

A Study of the Compact Water Vapor Radiometer for the Karl G. Jansky Very Large Array

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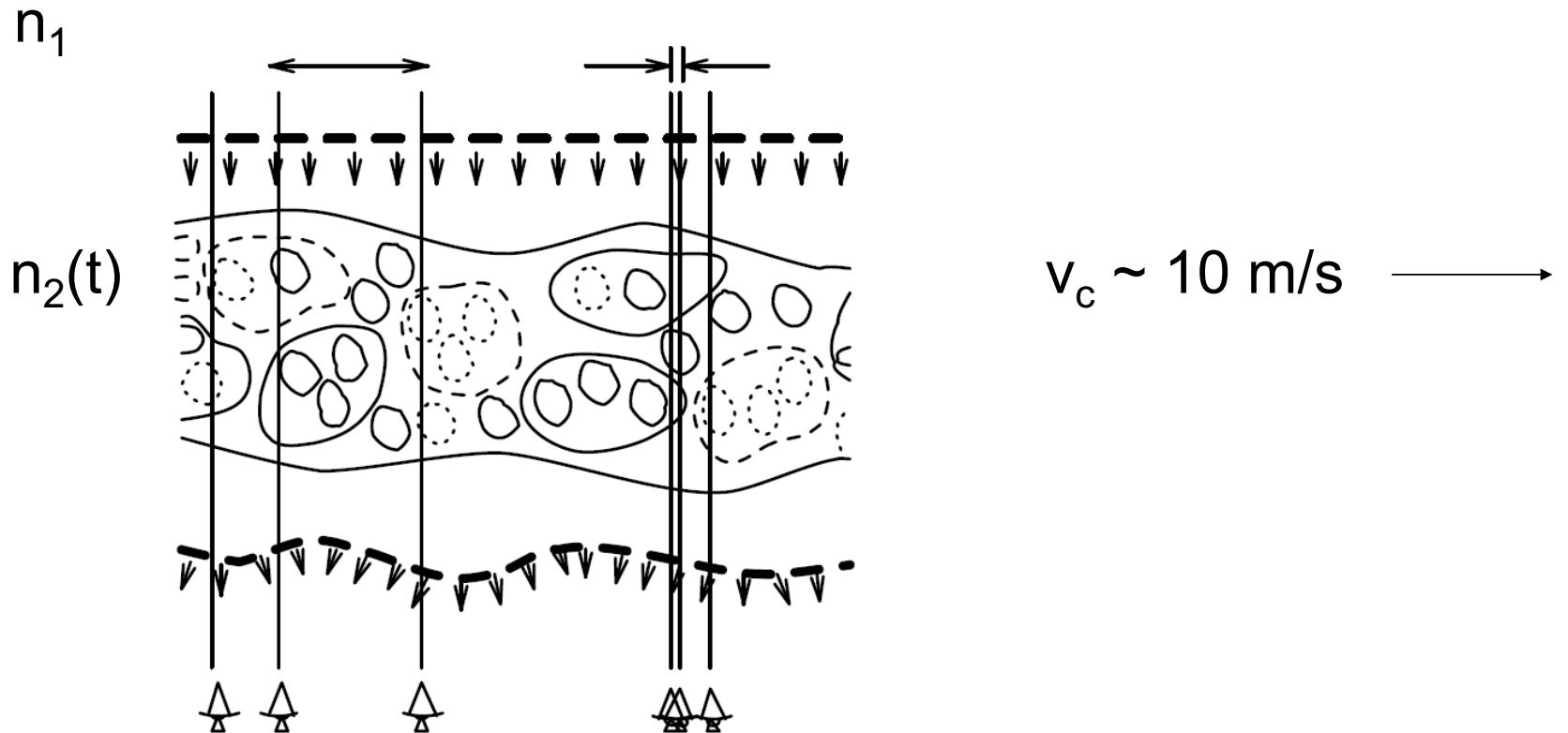
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Craig Hennies, Wayne Koski, George Peck, Brent Willoughby, Matt Morgan

Acknowledgment: NRAO Graduate Summer Research Assistantship Program



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TORONTO



$$\mathcal{L} \simeq \mathcal{L}_D + \mathcal{L}_V \simeq 0.228P_0 + 6.3w$$

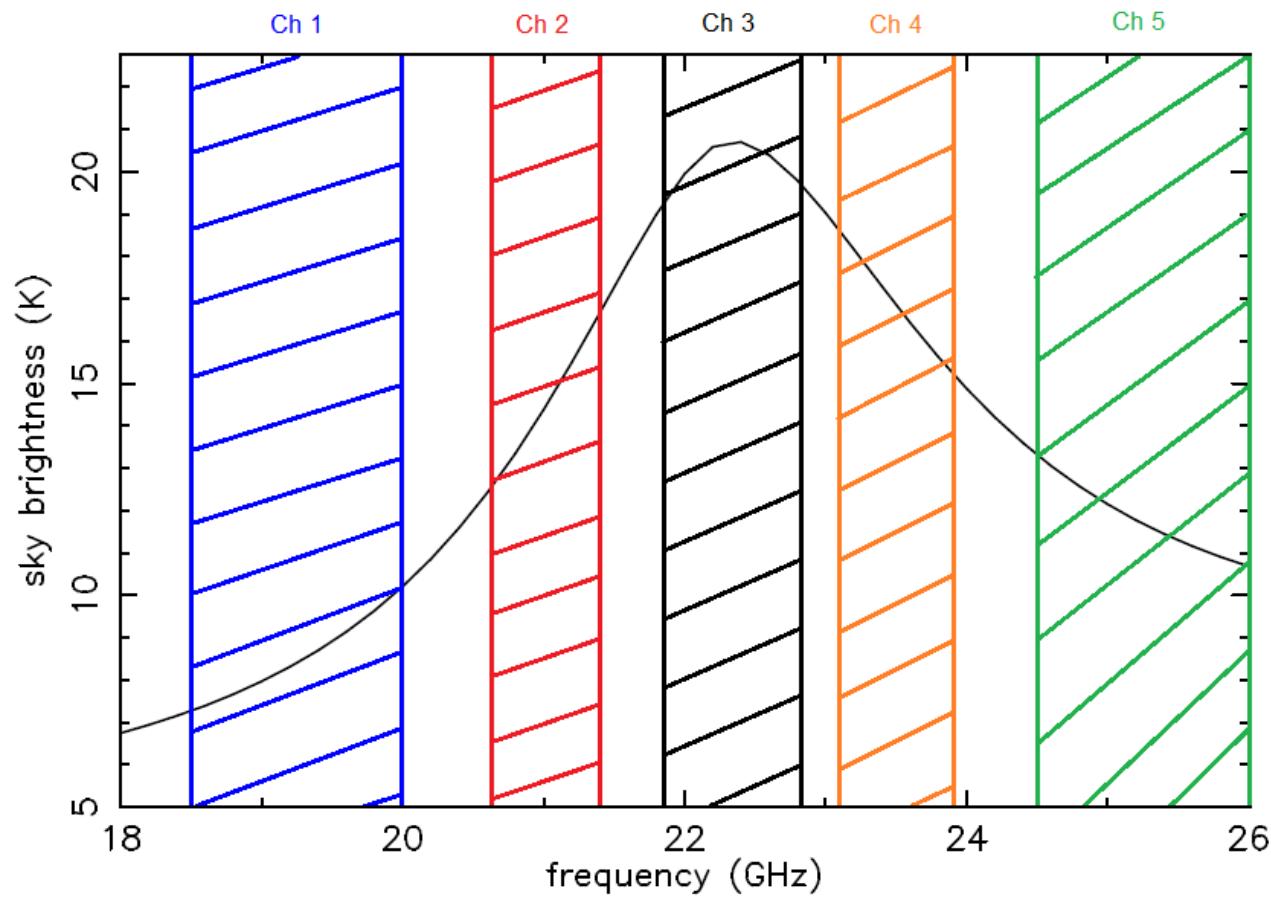
Water Vapor Radiometry

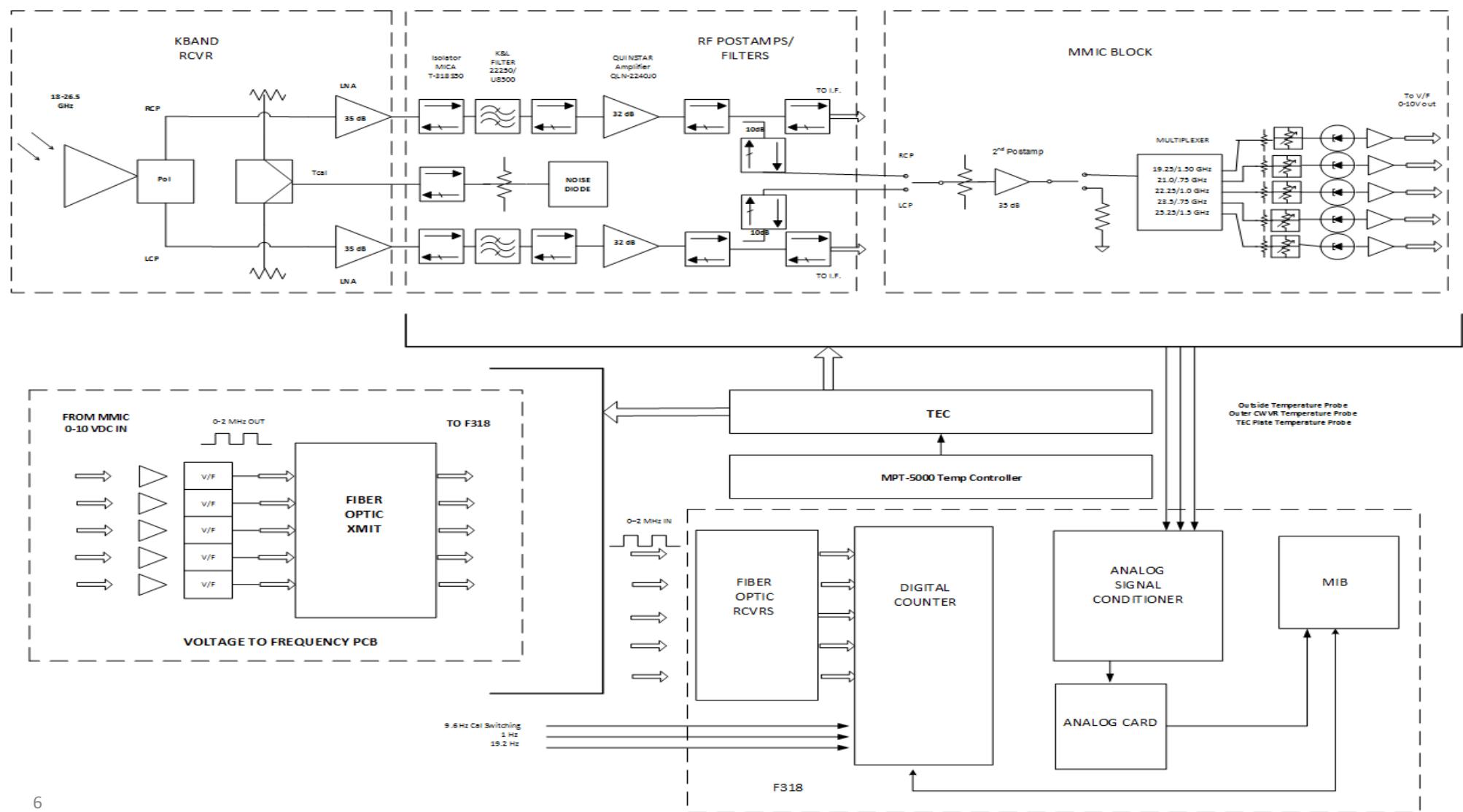
- WV \longrightarrow Continuum & Line Emission, T_{sky}
- ΔWV \longrightarrow $\Delta T_{\text{sky}} \propto \Delta \phi_{\text{astro}} \longrightarrow$ Empirical Correction Factor
- Liquid water \longrightarrow Continuum
- Observe 22 GHz WV line
- Channels at line & away from line
- Distinguish liquid water & WV

Objectives

- Characterize CWVR prototype in lab
- Gain stability
- Temperature stability
- Channel isolation
- Dynamic range
- Pathfinder to evaluate WVR for EVLA and ngVLA

CWVR 5 Channels





Instrument Setup



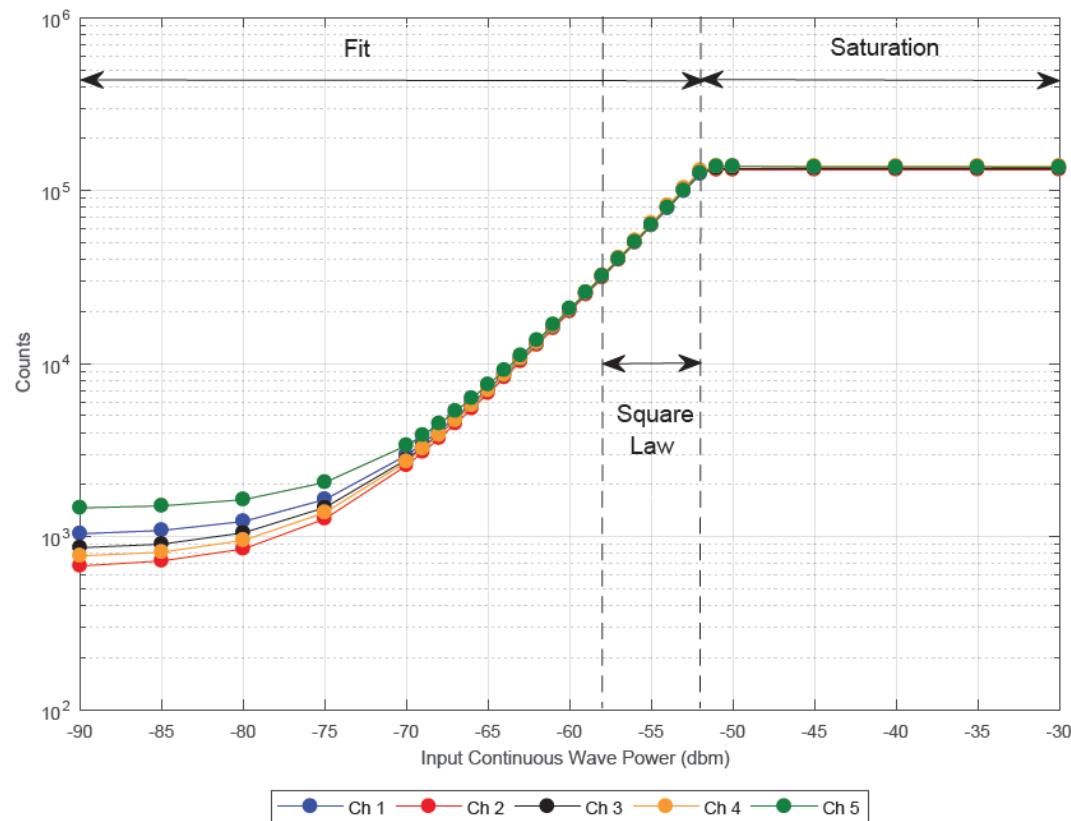
- Gain Stability Requirements (4 Channels)

