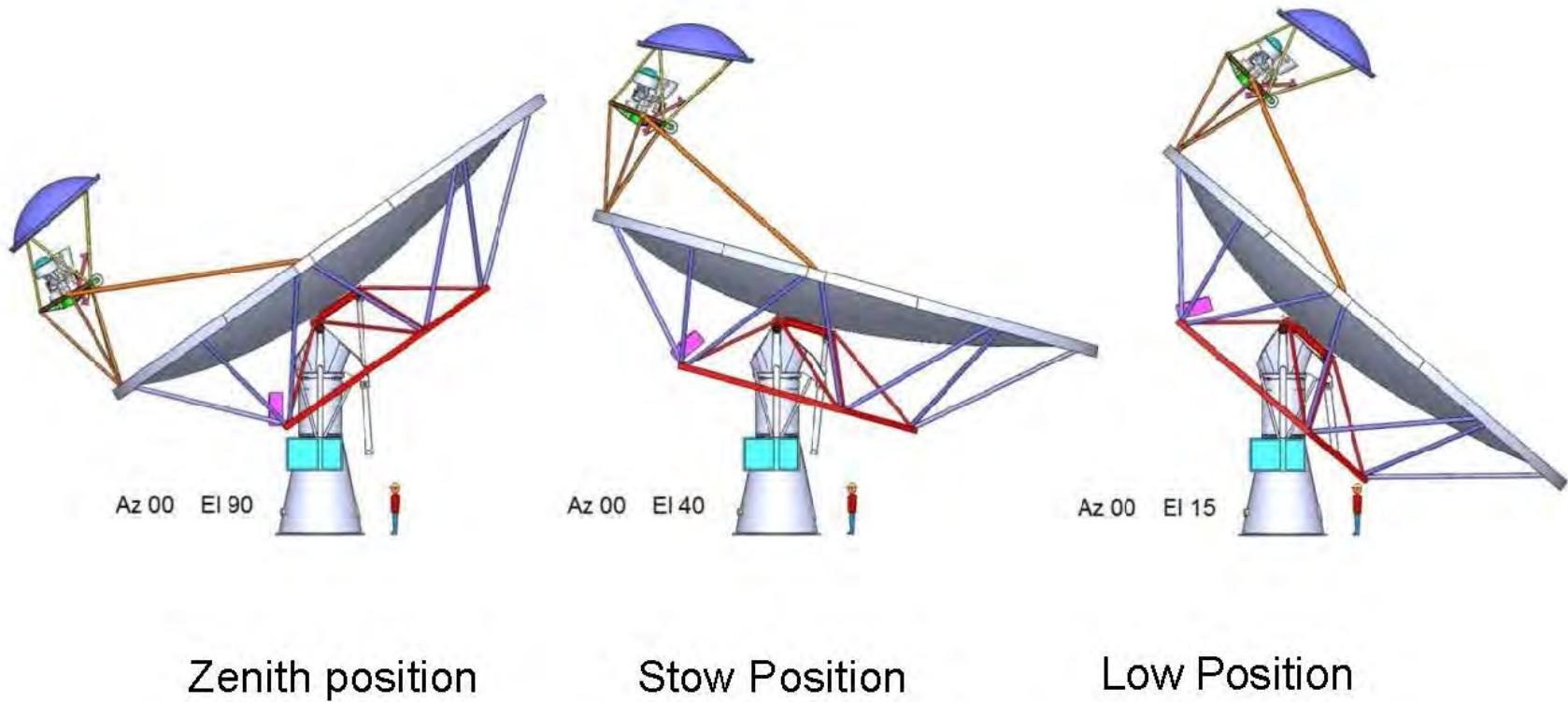
Fig. 3.35 Diffraction loss vs. subreflector size