- $\Delta T \propto \Delta P_{in} = w_2 P_2 + w_3 P_3 + w_4 P_4 + w_5 P_5$
 - $w_2 = -0.5, w_3 = 1, w_4 = -0.5, w_5 = 0.25$
 - $\sim 35 \mu\text{m}$ of WV $\longrightarrow 220 \mu\text{m}$ of electrical path delay ($\lambda/30$ for $\lambda = 7 \text{ mm}$)
 - For $\Delta T_{rms} \sim 25 \text{ mK}, T_{i,rms} \sim 20 \text{ mK}$
 - For $T_{sys} = 50 - 100 \text{ K}$ and $\tau = 2.5 - 10^3 \text{ seconds}$
 - $\Delta g / g \sim 2.5 - 5 \times 10^{-4}$ $\Delta g_i / g_i \sim 2 - 4 \times 10^{-4}$
-

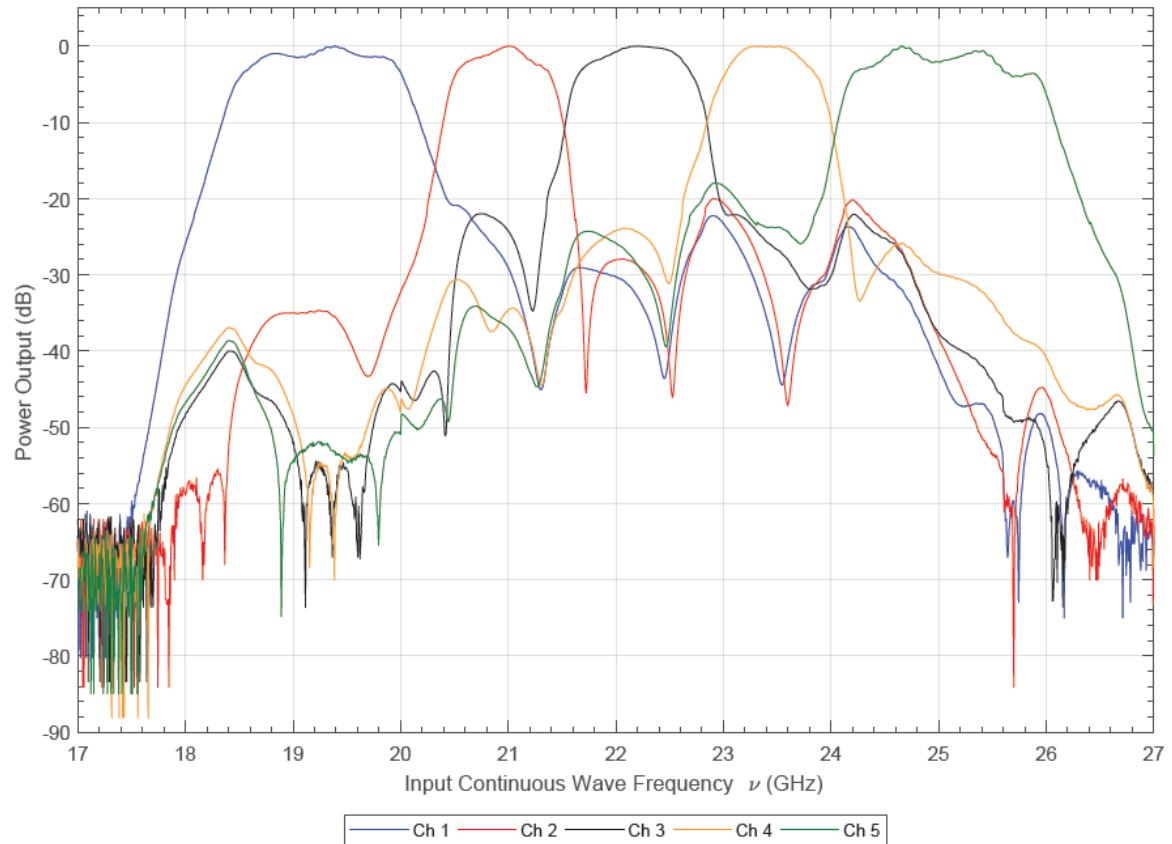
- Channel Isolation Requirements (4 Channels)

- $\sim -20 \text{ dB}$
- $\sim 1\%$ power leakage between any two channels

Dynamic Range



Channel Isolation

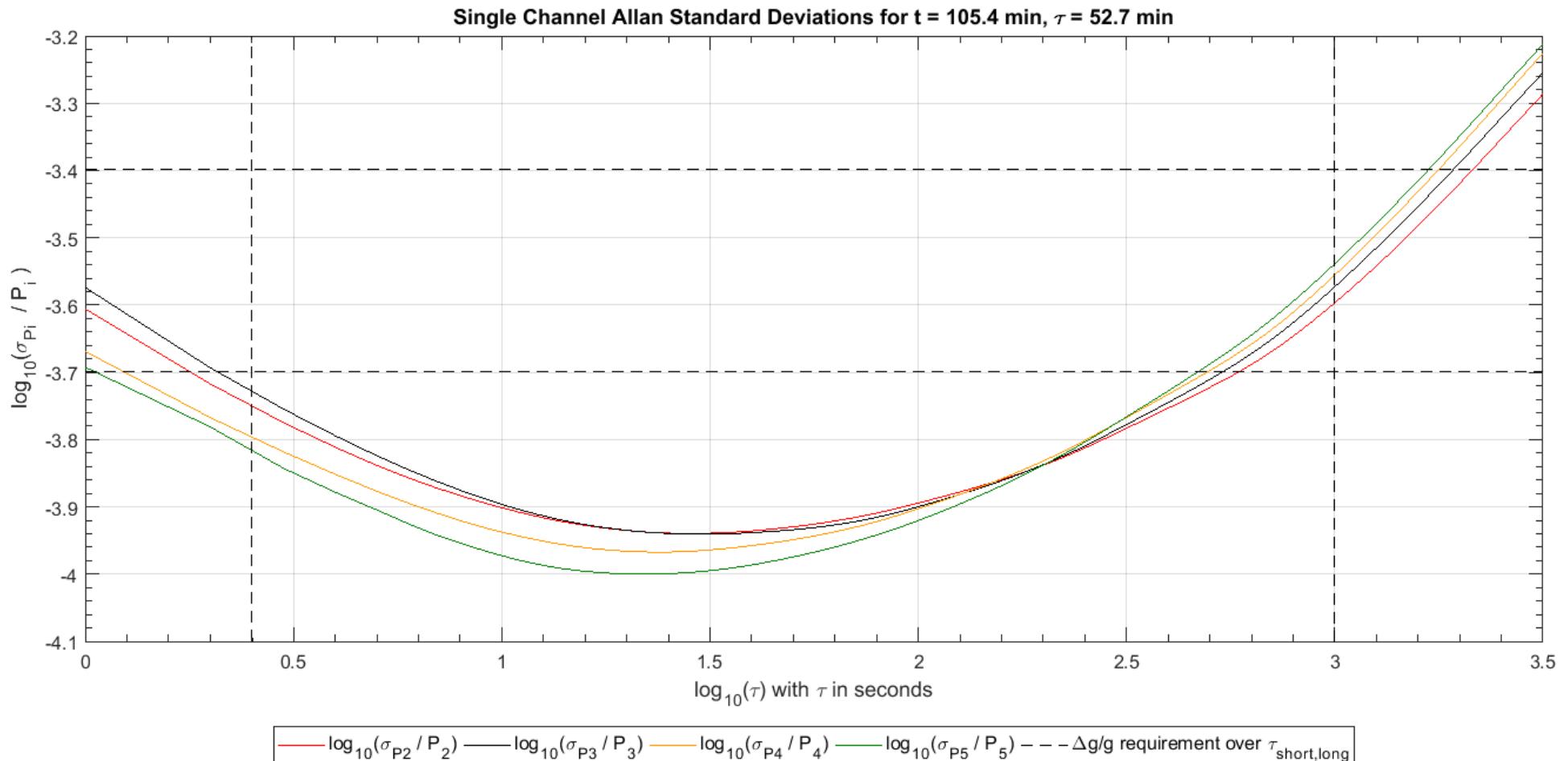


Channel Isolation Values

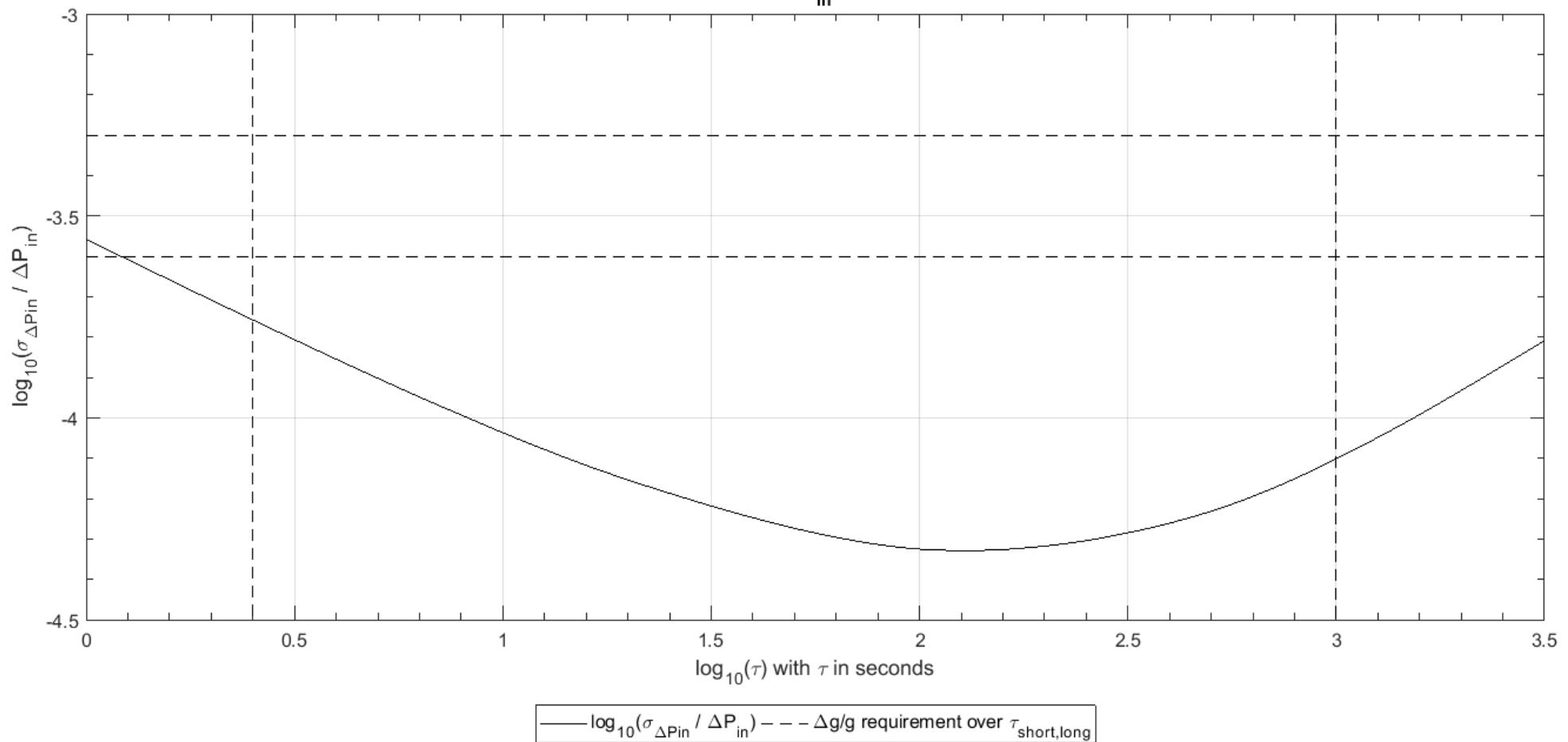
- $$IS_{xy} = \frac{\int_{\nu_i}^{\nu_f} P_x(\nu)P_y(\nu)d\nu}{\int_{\nu_i}^{\nu_f} P_y(\nu)d\nu}$$

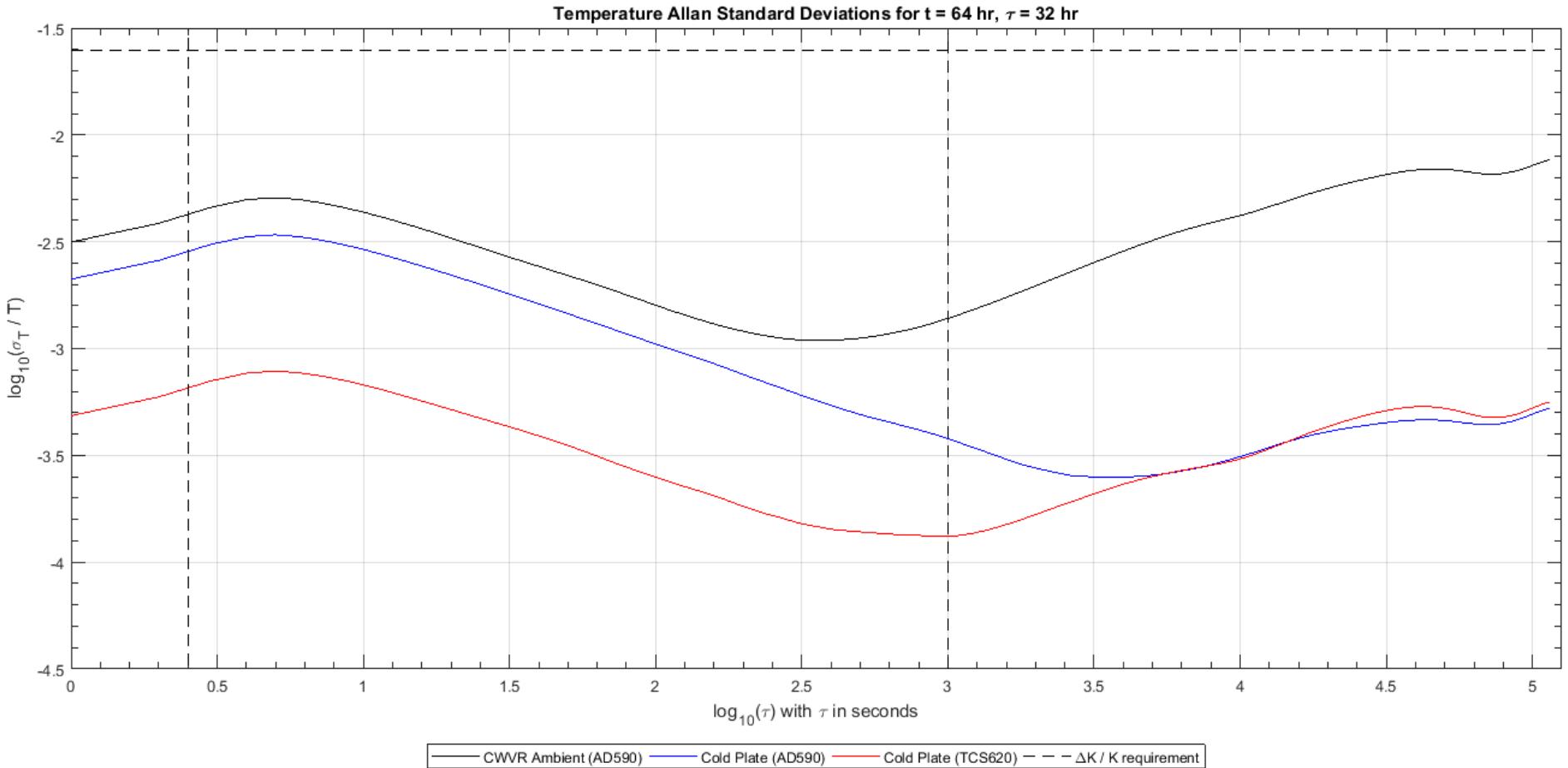
where IS_{xy} is leakage of x into y

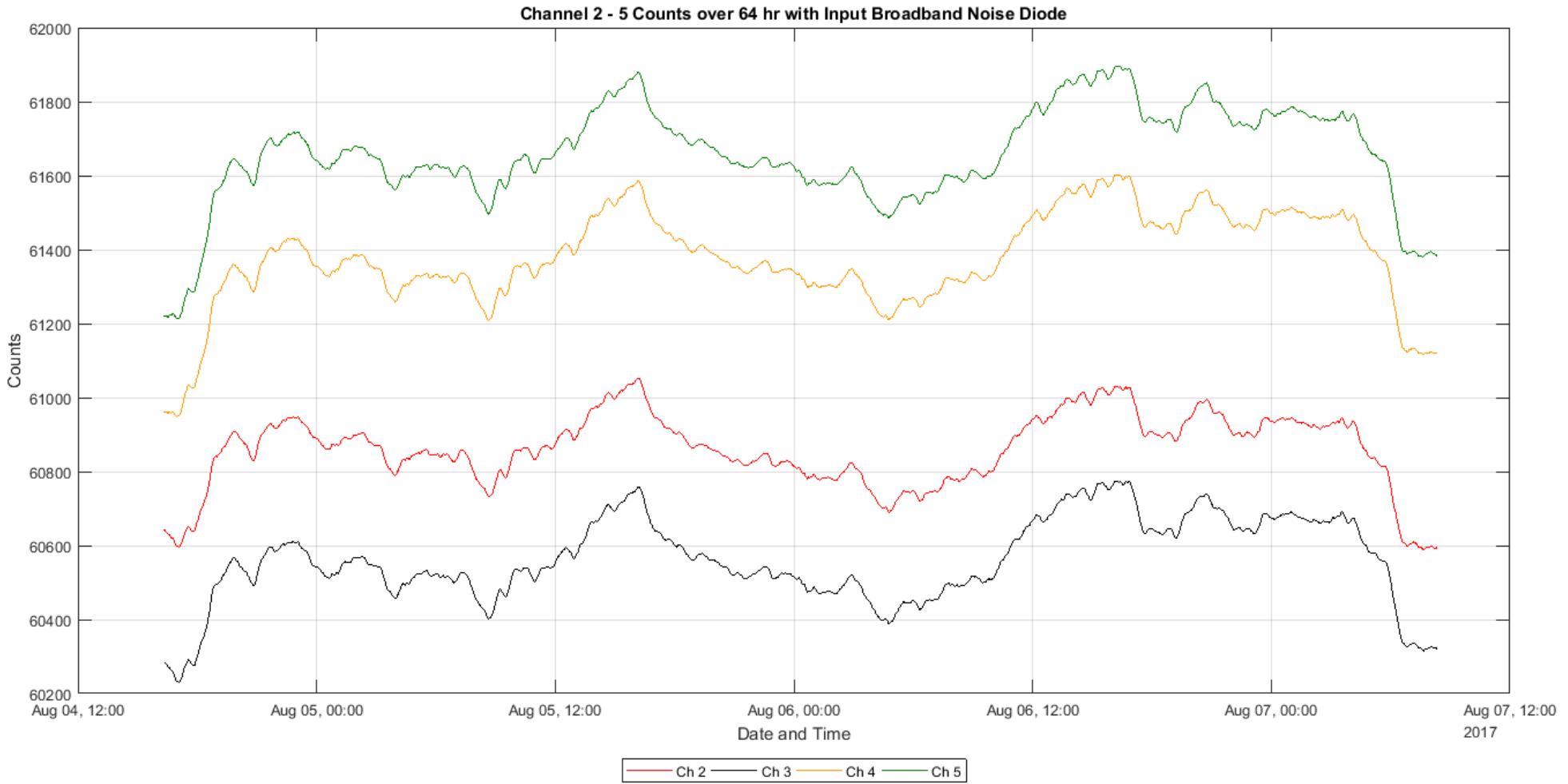
IS_{12} (dB)	IS_{13} (dB)	IS_{14} (dB)	IS_{15} (dB)
-25.09	-30.79	-29.25	-32.38
IS_{21} (dB)	IS_{23} (dB)	IS_{24} (dB)	IS_{25} (dB)
-27.42	-22.90	-26.10	-27.72
IS_{31} (dB)	IS_{32} (dB)	IS_{34} (dB)	IS_{35} (dB)
-31.99	-21.78	-20.25	-25.46
IS_{41} (dB)	IS_{42} (dB)	IS_{43} (dB)	IS_{45} (dB)
-31.15	-25.67	-20.95	-22.74
IS_{51} (dB)	IS_{52} (dB)	IS_{53} (dB)	IS_{54} (dB)
-32.34	-25.35	-24.22	-20.81