The Object of Today's Talk

SKA Dish Verification Antenna 1, known as DVA-1

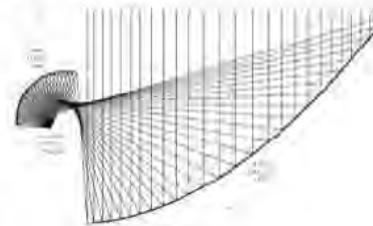


Antenna Several Positions



Optics Design

Features of the design



- Clear optical path, no blockage or scattering.
- Shaped optics, leads to very low spillover. (~ -50db wide angle)
- Very low spillover yields very low antenna noise temp. (<6 K ground)
- Very low spillover results in high rejection of RFI and strong sources.
- Shaped optics yield high efficiencies, total result is a high A_{eff} / T_{sys} .
- Ample space and access to mount multiple feeds on an indexer.
- PAF works effectively at either secondary or primary focal area
- Feed arm high chosen for structural cost reasons.
- Feed arm low may produce slightly lower spillover for some WBSPFs.
- Feed maintenance access via a standard bucket truck.
- Primary area is 22% over symmetric but antenna cost is 13% more.
- Primary surface accuracy will need to be <1mm rms, $1/30 \lambda$.

More features will be listed in the structural design section.

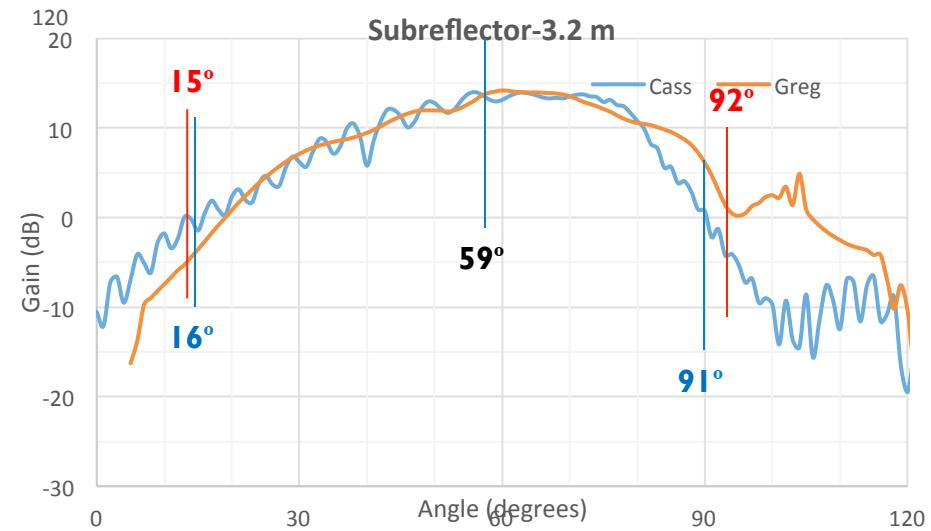
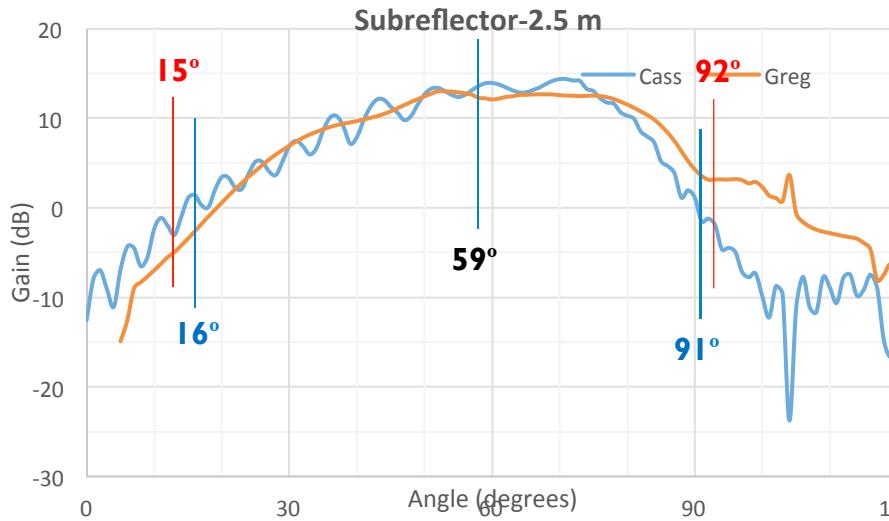
SCAN LOSS, COMA LOBE