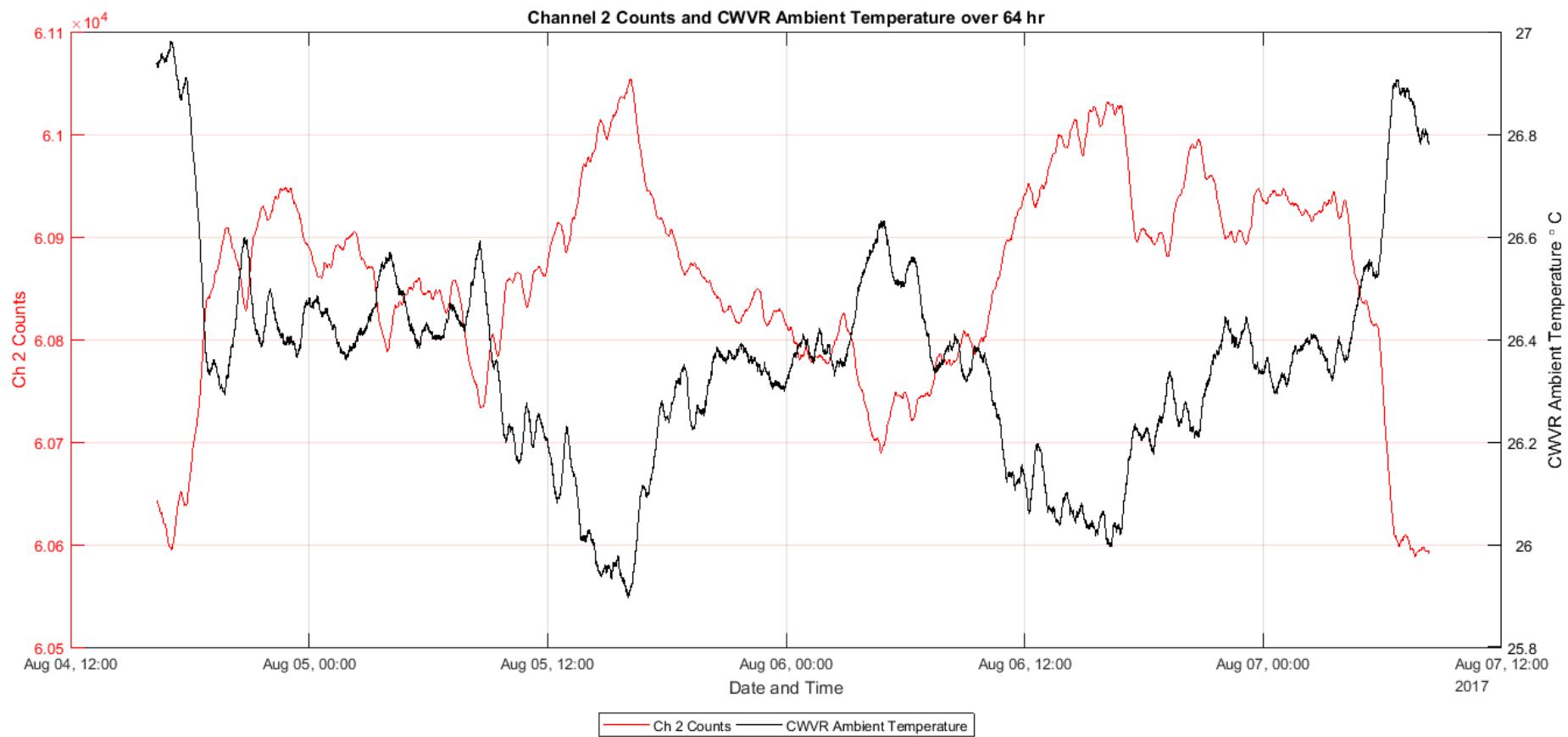


Allan Standard Deviation of ΔP_{in} for $t = 105.4$ min, $\tau = 52.7$ min

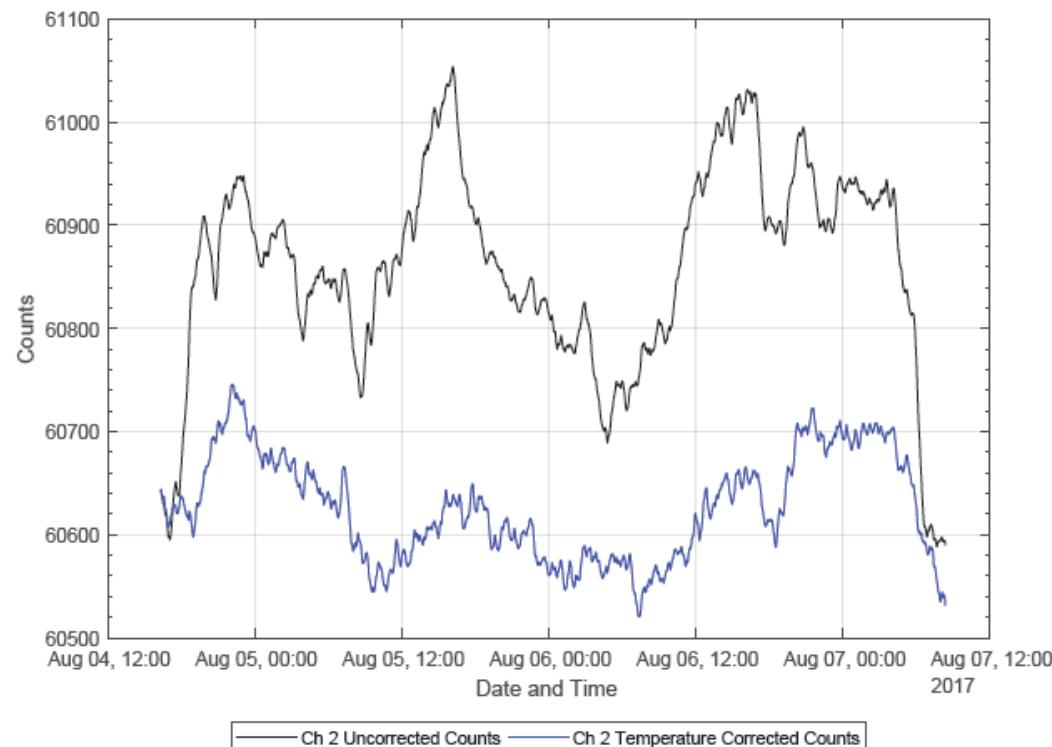






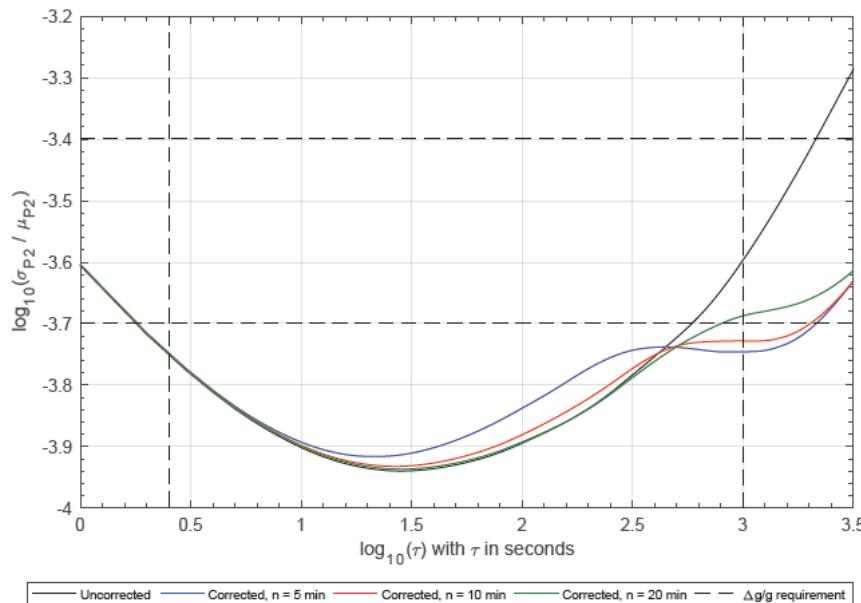


Temperature Correction

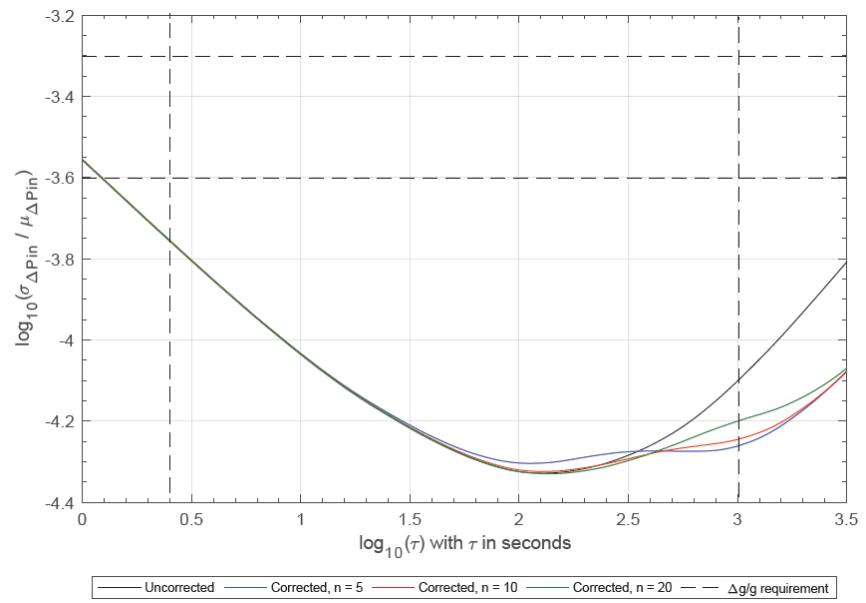


Stability with Temperature Correction

Single channel



Observable



Summary

- Phase fluctuations limit resolution and sensitivity
- CWVR prototype tested in lab
- Gain and temperature stability requirement met
- Channel isolation requirement met
- Correlation between temperature and gain
- Temperature correction improves stability
- EVLA Memo 203

Future

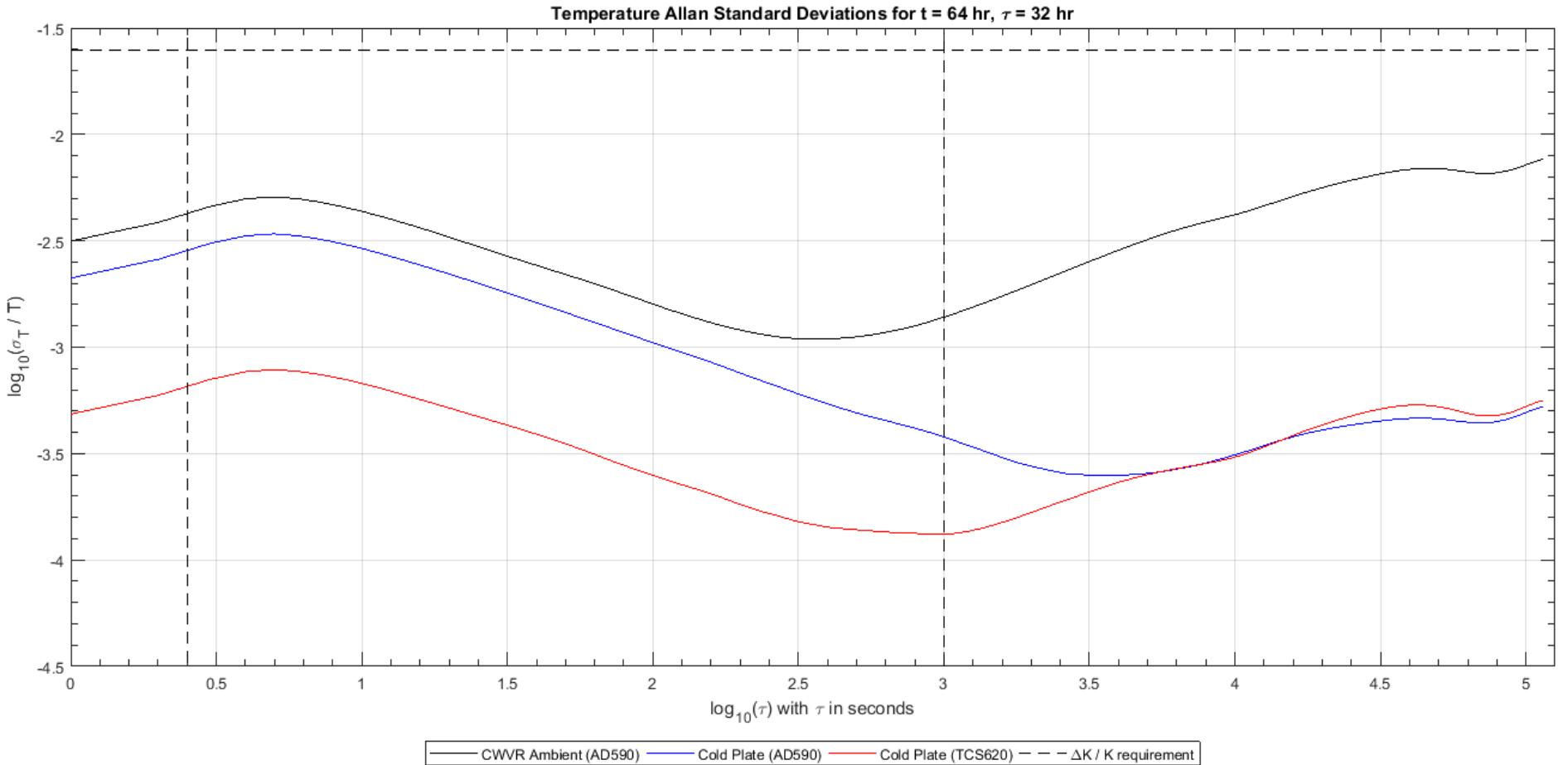
- Build and install four CWVRs for further on-sky testing
- Evaluate use of WVR for EVLA and ngVLA

References

1. Butler, B., Some Issues for Water Vapor Radiometry at the VLA, VLA Scientific Memo # 177, 1999.
2. Carilli, C. L, and Holdaway, M. A, Tropospheric phase calibration in millimeter interferometry, *Radio Science*, vol. 34, no. 4, pp. 817-840, 1999.
3. Chandler, C. J, Brisken, W. F, Butler, B. J, Hayward, R. H, M.,Willoughby, B. E, Results of Water Vapor Radiometry Tests at the VLA, EVLA Memo # 73, 2004.
4. Chandler, C. J, Brisken, W. F, Butler, B. J, Hayward, R. H, Morgan, M.,Willoughby, B. E, A Proposal to Design and Implement a Compact Water Vapor Radiometer for the EVLA, EVLA Memo # 74, 2004.
5. Clark, B., Calibration Strategies for the Next Generation VLA, ngVLA Memo # 2, 2015.
6. Desai, K., Measurement of turbulence in the interstellar medium, Ph.D. thesis, 89 pp., Univ. of Calif. at Santa Barbara, 1993.
7. Holdaway, M. A., Possible phase calibration schemes for the MMA, Millimeter Array Memo. 84, 14 pp., Natl. Radio Astron. Obs., Socorro, N. M., 1992.
8. Thompson, A. R, Moran, J. M, Swenson Jr., G. W, *Interferometry and Synthesis in Radio Astronomy*, Second Edition, 2001, John Wiley & Sons.
9. Sutton, E. C., and Hueckstaedt, R. M., Radiometric monitoring of atmospheric water vapor as it pertains to phase correction in millimeter interferometry, *Astron. Astrophys. Suppl. Ser.*, 119, 559-567, 1997.

Thank you.

Extra Slides



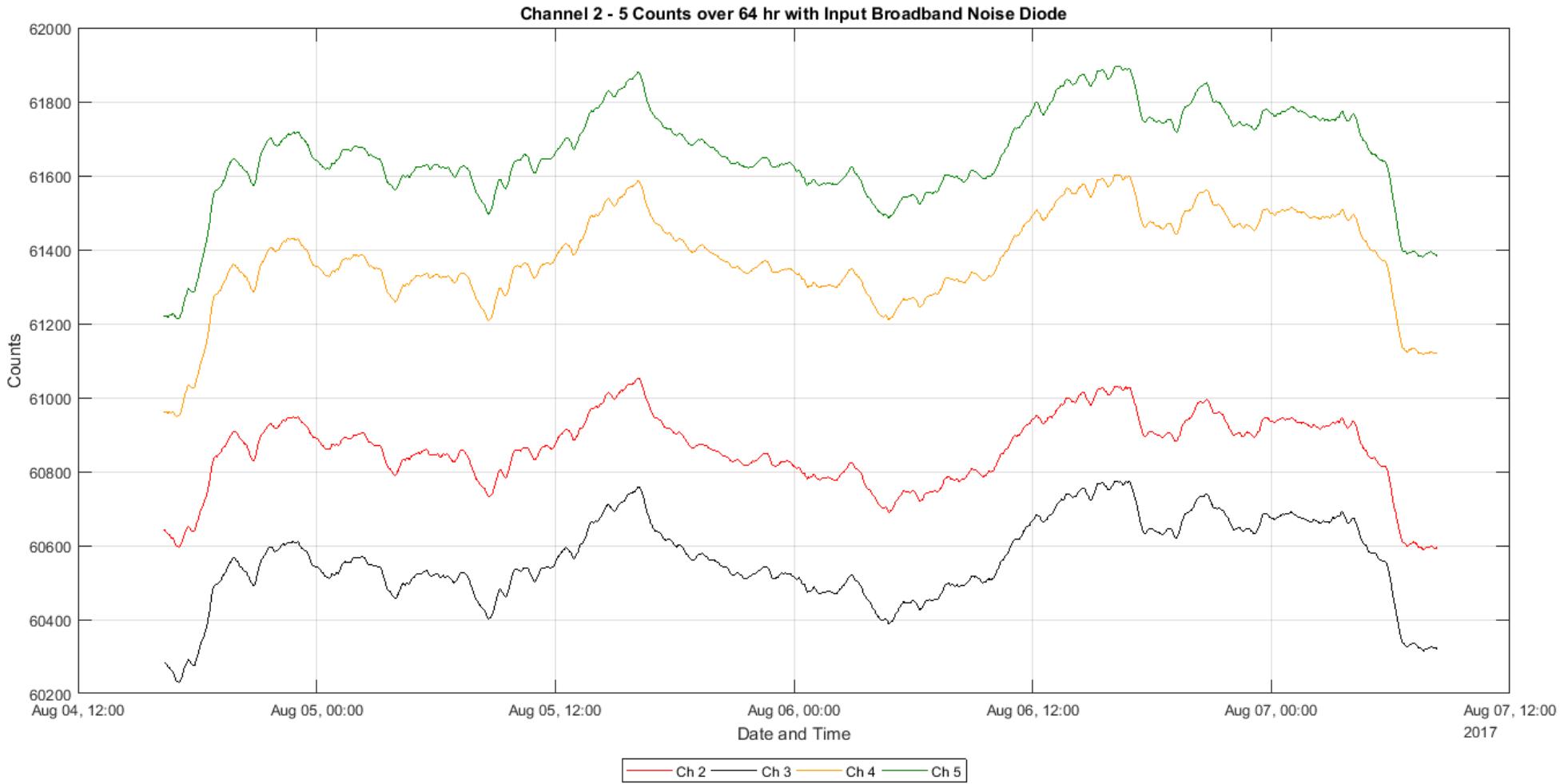
Allan Standard Deviations

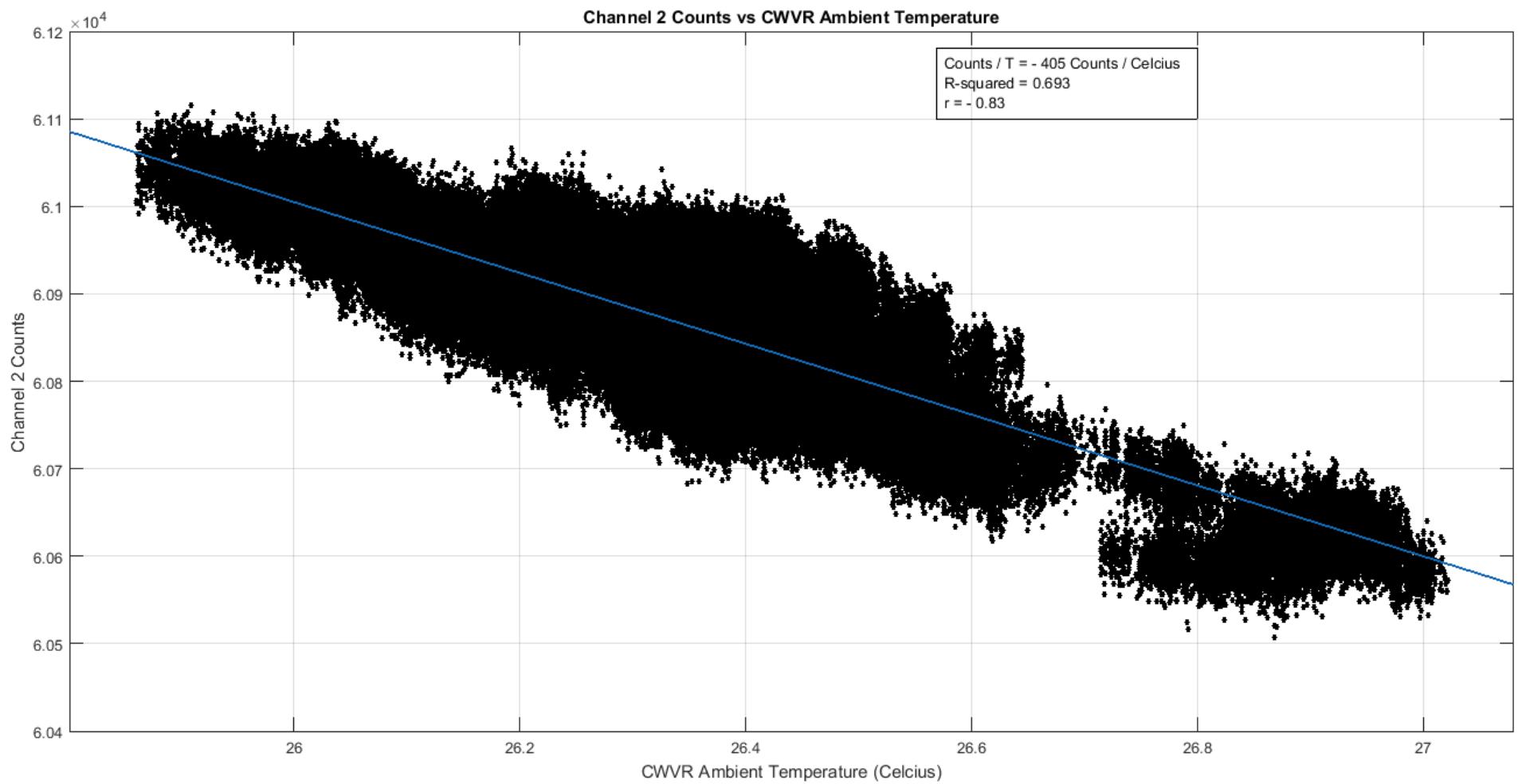
$$\sigma_P(\tau) = \left\{ \frac{1}{2} \langle \{P(t) - P(t - \tau)\}^2 \rangle \right\}^{\frac{1}{2}}$$

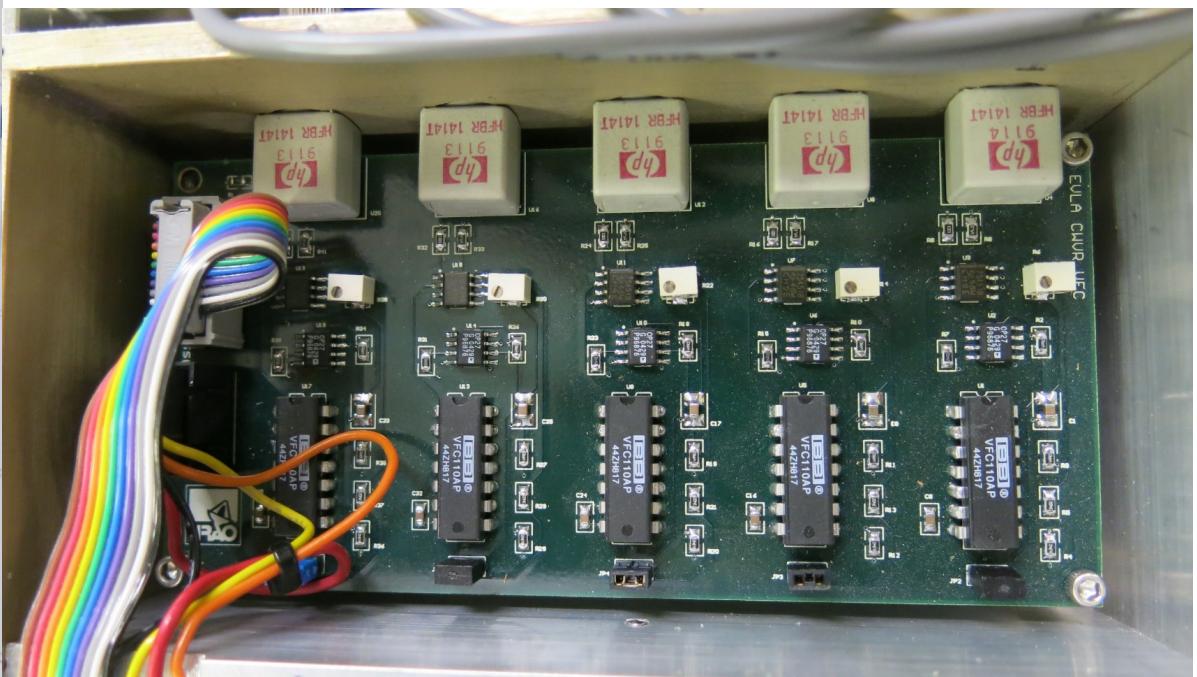
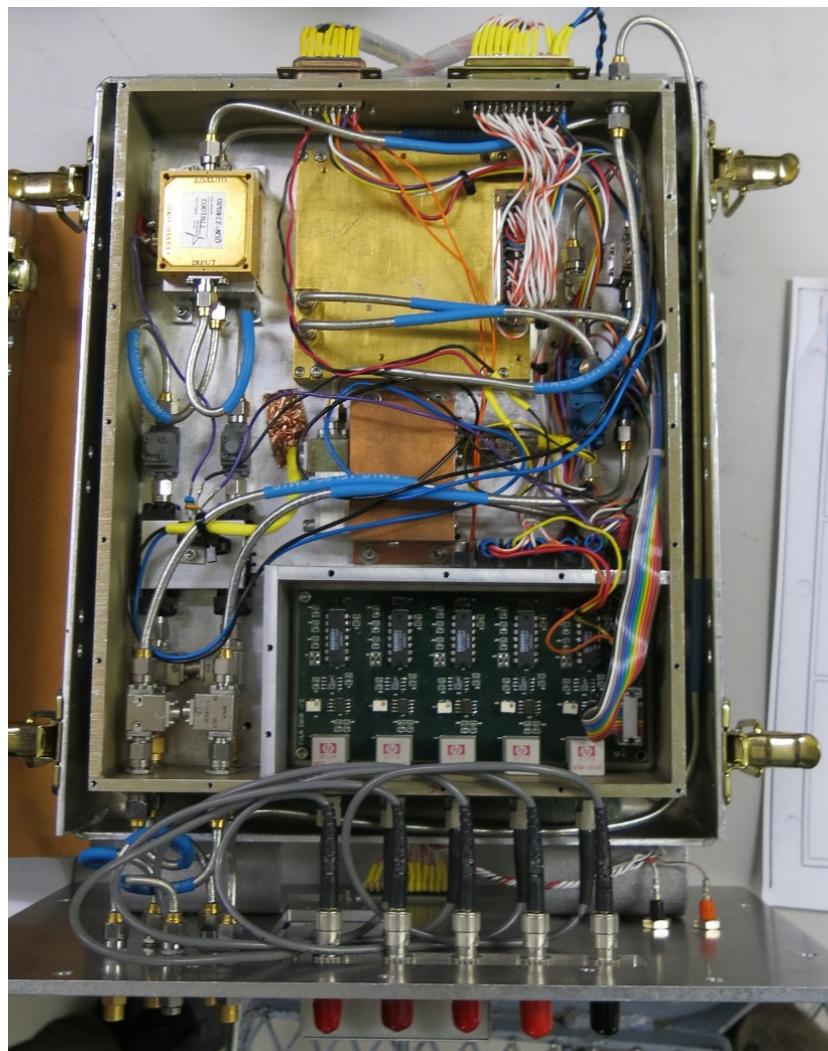
$$\sigma_P(\tau) = \left\{ \frac{1}{2} \sum_{j=1}^{N/2} \frac{1}{N - \tau_j} \sum_{i=1}^{N-\tau_j} [P(t_i + \tau_j) - P(t_i)]^2 \right\}^{\frac{1}{2}} \quad \text{and } \mu_{norm} = \langle P(t) \rangle$$

$$\sigma_{P_x - P_y}(\tau) = \left\{ \frac{1}{2} \sum_{j=1}^{N/2} \frac{1}{N - \tau_j} \sum_{i=1}^{N-\tau_j} \{[P_x(t_i + \tau_j) - P_y(t_i + \tau_j)] - [P_x(t_i) - P_y(t_i)]\}^2 \right\}^{\frac{1}{2}} \quad \text{and } \mu_{norm} = \frac{\langle P_x(t) + P_y(t) \rangle}{2}$$

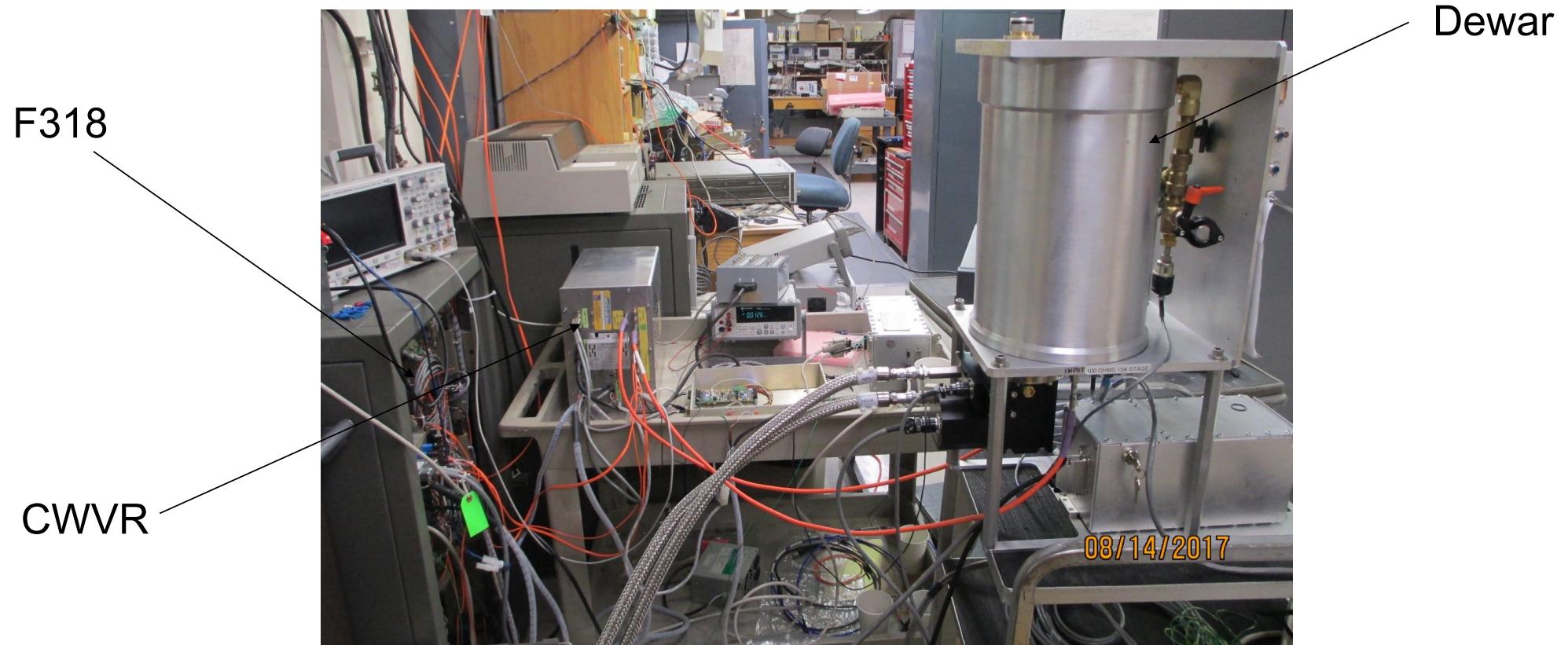
$$\sigma_{\Delta P_{in}}(\tau) = \left\{ \frac{1}{2} \sum_{j=1}^{N/2} \frac{1}{N - \tau_j} \sum_{i=1}^{N-\tau_j} \left\{ \sum_{k=1}^5 w_k P_k(t_i + \tau_j) - \sum_{k=1}^5 w_k P_k(t_i) \right\}^2 \right\}^{\frac{1}{2}} \quad \text{and } \mu_{norm} = \frac{\langle P_1(t) + P_2(t) + P_3(t) + P_4(t) + P_5(t) \rangle}{5}$$