January 2017

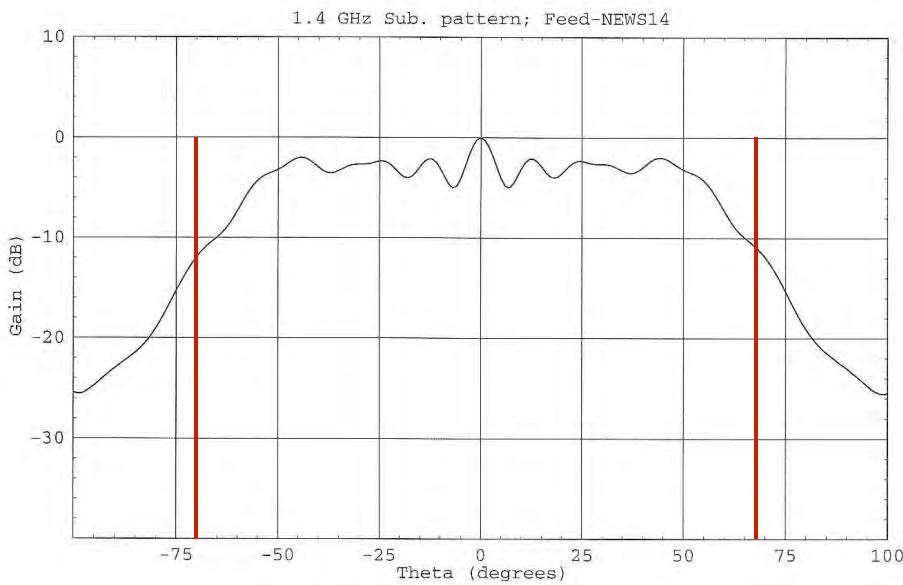
National Radio Science Meeting – Boulder, CO



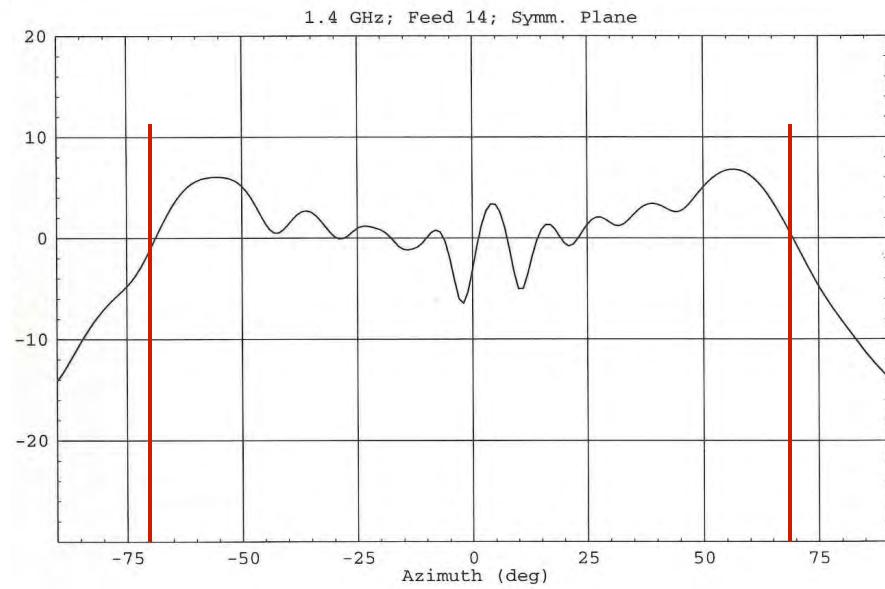
SUBREFLECTOR PATTERN AT 1.2 GHz



SUBREFLECTOR SCATTERED BEAM (1.4 GHz)