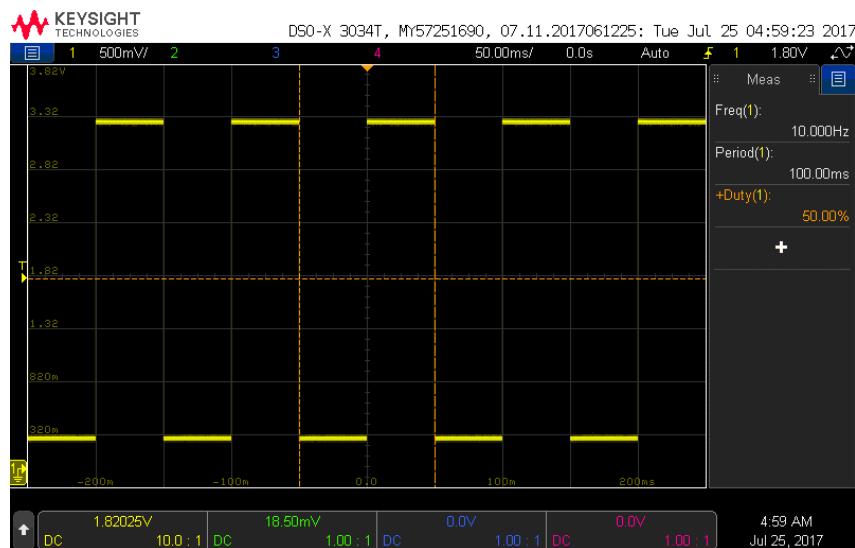


Instrument Setup

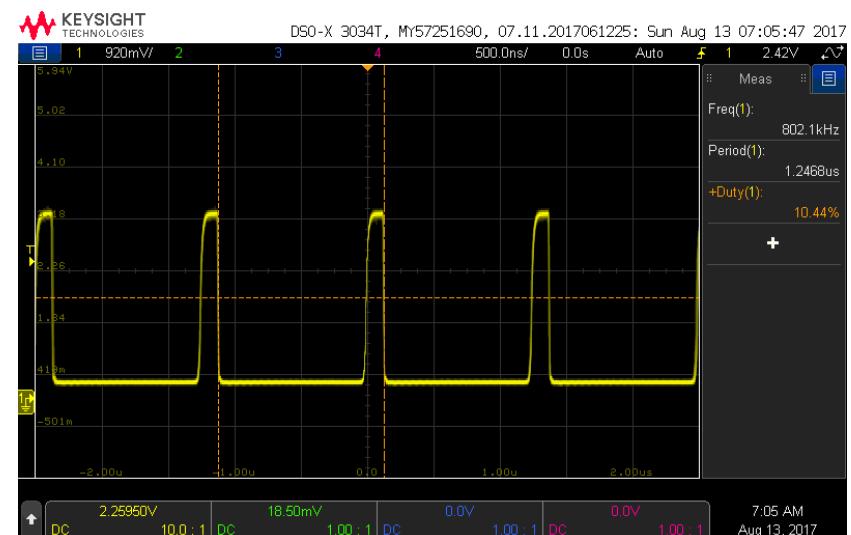


Voltage – Frequency Converter

10 Hz Calibration Signal



V-F Board Frequency Output

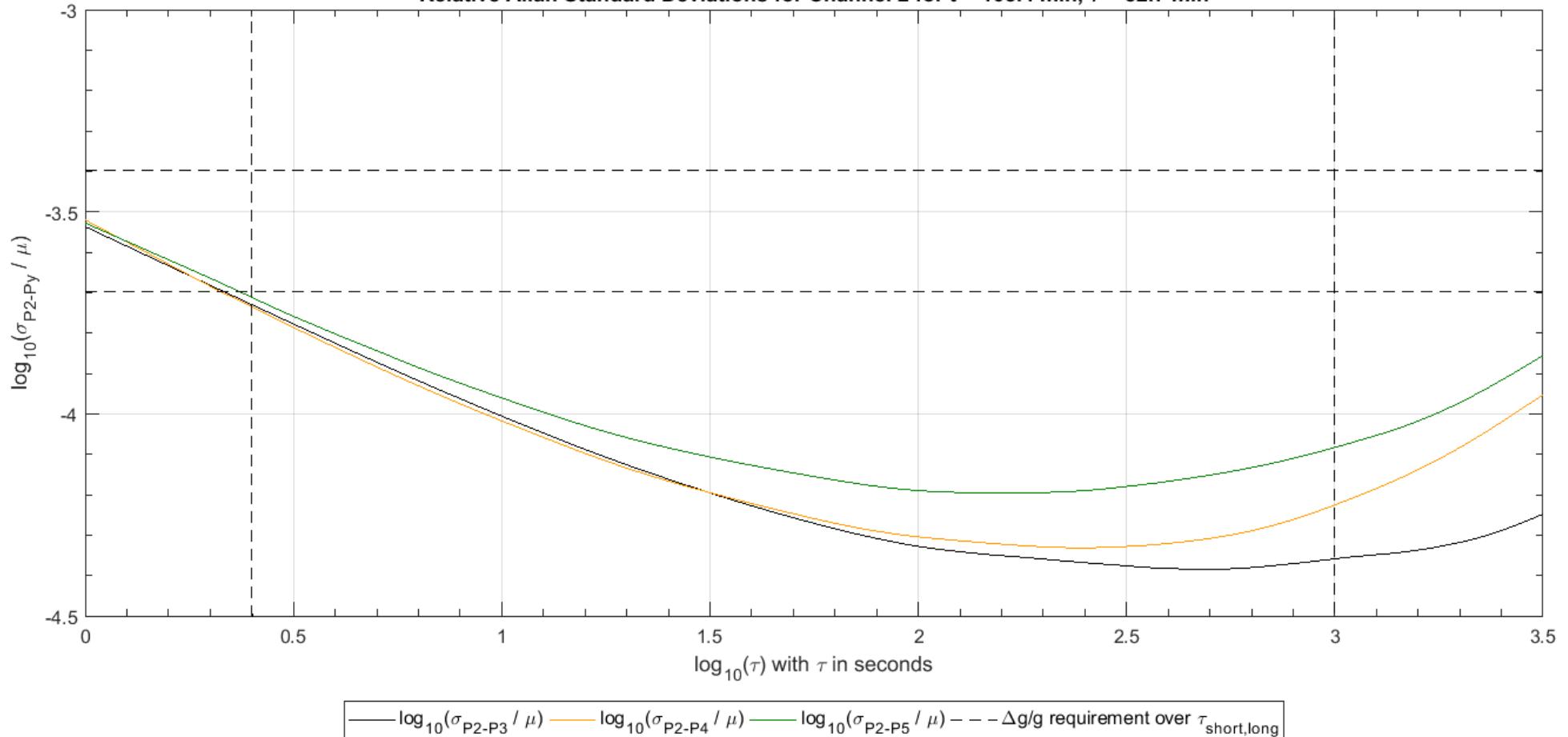


$V_{out} = 0 - 10 \text{ V} \longleftrightarrow v_{out} = 0 - 2 \text{ MHz}$

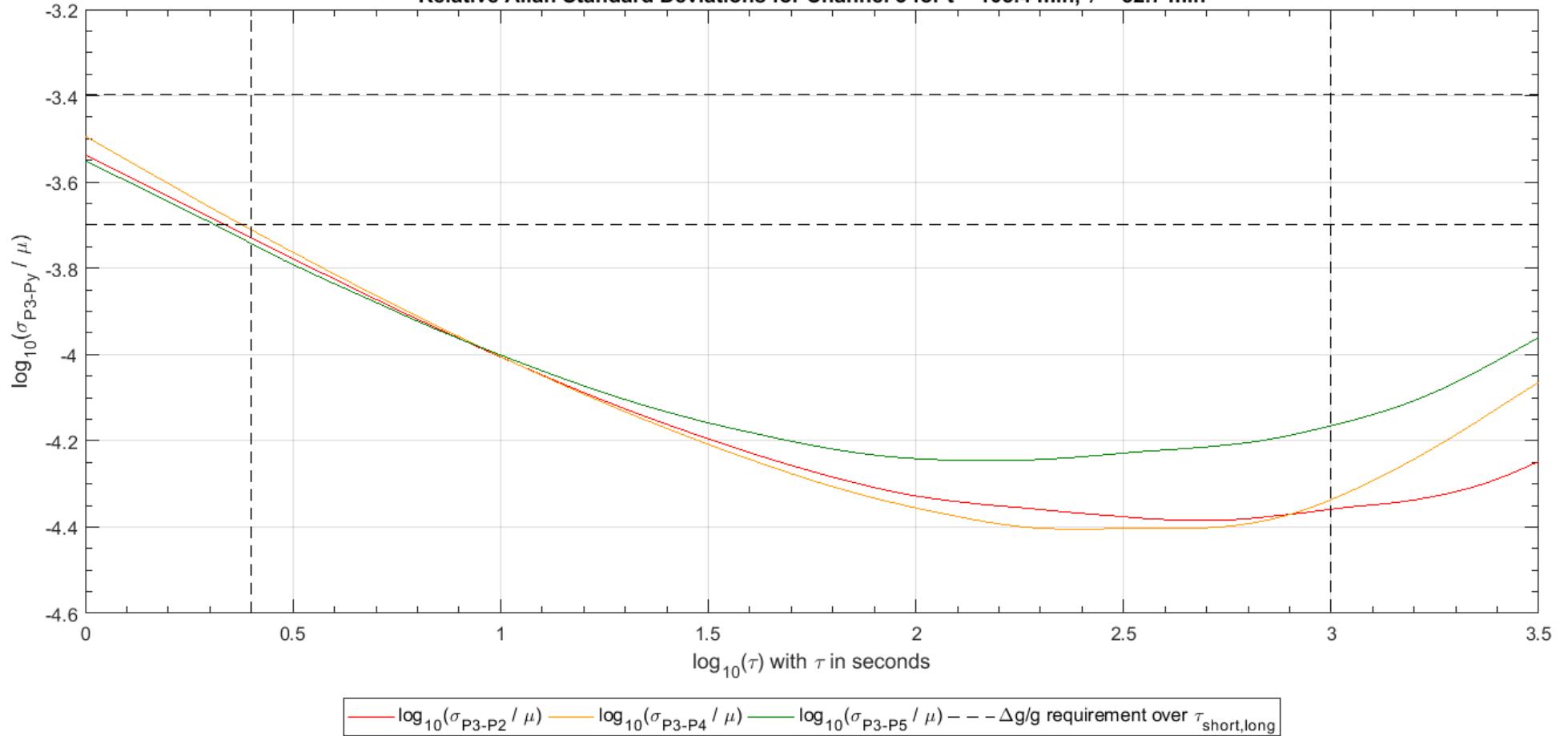
$$\text{Ch1}_{\text{Low,High}} = \frac{802.1 \times 10^3 \text{ cycles}}{\text{sec}} \times 50 \text{ ms} \times \frac{1 \text{ sec}}{10^3 \text{ ms}} \sim 40,000 \text{ cycles or counts}$$

$\text{Ch1}_{\text{Total}} = \text{Ch1}_{\text{Low}} + \text{Ch1}_{\text{High}} \sim 80,000$ cycles or counts

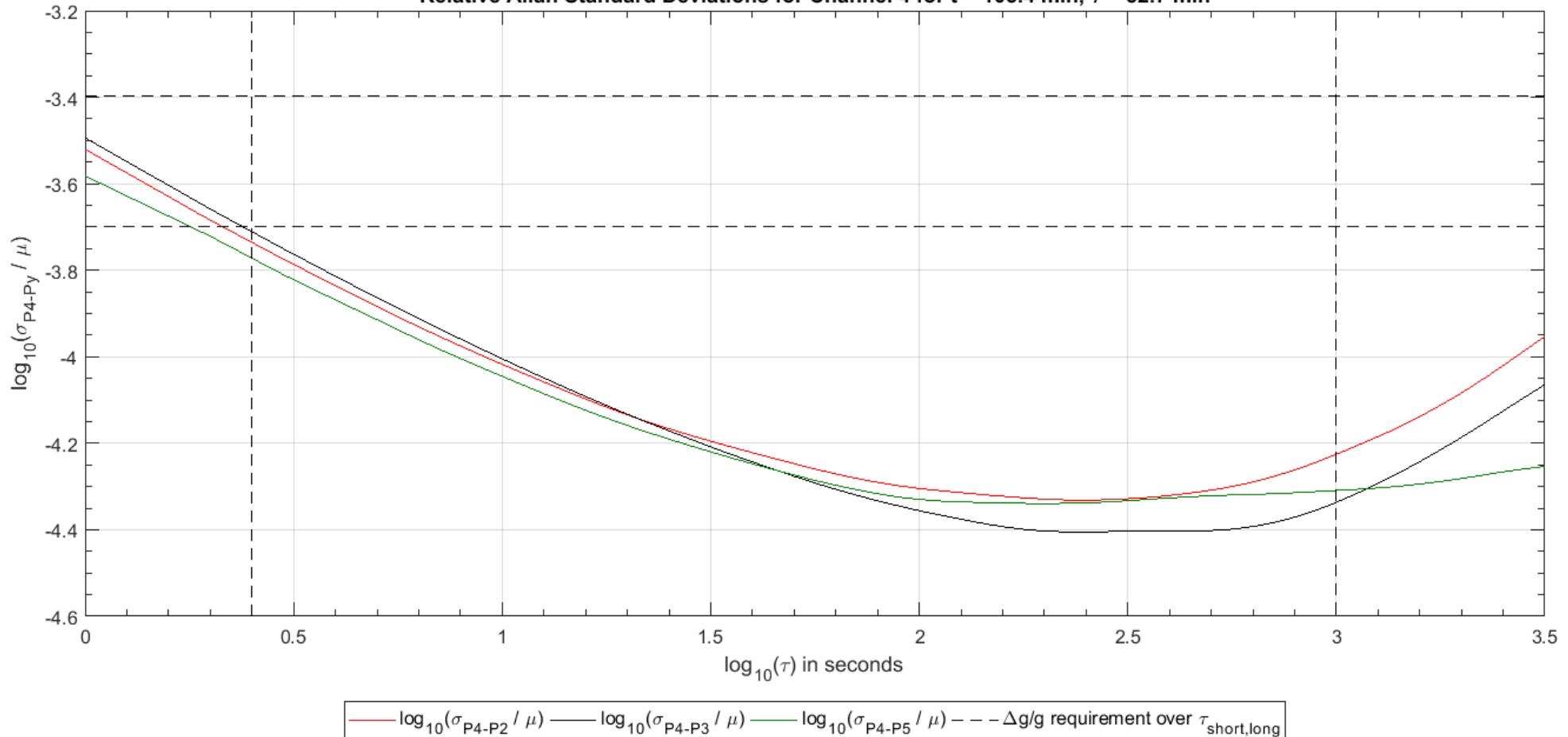
Relative Allan Standard Deviations for Channel 2 for $t = 105.4$ min, $\tau = 52.7$ min



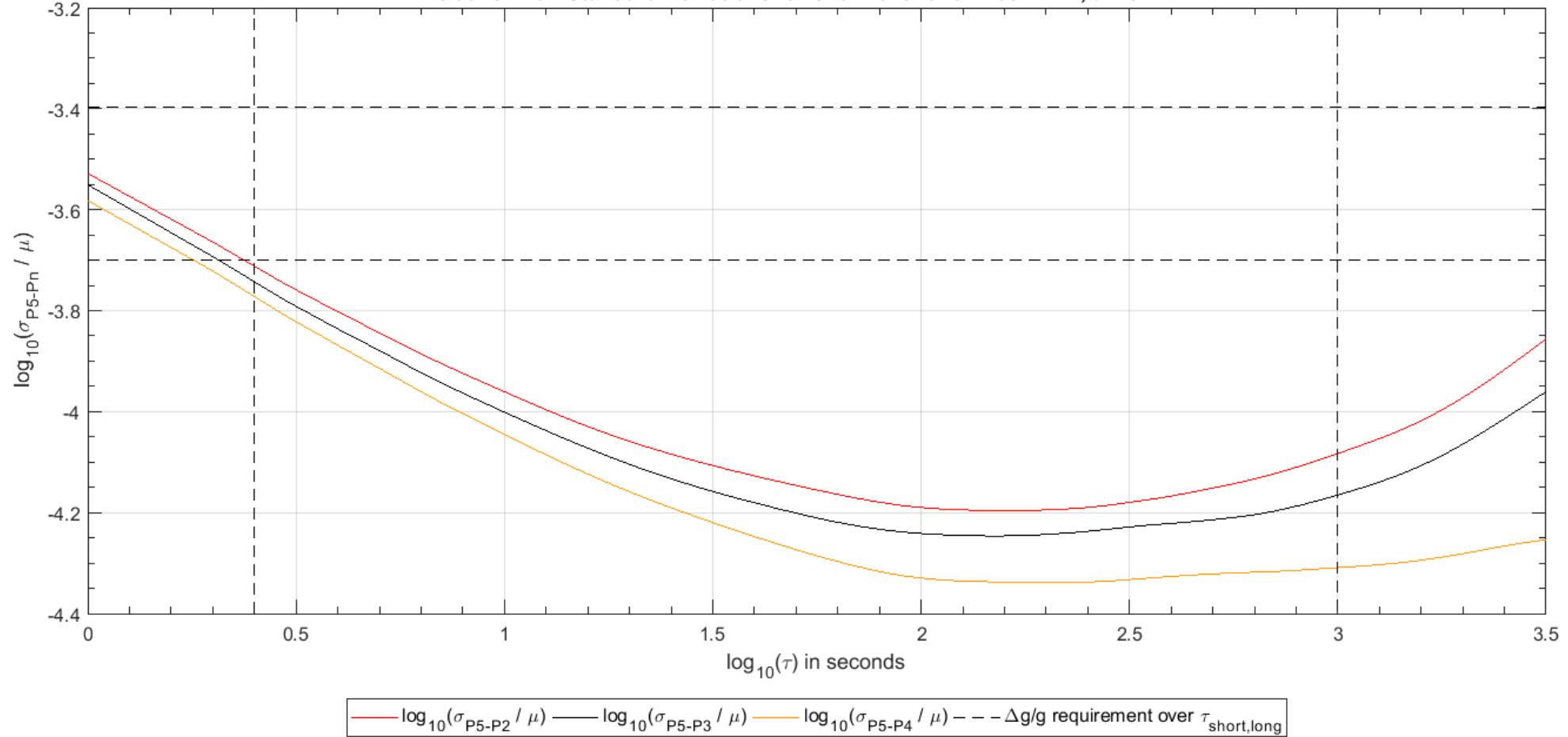
Relative Allan Standard Deviations for Channel 3 for $t = 105.4$ min, $\tau = 52.7$ min

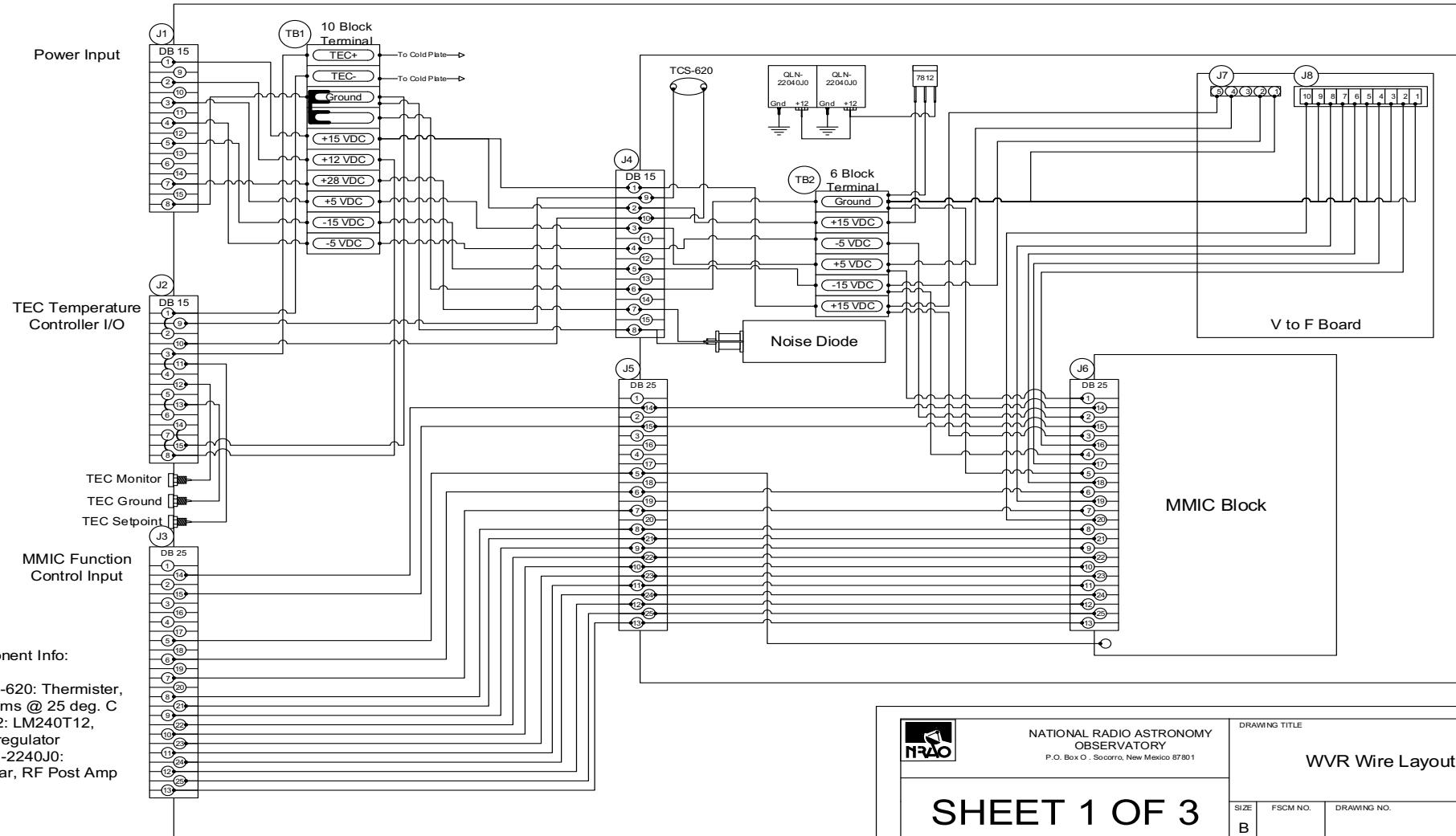


Relative Allan Standard Deviations for Channel 4 for $t = 105.4$ min, $\tau = 52.7$ min



Relative Allan Standard Deviations for Channel 5 for $t = 105.4$ min, $\tau = 52.7$ min





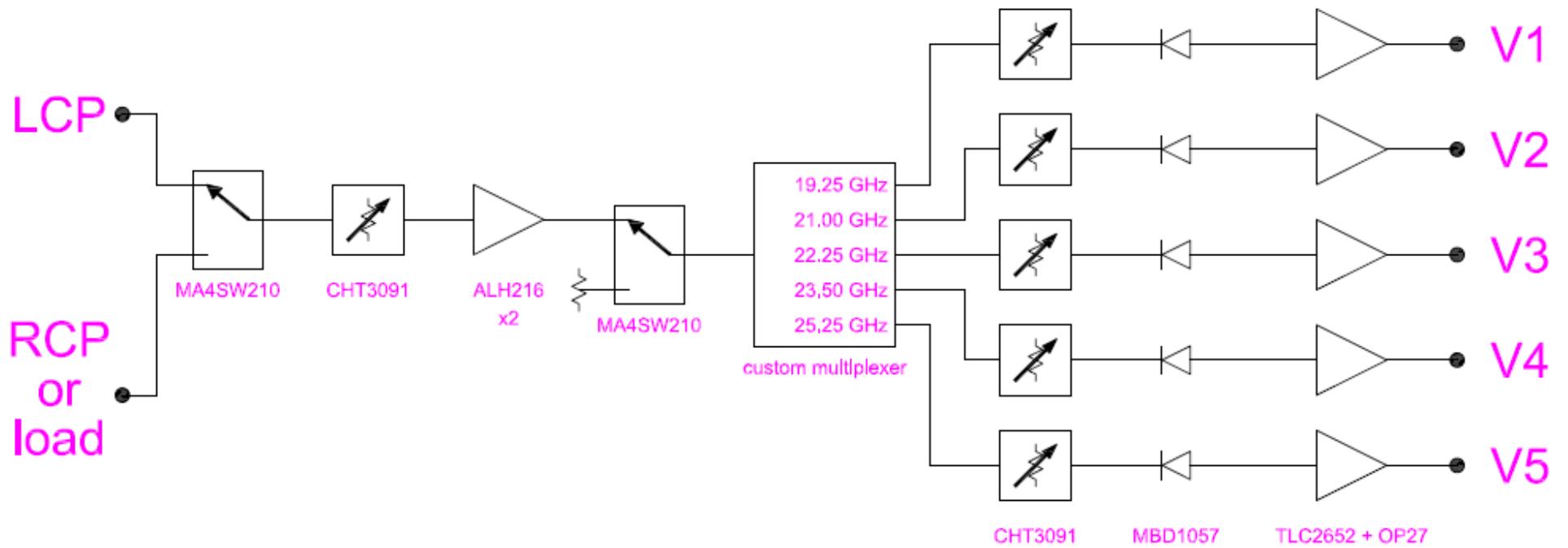
NATIONAL RADIO ASTRONOMY
OBSERVATORY
P.O. Box O - Socorro, New Mexico 87801

DRAWING TITLE

WVR Wire Layout

SHEET 1 OF 3

SIZE	FSCM NO.	DRAWING NO.
B		



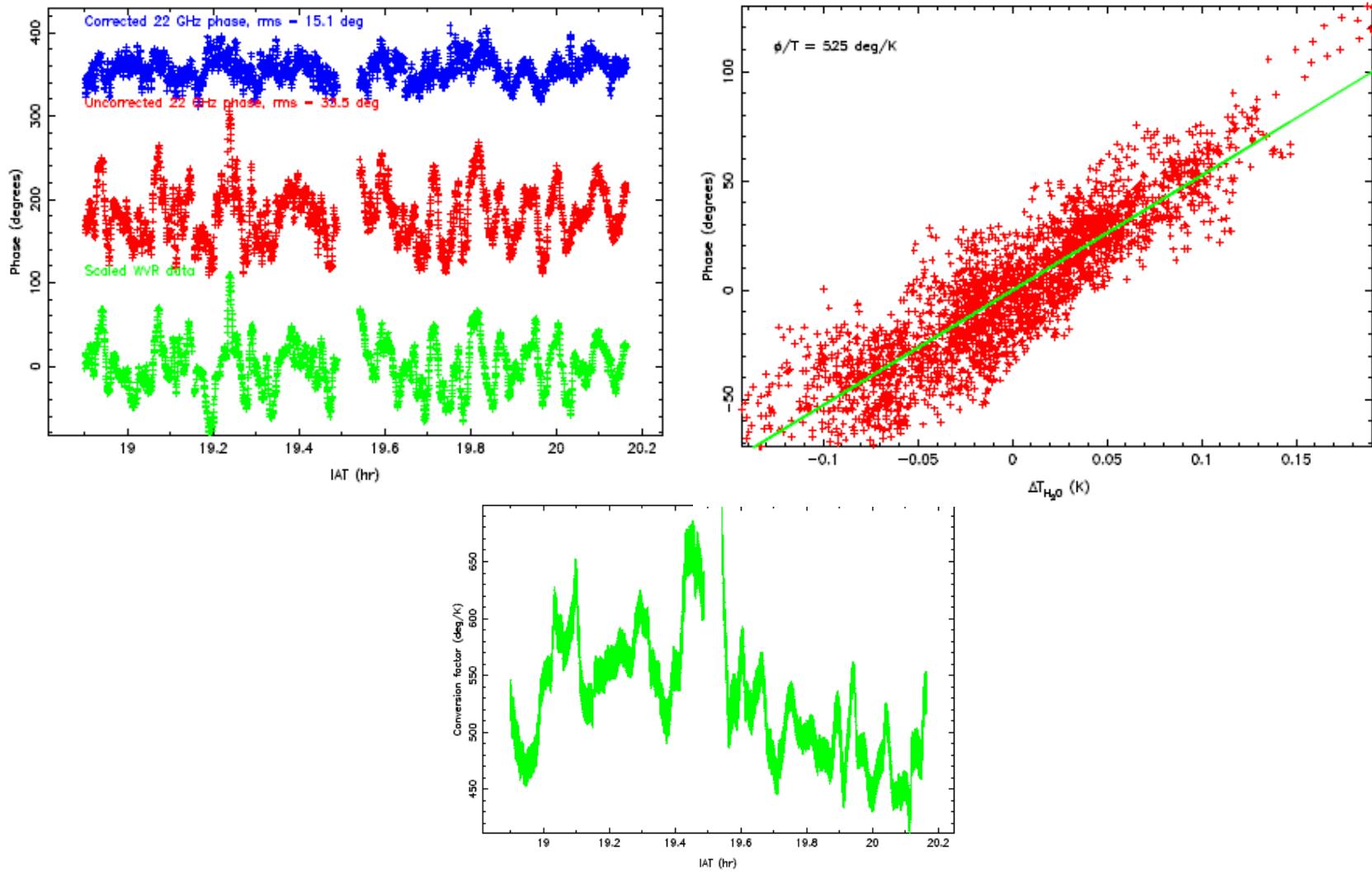
- Gain Stability Requirements (5 Channels)