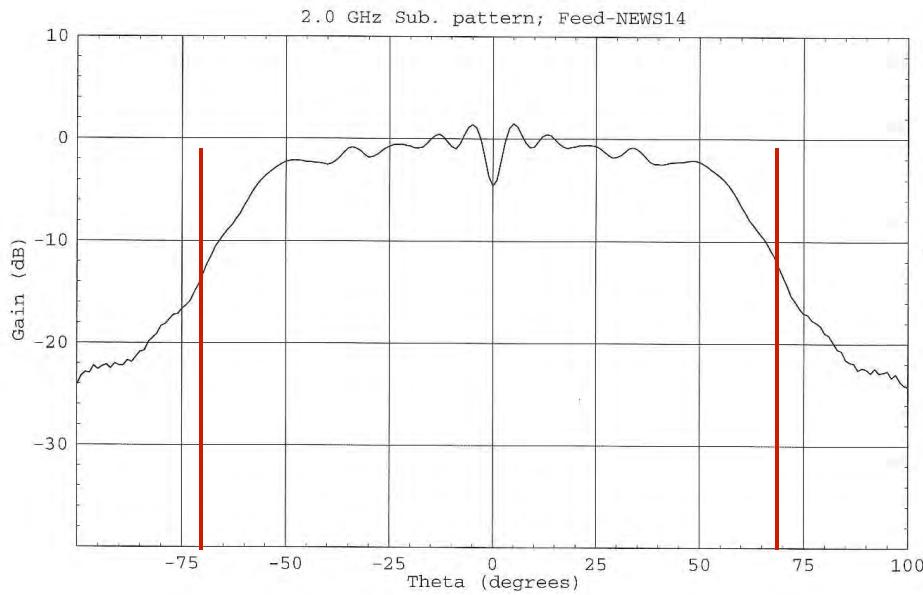
HYPERBOLIC SUBREFLECTOR



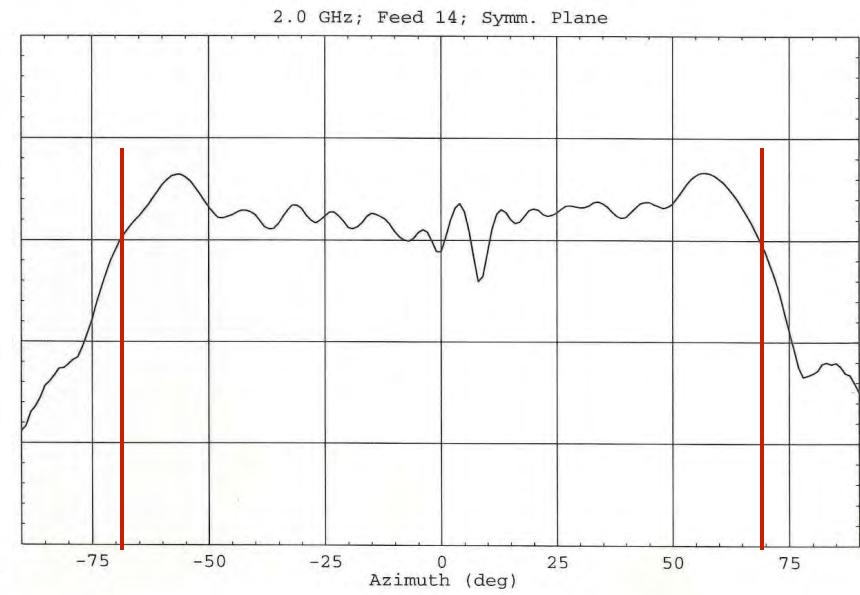
VLA SHAPED

$$\Theta_{\text{edge}} = 67.86^\circ$$

SUBREFLECTOR SCATTERED BEAM (2.0 GHz)



HYPERBOLIC SUBREFLECTOR



VLA SHAPED

$$\Theta_{\text{edge}} = 67.86^\circ$$