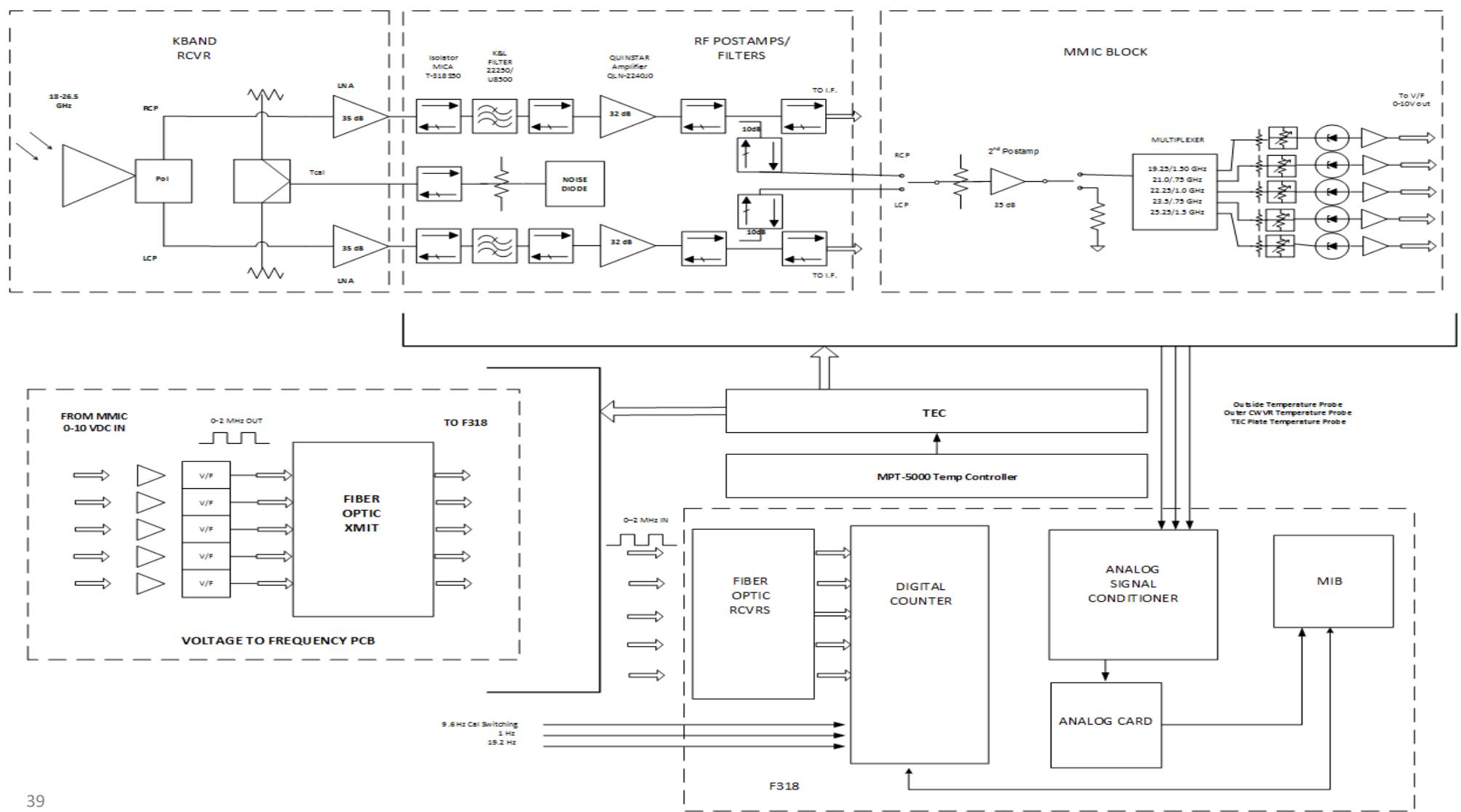
- $\Delta T \propto \Delta P_{in} = w_1 P_1 + w_2 P_2 + w_3 P_3 + w_4 P_4 + w_5 P_5$
 - $w_1 = 0.25, w_2 = -0.5, w_3 = 1, w_4 = -0.5, w_5 = 0.25$
 - $\sim 35 \mu\text{m}$ of WV $\longrightarrow 220 \mu\text{m}$ of electrical path delay ($\lambda/30$ for $\lambda = 7 \text{ mm}$)
 - For $\Delta T_{rms} \sim 25 \text{ mK}$, $T_{i,rms} \sim 19.612 \text{ mK}$
 - For $T_{sys} = 50 - 100 \text{ K}$, $\tau = 2.5 - 10^3 \text{ seconds}$
 - $\Delta g / g \sim 2.5 - 5 \times 10^{-4}$ $\Delta g_i / g_i \sim 1.96 - 3.92 \times 10^{-4}$
- Observable
 Individual Channel

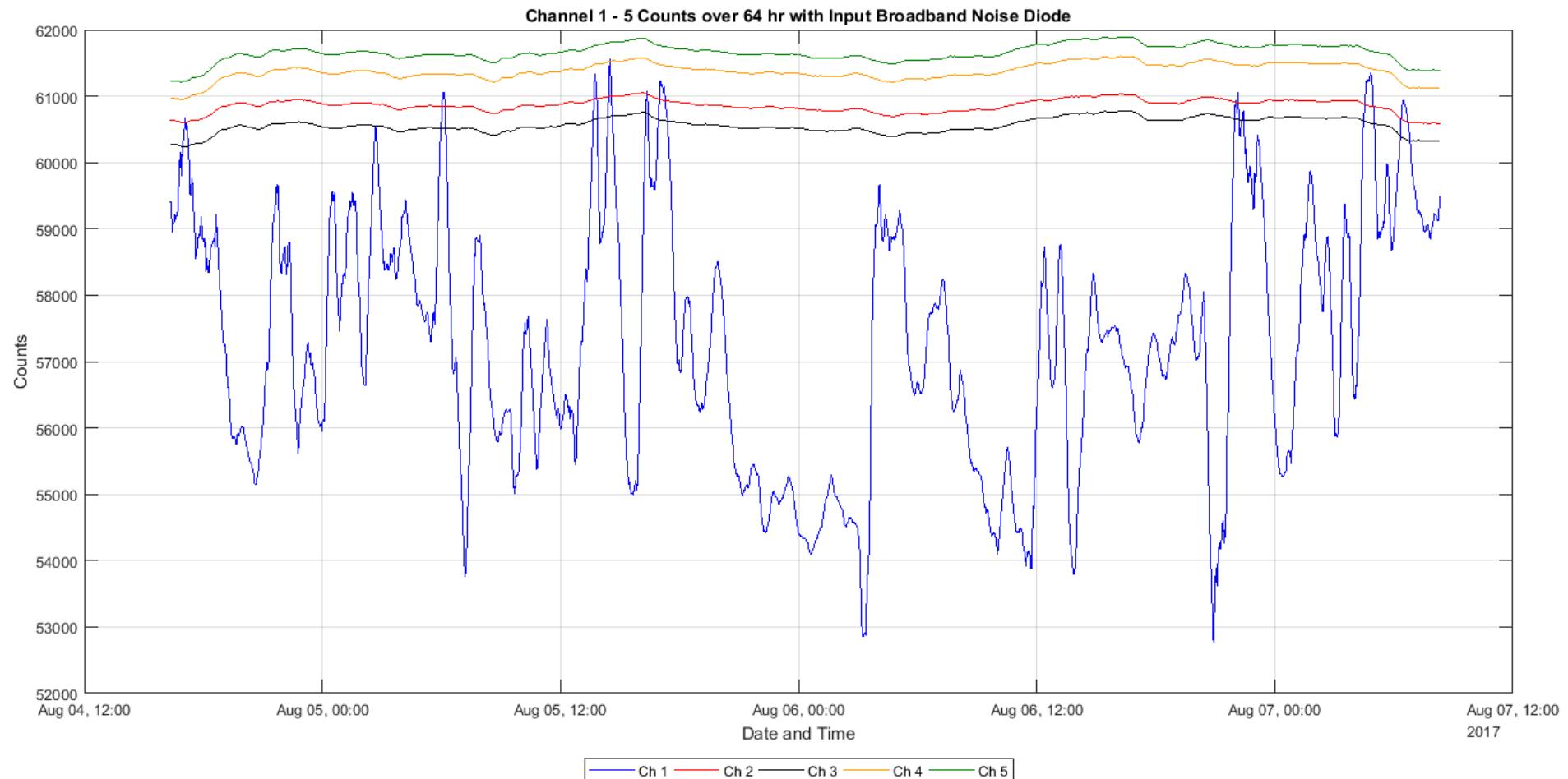
- Channel Isolation Requirements (5 Channels)

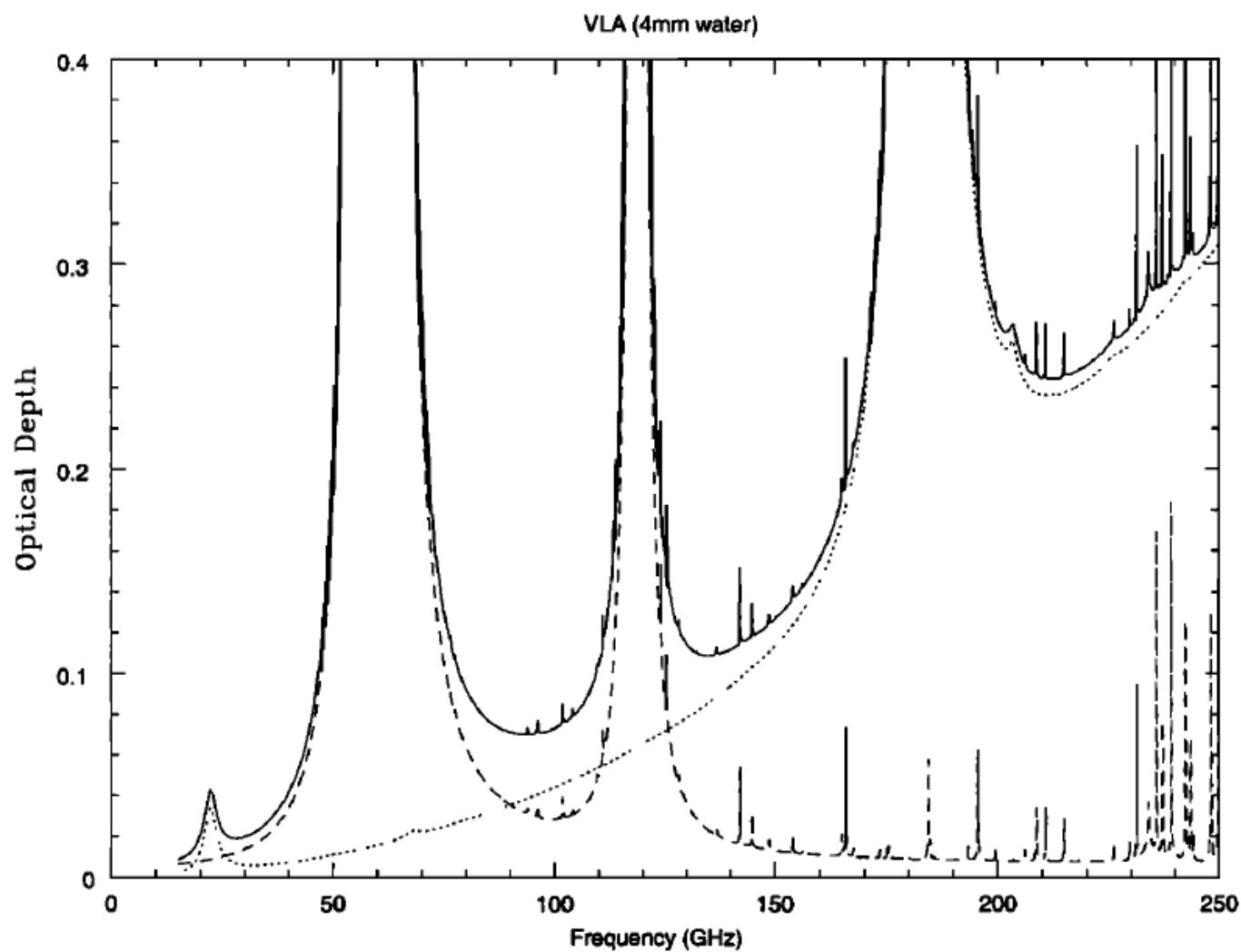
- $\sim -20 \text{ dB}$
- $\sim 1\%$ power leakage between any two channels

	v (low) (GHz)	v (center) (GHz)	v (high) (GHz)	Δv (GHz)
Ch1	18.5	19.25	20	1.5
Ch2	20.625	21	21.375	0.75
Ch3	21.75	22.25	22.75	1
Ch4	23.125	23.5	23.875	0.75
Ch5	24.5	25.25	26	1.5









$$Count_{corr,i} = \begin{cases} Count_i & \text{for } i = 1, 2, 3, \dots, n \\ Count_i - A(T_{sm,i} - T_{ave}) & \text{for } i = n+1, n+2, \dots, N \end{cases} \quad (23)$$

$$T_{ave} = \frac{1}{n} \sum_{i=1}^n T_i \quad (24)$$

$$T_{sm,i} = \frac{1}{n} \sum_{j=i-n}^i T_j \quad (25)$$

where $A = -405$, $Count_{corr,i}$ is the temperature corrected count at point i , $Count_i$ is the measured count at point i , T_{ave} is the mean of the CWVR ambient temperature for the first n seconds of a N -second total observation time, $T_{sm,i}$ is the temperature at point i taken as the mean from the preceding n seconds to point i , and T_j is



AD590, TCS620 (Cold Plate)